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ABSTRACT

In the application of efficient materials, including spintronics devices, magnetic field sensors, storage devices, and waste heat energy recovery systems, the anomalous transport phenomena play a crucial role. The anomalous transport, including the AHE and ANE are driven by ¹Berry curvature, which is a geometrical property of SOC electronic bands in the magnetic materials. The Present study utilized the ab-initio calculation method to explore the AHE and ANE in the Co₂CrAs and Co₂CrSb types of Co-based Ferromagnetic Heusler alloys, with magnetic moment of 5 μ_B . The net magnetization oriented along the [001] direction, the major Berry curvature originates from specific electronic states lying at the Fermi energy in the bandstructure under the SOC effect. The overall large Berry curvature further leads to the large AHC and ANC with values 584.38 (-668.99) Scm^{-1} and -4.71 (-2.68) $\text{Am}^{-1}\text{K}^{-1}$, for Co₂CrAs (Co₂CrSb) Heusler alloy. The pronounced anomalous transport responses obtained for Co₂CrAs and Co₂CrSb Heusler alloys suggest that these materials could serve as promising candidates for emerging quantum technologies and thermoelectric applications.

CHAPTER 1

INTRODUCTION

Over the last decade, the material science community has shown growing interest in materials with strong Anomalous Transport behaviour driven by their applicability in spintronics, energy conversion, sensing, and quantum devices [1–3]. Anomalous transport phenomena primarily encompass the AHE and the ANE, both of which arise independently of the conventional Lorentz-force mechanism associated with an external magnetic field [4]. The AHE is results of the appearance of a transverse voltage generated by a longitudinal charge current as a consequence of intrinsic magnetization.

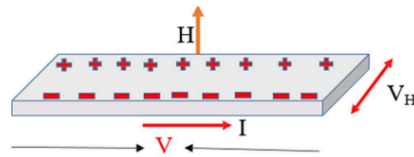


Figure 1: Anomalous Nernst effect (ANE)[9].

In contrast, ⁶the ANE represents the thermoelectric analogue of the AHE, where a temperature gradient in a magnetic material produces a transverse electrical response [5].

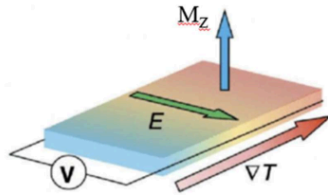


Figure 2: Anomalous Nernst effect (ANE)[9].

Despite the traditional Seebeck effect-based thermoelectric (TE) phenomenon, ANE based TE device overcomes the limited device connection complications and also provides large TE efficiency [1,6,7]. AHE and ANE are most popular Anomalous Transport Phenomena, which are exciting because their origin is internal magnetic field instead of external magnetic field. A quantum transport phenomenon where electric current flows through magnetic material, giving a perpendicular voltage without applying an external magnetic field, is known as the AHE [36,37], Which is differ from the conventional Hall effect. This phenomenon arises due to magnetism's complex interplay, spin-orbit coupling, and scattering mechanism. The fundamental microscopic mechanism underlying anomalous transport phenomena remains an active topic of investigation. The foundation of AHE origin was first mentioned in the work of Karplus and Luttinger in the 1905s, which describes intrinsic contributions that do not depend on scattering and extrinsic mechanisms introducing asymmetrical impurity scattering [6,3 6,38]. Within the Karplus–Luttinger framework, these effects are explained as intrinsic responses originating from spin–orbit coupling and spontaneous magnetization, mediated by the Berry curvature of the electronic band-structure [8,9]. Berry curvature is a geometric characteristic of coupled electronic

bands that behaves like an effective magnetic field in momentum space and plays a central role in generating anomalous transport responses [10]. It changes sign under time-reversal symmetry while remaining invariant under spatial inversion. Consequently, a finite net Berry curvature can arise only when time-reversal symmetry, inversion symmetry, or both are broken [11]. Magnetic materials naturally exhibit the TRS breaking, and the non-centrosymmetric systems have breaking IS, which might be the ideal candidate for the study of the Anomalous transport phenomena [12,13].

1.1 Literature review

Quantum phenomena like Anomalous Transport phenomena (ATP) have attracted researcher due to huge application in spintronics, Sensors And quantum technologies. Initially, scientists believed that this phenomenon was directly proportional to the magnetization of material, but recent theory says that they originate from the Berry curvature of electric bands near the Fermi levels [38]. This effect was observed in many materials, and topological materials are potentially remarkable [40].

In this sequence, Nagaosa et al. [4] predicted a giant anomalous hall transport in magnetic materials. His work clarified role of berry curvature in calculating hall conductivity. Further Xiao et al. [5] confirmed in momentum space Berry curvature is an effective magnetic field, which influences electron transport in materials. Berry curvature had many unconventional transport responses due to which this is one of the important factors to explore topological properties of materials. As it remains invariant under inversion symmetry, and change sign under time-reversal symmetry,

finite Berry curvature require breaking of at least one or both symmetries. Therefore, magnetic and non-centrosymmetric compounds are ideal system for anomalous transport phenomenon.

Heusler alloys are one of the promising candidate which show topological property like Anomalous Transport property due to their half-metallicity, large Curie temperature and large spin polarization. Many research work of scientists have reported huge AHC and ANC in Co-based Heusler alloys driven by Berry curvature.

Guin et-al, experimentally explore the AHC and the ANC of ferromagnetic Heusler alloys, their work mainly focused on Berry curvature near fermi level generate high transport coefficients. And magnitude of the AHC and the ANC depend on electronic topology[17].

While Noky et al. predicted Berry-Curvature-driven transport behaviour of many magnetic alloys by first- principle. The conclusion of their work is topological band and Weyl nodes crossing near fermi-level show better transport properties. And focus on importance of symmetry breaking and spin-orbit coupling to generate large Berry curvature[19].

Several study have done to explore transport properties in Co-based Heusler Alloys. Kakti et al. predict magnetic properties and topological properties in Heusler Alloys and reported that transport response depend on electronic band structure. Chatterjee et al. study of magnetic system demonstrate that Berry curvature distribution can be enhanced by breaking of symmetry[20].

Wang et al. thoroughly studied the existence of nodal lines and the Weyl points in the Co_2ZrSn full Heusler system using first-principles calculation [61]. Co_2MnGe Heusler

alloy has been predicted to exhibit the multiple Weyl cone in the band structure [62]. Chang et al. analysed the nodal line and Weyl points in the Co_2TiX ($X = \text{Si}, \text{Ge}$ or Sn) using the first principles calculation [63]. Recently, a giant AHC of about 1600 S/cm has been observed in the Co_2MnAl ferromagnetic topological semimetal [64]. This large AHE in Co_2MnAl is attributed to the presence of nodal rings and Weyl points near the Fermi energy. Another well-known system is Co_2MnGa Heusler alloy which is reported to show large AHC and ANC about 1200 S/cm and 4.0 A/m-K due to the gapped nodal lines near the Fermi energy [65]. The large AHE and ANE are theoretically reported in the Co_2FeGe Heusler alloy above 100 meV to the Fermi level due to the SOC-induced nodal line symmetry breaking [66, 67]. Very recently, our group theoretically predicted a large AHC of about 1000 S/cm in the Cu_2CoSn , where the gapping in the nodal line creates large Berry curvature at the Fermi surface [68]. Considering the potential of the Co-based Heusler alloys as the topological semimetal with large anomalous transport response, high Curie temperature, and high-spin polarization, makes these systems potential candidates for spintronic applications [69, 70, 71]. These materials carry the magnetic properties without any magnetic entity, which makes them a possible candidate for the study of Anomalous transport. Heusler alloys are classified as Half Heusler and Full Heusler alloys based on their chemical composition. If the composition is XYZ with a 1:1:1 stoichiometry, then it's a Half Heusler alloy, and if X_2YZ with a 2:1:1 stoichiometry, where the transition metals are X and Y, and Z is a main group element [16]. Recently, Guin et al. experimentally and theoretically predicted a giant AHC and ANC in a Co-based Full Heusler alloy [17]. Although numerous studies on magnetic Heusler alloys exist in the literature, only a

limited number address the TRS breaking criterion linked with Berry curvature and the associated anomalous transport behaviour [13,18–25].

We are interested in investigating Co-based Heusler alloys, focusing on topological semimetals for large anomalous transport responses. The Berry curvature arising from the topologically protected bands in these materials leads to pronounced anomalous Hall and Nernst effects. The AHE holds potential for spintronics applications, such as nanoscale read head sensors, high-frequency Hall sensors, memory devices, etc. Additionally, the ANE could enable more efficient conversion of heat into electricity compared to traditional thermoelectric materials.

Co_2CrAs and Co_2CrSb are types of Co-based magnetic full Heusler alloys, which were theoretically predicted both materials as Ferromagnetic half Metallic system by Kanbur et al. [26]. However, some other studies also present in the literature on these alloys consider only the effect of pressure and temperature, and mostly are focused on the half-metallic feature [27,28]. But no one has yet explored their Anomalous transport behaviour, led by the Berry curvature feature. To fill this gap, motivated by this, this study systematically presents a computational prediction of the Berry curvature-driven AHE and ANE in the Magnetic Heusler alloys.

CHAPTER 2

METHODOLOGY

The study of Anomalous Transport properties was done using DFT-based first-principles calculations. The calculations were performed using VASP with the projector augmented wave (PAW) method and generalized gradient approximation (GGA) for exchange-correlation effects [48]. Structural optimization was followed by analysis of mechanical stability through the calculation of elastic constants. Electronic properties were studied by calculating band structures and density of states. To examine topological characteristics, spin-orbit coupling (SOC) was included in band structure calculations. The anomalous transport properties were calculated via Wannier charge center evolution by employing Wannier90 and WannierTools [49,50]. All computational tools employed in this study include VASP, Wannier90 and Wannier tool. In the following sections, the computational methods and packages are discussed in detail.

2.1 Density Functional Theory (DFT)

The density functional based method is one of the most popular theoretical methods for electronic properties of materials at the atomic level. It is the backbone of contemporary computational condensed matter physics and material science. The approach is the principle that ground-state of an interacting many-electron system can be fully specified by its electron density, as opposed to the complicated many-body wave function. The basic thought behind this method is the mapping of a complicated many-body problem into an easier one by taking recourse to a system of non-

interacting electrons that have the same electron density as the interacting system in question. This mapping considerably eases the computational complexity at the expense of none of the important physics. This theoretical concept became feasible with the advent of the Kohn-Sham (KS) formulation, which gives a means to solve for the ground-state electron density through the use of self-consistent field methods. The KS equations are a collection of single-particle equations that are simpler to solve numerically. The validity of this approach is highly dependent on the proper modelling of the exchange-correlation energy, a phrase that describes the quantum mechanical interactions between electrons, such as their mutual repulsion and quantum exchange effects. In the KS version of DFT, the many-electron problem of interacting electrons is solved by a set of non-interacting electrons defined in terms of the following self-consistent equations:

$$-\frac{\hbar^2}{2m} \nabla^2 + V_{\text{eff}}(\mathbf{r}) \Psi_i(\mathbf{r}) = \epsilon_i \Psi_i(\mathbf{r}) \quad (2.1)$$

Here $\Psi_i(\mathbf{r})$ are the KS orbitals, ϵ_i - the associated eigenvalues and $V_{\text{eff}}(\mathbf{r})$ - the effective potential, given by:

$$V_{\text{eff}}(\mathbf{r}) = V_{\text{ext}}(\mathbf{r}) + V_{\text{H}}(\mathbf{r}) + V_{\text{xc}}(\mathbf{r}) \quad (2.2)$$

Here $V_{\text{ext}}(\mathbf{r})$ - external potential, $V_{\text{H}}(\mathbf{r})$ - the Hartree Potential and $V_{\text{xc}}(\mathbf{r})$ - the exchange correlation potential. The electron density is derived from Kohn-Sham orbitals as:

$$n(\mathbf{r}) = \sum_i^{\text{occ}} |\Psi_i(\mathbf{r})|^2 \quad (2.3)$$

These equations are then solved iteratively until self-consistency is established that is, until input and output electron densities agree. Over the last few decades, the

density functional based method has been extremely successful in the prediction of a broad spectrum of material properties such as structural stability, electronic band structure, magnetic ordering, and even topological features. It is especially useful for the investigation of new materials like topological insulators, superconductors, and thermoelectric, where experimental information can be scarce or hard to obtain [51].

2.2 Exchange correlation functionals

The exchange-correlation functional is the key ingredient in DFT. It embodies the combined impact of exchange and correlation electron interactions that are two quantum mechanical effects that are difficult to represent accurately. As the precise form of this functional is not known for the majority of real systems, several approximations have been formulated to render DFT computationally useful. The way the electron density and its spatial fluctuation are treated in these approximations varies, leading to a range of functionals with different strengths and limits. The LDA, GGA are the most commonly utilized forms. Each has particular uses depending on the kind of system being studied.

2.2.1 Generalized Gradient Approximation(GGA)

The GGA is a development beyond LDA in that the electron density at every point and how it varies in space are taken into account. This permits GGA functionals to have a more realistic description of the behaviour of inhomogeneous electron systems, such that they can be more accurately used for molecules, surfaces, and transition metal oxides. GGA fixes many of the deficiencies of LDA, making more accurate predictions

of lattice parameters, cohesive energies, and magnetic properties. The most popular GGA functionals are the Perdew-Burke-Ernzerhof functionals [52]. GGA is usually regarded as the norm for most solid-state DFT calculations because it provides a good balance between accuracy and computational expense.

¹⁰ **Perdew-Burke-Ernzerhof**

The PBE functional is among the most popular GGA functionals. It is an improvement over the LDA since it includes the gradient of the electron density, enabling it to better handle inhomogeneities. In this study, PBE was selected for the exchange-correlation potential because of its compromise between computational cost and structural and electronic property reproduction accuracy. PBE is particularly accurate for the study of semiconductors and transition metal compounds, and is used in most conventional DFT codes, such as VASP [48].

2.3 Computational packages

2.3.1 VASP

The VASP is a tool employed for conducting quantum mechanical calculations. This involves the use of PAW, coupled with a plane wave basis set [48]. VASP solves ¹² the many-body Schrödinger equation approximately by solving the KS equation (in the framework of DFT) or by solving the Roothaan equations (in the framework of the Hartree-Fock approach). Additionally, certain hybrid functionals that inherit aspects from both the Hartree-Fock approach and the DFT are also available [53]. VASP calculates key quantities through a plane wave basis: single-electron orbitals, charge density, and local potential. The

exchange the electrons and ions is either expressed with the help of the ¹⁰PAW method or with the help of norm-conserving or ultrasoft pseudopotentials [48].

VASP carries out calculations using 4 necessary input files, which are

- **INCAR:** This file is used to determine what kind of calculation has to be done on the investigated system. There are certain tags specified in the INCAR file which we have to set to select a certain algorithm and set the parameters.
- **POSCAR:** This file gives the details of the system that we study. It consists of the atomic positions in the unit cell and the translational vectors.
- **POTCAR:** This file consists of the pseudopotential for every single atomic species which is present in Mendeleev's.
- **K-point sampling:** A crystalline solid is composed of unit cells with a periodic arrangement of atoms. The solid is initially transformed into a supercell with several unit cells to handle the full solid. After the supercell is expanded to infinity using the periodic boundary conditions, it is transformed into reciprocal space contained within the first Brillouin zone (BZ). We can further compress the BZ by using symmetry operations to transfer the entire solid to the irreducible Brillouin zone (IBZ). An endless number of wave functions can be produced by using k-vectors to represent the points in an IBZ. Each k-point contains information about the kinetic energy, direction, and amplitude of the wave vector at that specific location. Since it is nearly impossible to take into account every k-point, DFT computations employ a small number

of k-points utilizing the following schemes:

- Monkhorst-Pack method: ³ In order to determine the ground state energy, which is converged in DFT calculations for each system, Monkhorst and Pack presented a method in 1976 to create a homogeneous mesh of k-points sampled throughout the whole IBZ[19].
- Γ -point: A large supercell can be fully described by a single point, which is described as Γ -point. Since it is the place where real and reciprocal spaces coincide, a real wave function will be employed [20,21].

2.3.2 Wannier90

Wannier90 is an open-source tool designed to construct maximally localized Wannier functions (MLWFs) from DFT outputs [49]. In this study, it played a crucial role in generating a tight-binding Hamiltonian that accurately reproduces the ab initio band structure, particularly near the Fermi level. The process started with the wannier.win file which defines the projections, number of bands, frozen and disentangled energy windows, and other parameters necessary for Wannierization. The wannier.eig file provided the band eigenvalues of VASP, while the wannier.mmn and wannier.amn files contained matrix elements and projection overlaps, respectively. These were necessary for the localization process and the formation of MLWFs. The output Wannier functions maintained the symmetry and character of the initial atomic orbitals but were spatially localized, which is very important in investigating topological properties.

2.3.3 WannierTool

WannierTools is a versatile software package employed to investigate the topological properties of materials based on tight-binding models extracted from Wannier90 [54]. In this paper, WannierTools was used to compute the BC, AHC and ANC. The fundamental input to these calculations is the wt.in file that sets a variety of computational parameters.

2.4 Summary

The study employed DFT using the VASP code with the PAW method and the PBE form of the GGA for exchange-correlation effects. Structural optimization, elastic constants, and electronic properties were evaluated, with SOC included to analyze topological features. Wannier90 was used to generate maximally localized Wannier functions and construct tight-binding models. WannierTools facilitated the computation of Anomalous transport properties. The methodology integrates electronic structure analysis and anomalous conductivities calculations through VASP, Wannier90, and WannierTools.

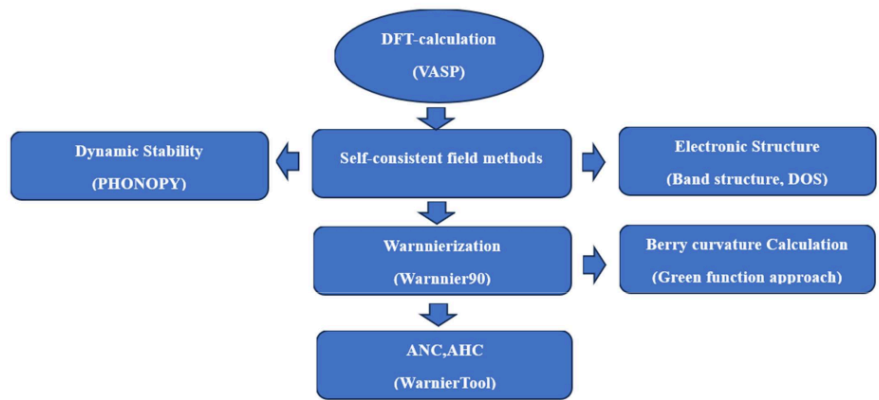


Figure 3: Schematic representation of the DFT-based workflow.

CHAPTER 3

BERRY CURVATURE DRIVEN ANOMALOUS TRANSPORT BEHAVIOUR IN FERROMAGNETIC HEUSLER ALLOYS

3.1 Introductions

In recent years, the material science community has shown growing interest in materials with strong Anomalous Transport behaviour driven by their applicability in spintronics, energy conversion, sensing, and quantum devices. Anomalous Transport Phenomena mainly include the AHE and ANE, which are not driven by the Lorentz force in an external magnetic field. The AHE is results of the appearance of a transverse voltage generated by a longitudinal charge current as a consequence of intrinsic magnetization. On the other hand, ANE is thermoelectric counterpart of AHE, which is characterised as a longitudinal current govern by temperature gradient in the magnetic materials. Despite the traditional Seebeck effect-based thermoelectric (TE) phenomenon, ANE based TE device overcomes the limited device connection complications and also provides large TE efficiency. The microscopic origin of the anomalous transport phenomena is not fully understood; however, the Karplus–Luttinger (KL) mechanism attributes it to intrinsic magnetism and spin–orbit coupling (SOC) through the BC of the electronic bands. BC is a geometrical property of entangled electronic bands, which acts as a fictional magnetic field, and is responsible for the anomalous transport. It is odd under the time reversal operation and even under the IS operation. Therefore, to obtain a resultant non-zero BC, one needs to break either TRS or IS or both. Magnetic materials naturally exhibit the TRS breaking, and the non-centrosymmetric systems have breaking IS, which might be the ideal candidate for the

study of the Anomalous transport phenomena. Numerous studies on magnetic Heusler alloys exist in the literature, only a limited number address the TRS breaking criterion linked with Berry curvature and the associated anomalous transport behaviour. Co_2CrAs and Co_2CrSb are types of Co-based magnetic full Heusler alloys. Rai et al. theoretically predicted both materials as Ferromagnetic half Metallic system. However, their Anomalous transport behaviour, led by the Berry curvature feature on these materials, is unexplored yet. To fill this gap, motivated by this, this study systematically presents a computational prediction of the Berry curvature-driven **AHE** and **ANE** in the Magnetic Heusler alloys.

¹² 3.2 Computational Details

The first-principles calculations were performed ¹ to investigate the electronic, magnetic, Topological and transport properties of Heusler alloy. Density functional theory (DFT) is used which is implemented in ⁵ the Vienna ab initio simulation package (VASP), employing the projector augmented-wave (PAW) method [34-36]. Further, the exchange-correlation effects were treated within the generalized gradient approximation (GGA+U) using the Perdew-Burke-Ernzerhof (PBE) functional, where calculated Hubbard U and exchange J parameters were approximately 3.94 and 0.81 eV for cobalt (Co), [37]. In order to perform spin-polarized calculations and structural optimization, a convergence criterion for the self-consistent field energy of 10^{-5} eV ² was set. For the plane wave basis, the energy cut-off value was set to 520 eV. A fully optimized Γ -centred k-mesh grid of $11 \times 11 \times 11$ was used. For a full relativistic approach, we also include the effect of spin-orbital coupling and consider magnetisation along (001) plane. Further, using maximally localized Wannier

functions (MLWFs), we constructed a tight-binding Hamiltonian by Wannier90 code. The WannierTools package was used to calculate the transport properties and identify the Weyl nodes within the bulk electronic structure, as well as the surface Fermi arc, thereby confirming the topological nature of the system [38]. In addition, the Berry curvature distributions are calculated using the Kubo formulation as given equation 3.1. The AHC and ANC were evaluated using WannierTools with a dense $200 \times 200 \times 200$ k-mesh for high precision using the given equations 3.2 and 3.3, respectively [40,14].

3.3 Structural Properties

The structural properties, including stable structural phase and lattice constant for Co_2CrAs and Co_2CrSb Heusler alloys, are computed by the structural optimization curve. Heusler alloys with the chemical formula X_2YZ typically crystallize in the cubic $L2_1$ structure (AlCu_2Mn prototype), where X and Y refer to transition-metal elements, and Z refer to groups III, IV, or V of the periodic table. The $L2_1$ phase is centrosymmetric, meaning it preserves inversion symmetry. In this arrangement, the X atoms occupy the (0.25, 0.25, 0.25) and (0.75, 0.75, 0.75) Wyckoff sites, while the Y and Z atoms reside at (0.5, 0.5, 0.5) and (0, 0, 0), respectively, as illustrated in Fig. 1(a) and (b). However, another structural phase also exist in the X_2YZ stoichiometry, with the similar Wyckoff positions, which can be achieved by replacing one X atomic position with the Y atom, in the $L2_1$ structure and vice versa [33,34]. Fig. 1 (c) and (d) curve represents the variation in ground state energy of a conventional unit cell with respect to the lattice constant. For Co_2CrAs and Co_2CrSb , the calculated energy separation

between the L2₁ and Xa structural configurations is 0.87 eV and 3.49 eV, respectively. These values demonstrate that, in both compounds, the L2₁ structure is energetically more favourable than the Xa phase. Further, the optimized lattice constant correspond to the minimum energy are found to be 5.78 Å and 6.00 Å for Co₂CrAs and Co₂CrSb Heusler alloys, respectively, which is well in **agreement** with the **previously reported results**, also listed in Table I [26–28,35]. Due higher energetic stability in L2₁ phase over Xa, we consider L2₁ structural phase for all further calculations.

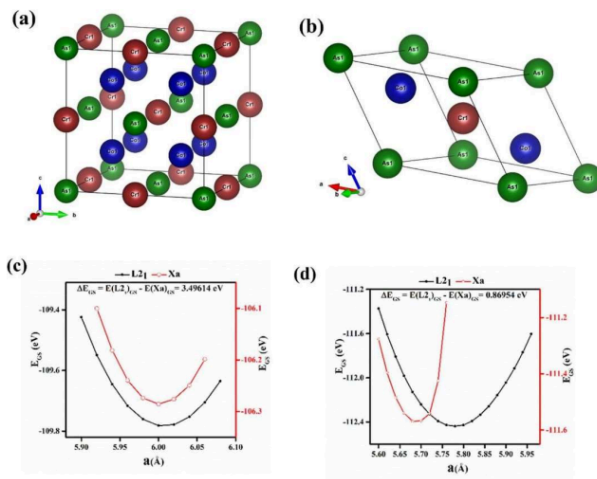


Figure 4:(a) Conventional unit cell of the Co₂CrZ (Z = As, Sb) Heusler alloys containing 16 atoms, with four atoms of each constituent element. (b) Corresponding primitive unit cell comprising four atoms, one from each element. (c) and (d) the phase stability optimization curve in both L2₁ and Xa phases, between Ground state energy

(EGS) with varying lattice constant a (Å) for Co_2CrAs and Co_2CrSb Heusler alloys respectively.

Table 1: Optimizes Lattice constants a (Å) and total magnetic moment (μB) for Co_2CrAs and Co_2CrSb Heusler alloy.

Heusler Alloy	Lattice constant a (Å)	Total magnetic moment (μB)
Co_2CrAs	5.78 [*] , 5.78 [#] , 5.81 [@] , 5.79 [§]	5.00 [*] , 5.00 [#] , 4.82 [@] , 5.01 [§]
Co_2CrSb	6.00 [*] , 6.00 [#] , 5.99 ^δ	5.00 [*] , 5.00 [#] , 4.94 ^δ

*this work, [#][26], [@][27], [§][35], and ^δ[28]

To ascertain the dynamic stability of the structures in the L21 phase, we also performed a calculation of phonon dispersion for both alloys. As illustrated in Fig. 2, the phonon dispersion bands are plotted against ¹³the high symmetry path Γ -X-U/K- Γ -L-W-X in the BZ. The phonon dispersion spectra carrying the total 12 phonon branches corresponding to the four atoms per unit cell as shown in Figure 2(a) and (b) for Co_2CrAs and Co_2CrSb Heusler alloys. For these alloys, we do not observe any negative frequency phonon branches, which ensure the dynamical stability of both Heusler alloys in the magnetic phase.

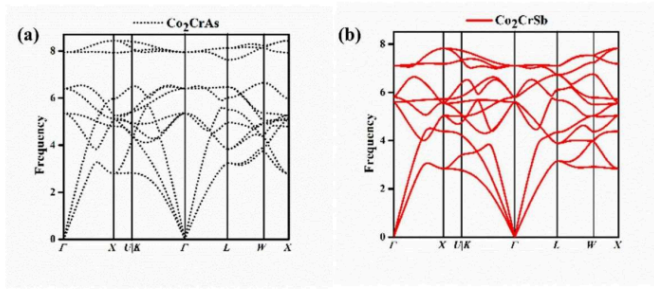


Figure 5: Phonon dispersion spectra along the high- symmetric k-path for (a) Co_2CrAs and (b) Co_2CrSb Heusler alloys.

3.4 Electronic, Magnetic, and Topological properties

To compute the magnetic nature and half-metallicity, the spin-polarized Density of states (DOS) and electronic bandstructure are calculated for both alloys. Fig. 3(a and b) display the total and partial DOS plot, which shows that the main Co-d, Cr-d, and As/Sb-p orbitals contribute near the Fermi level in both spin channels. In addition, the absence of electronic states at the Fermi level in the minority spin channel indicates the half-metallic nature of both Heusler alloys. Fig.3 (c and d) illustrates the spin-polarized electronic bandstructure for the Co_2CrAs and Co_2CrSb Heusler alloys, respectively. The minority spin states exhibit a clear semiconducting energy gap of value 0.39(0.28) eV for Co_2CrSb (Co_2CrSb) alloy. However, ¹ the majority spin states cross E_F and form a conducting channel between conduction and valence bands, which further confirms the half-metallic nature of both alloys. In addition to evaluating the magnetic properties of the

alloys, we also calculate the magnetic moment against all atoms present in the unit cell. Both the alloys exhibit ferromagnetic behaviour with a net magnetic moment value of 5 μ_B , which is also given in Table 1, and compared with the previously reported results.

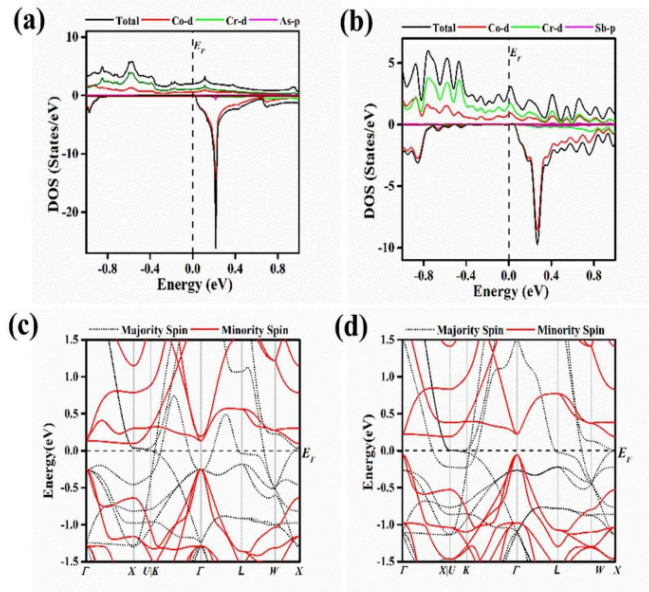


Figure 6: Spin Polarized total and partial Density of states (DOS) for (a) Co₂CrAs and (b) Co₂CrSb. Spin Polarized electronic bandstructure along the high symmetry k-path, for (c) Co₂CrAs and (d) Co₂CrSb Heusler alloys.

3.5 ² Berry Curvature, Anomalous Hall and Anomalous Nernst

Effect

Berry curvature analysis characterizes the geometrical (Berry) phase associated with electronic wave-functions in momentum space and is described by the phase shift acquired by a wave-function during cyclic evolution in k-space. It is evaluated using the Kubo formalism in conjunction with a ¹ tight-binding Hamiltonian constructed from the Wannier90 code, and can be expressed as follows [10,36,37]:

$$\Omega_{ij}^n(k) = \sum_{n \neq m} \frac{\langle n | \frac{\partial H}{\partial k_i} | m \rangle \langle m | \frac{\partial H}{\partial k_j} | n \rangle - (i \leftrightarrow j)}{(E_n - E_m)^2} \quad (3.1)$$

Where $\Omega_{ij}^n(k)$ is Berry curvature ij component of the n th band. ϵ_n and ϵ_m are ¹ the energy eigenvalues of the Hamiltonian H corresponding to the $|n\rangle$ and $|m\rangle$ eigenstates, ¹ respectively, the energy eigenvalue of the Hamiltonian H .

Fig. 4 displays the electronic band structures (upper panels) and the corresponding Berry curvature distributions (lower panels) for Co_2CrAs and Co_2CrSb Heusler alloys in the presence of SOC. When SOC is included, spin ceases to be a good quantum number, and the two spin channels must be treated collectively. Around the E_F , SOC take care of the band degeneracy and induces energy gaps between previously degenerate bands over a narrow k-path region. These SOC-split bands contribute

significantly to the Berry curvature when one of the split bands is occupied, and the other remains unoccupied. In contrast, pairs of states that are either both occupied or both unoccupied provide only a minor contribution to the overall Berry curvature [15,35,43–46].

Fig. 4(a) shows the Berry curvature profile for Co₂CrAs, where a pronounced peak and several weaker features are observed along the k-path (lower panel). To identify the initial phase of these peaks, an enlarged of the SOC-included band structure near E_F is presented alongside the Berry curvature. The dominant peaks arise from SOC-induced energy gaps between nearly degenerate electronic bands within a narrow k-region, as clearly seen in the enlarged view of Fig. 4(b). The smaller peaks share a similar origin; however, their smaller magnitude is attributed to comparatively larger energy separations between the interacting bands as from equation 1. Additionally, the small dip in Berry curvature around the Γ point results from aligned electronic states that are both occupied, leading to a suppressed Berry curvature amplitude.

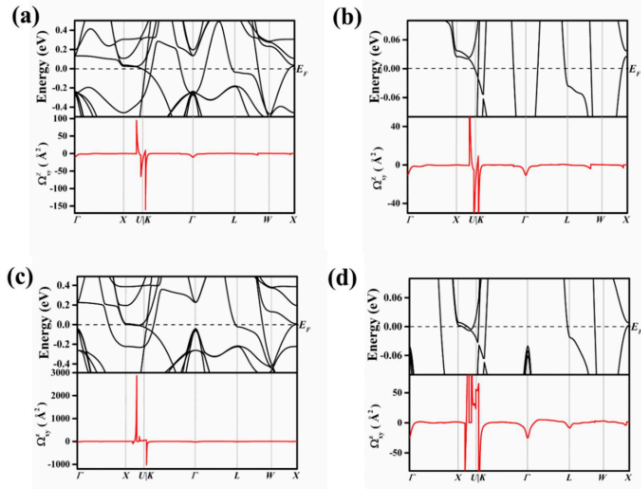


Figure 7: (a) Berry curvature feature (bottom channel) ² corresponding to electronic band-structure (lower channel) with SOC along the high-symmetry k-path for (a) Co₂CrAs and (c) Co₂CrSb. (b) and (d) is the magnified view of Berry curvature with bandstructure for (a) Co₂CrAs and (c) Co₂CrSb Heusler alloys, respectively.

For Co₂CrSb, as illustrated in Fig. 4 (c), three prominent peaks are observed, one positive and two negatives. These major Berry curvature peaks originate from SOC-induced energy gaps between electronic states near E_F within a confined k-region. The enlarged view in Fig. 4(d) reveals a minor dip near the Γ point with relatively small magnitude, which arises from electronic states situated below E_F that remain occupied. A comparison between the two alloys indicates that Co₂CrSb exhibits larger Berry curvature peaks than Co₂CrAs. This difference is attributed to the position of the SOC-gapped electronic states: in Co₂CrSb, these states lie directly at E_F , whereas in Co₂CrAs

they are positioned slightly above E_F , resulting in a comparatively weaker Berry curvature response.

Next, the AHC (σ_{xy}^A) is determined from the Berry curvature $\Omega_{ij}^n(k)$ using the following expression [47,48]:

$$\sigma_{xy}^A = \frac{-e^2}{h} \int_{BZ} \frac{d^3k}{(2\pi)^3} f(k) \Omega_{ij}^n(k) \quad (3.2)$$

The AHC for both Heusler alloys was calculated using Eq. 2 and ²plotted as a function of energy within ± 1000 meV around the E_F , as shown in Fig. 5(a). For Co_2CrAs , the AHC is $-309.67 \text{ S cm}^{-1}$ at fermi-energy and reaches a maximum of 584.38 S cm^{-1} at 0.13 eV above E_F , which is approximately 1.8 times larger than its value at E_F . Similarly, for Co_2CrSb , the AHC is $-167.26 \text{ S cm}^{-1}$ at fermi-energy and attains a maximum magnitude of $-668.99 \text{ S cm}^{-1}$ at 0.97 eV below fermi-energy, nearly five times greater than its value at the fermi-energy. Hence, a slight shift in the E_F can significantly enhance the AHC. Such a shift can be achieved through appropriate chemical doping or by applying lattice strain, thereby enabling larger AHC values. These negative AHC values indicate that regions of positive Berry curvature dominate

the overall response. These substantial values of AHC obtained for these Heusler alloys are comparable to previously reported results.

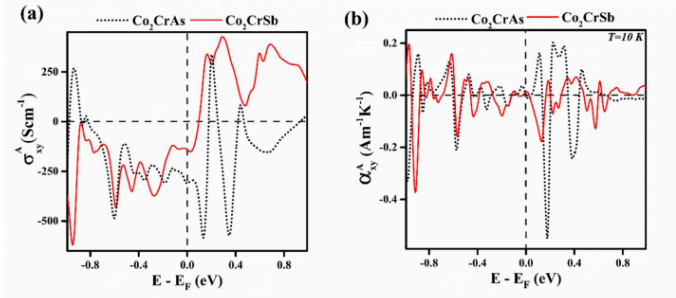


Figure 8: (a) Anomalous Hall conductivity with varying energy in the vicinity of Fermi level at 0 K and (b) Anomalous Nernst conductivity with varying energy in the vicinity of Fermi level at low temperature (10 K) for both Co₂CrAs and Co₂CrSb Heusler alloys.

Now AHC the thermoelectric counterpart, the ANC (α_{xy}^A), calculated as proposed by Xia et al. [4,54], can be expressed as:

$$\alpha_{xy}^A(T, \mu) = -\frac{1}{e} \int_{BZ} d\varepsilon \frac{\partial f(\varepsilon - \mu, T)}{\partial \varepsilon} \frac{\varepsilon - \mu}{T} \sigma_{xy}^A(\varepsilon) \quad (3.3)$$

And at low temperature, the Mott relation is used to calculate the ANC (α_{xy}^A), and can be obtained from AHC, as from the equation [10,55,56]:

$$\alpha_{xy}^A(T, \mu) = -\frac{\pi^2}{3} \frac{k_B^2}{e} \frac{\partial \sigma_{xy}^A}{\partial \varepsilon}(\varepsilon_F) \quad (3.4)$$

Where $f(k)$ stands for the Fermi-Dirac distribution function, k_B is the Boltzmann constant, μ is the chemical potential, \hbar is the reduced Planck constant, and integration is over the Brillouin zone. e is the electronic charge, and T is the actual temperature.

At low temperature ($T = 0$ K), the ANC calculated from the Mott relation given by equation 4, which is the energy derivative of the AHC. The ANC as a function of energy in the vicinity of E_F within ± 1000 meV for both alloys is shown in Fig. 5(b).

At $T = 10$ K, the Co_2CrAs alloy exhibits an ANC of $0.001 \text{ Am}^{-1}\text{K}^{-1}$ at E_F , which reaches a maximum value of $-0.55 \text{ Am}^{-1}\text{K}^{-1}$ at 0.17 eV above the E_F . Similarly, for Co_2CrSb , the ANC is $0.013 \text{ Am}^{-1}\text{K}^{-1}$ at E_F and attains a maximum of $-0.37 \text{ Am}^{-1}\text{K}^{-1}$ at 0.91 eV below E_F . These results indicate that even a slight shift in the chemical potential can lead to a substantial variation in the ANC.

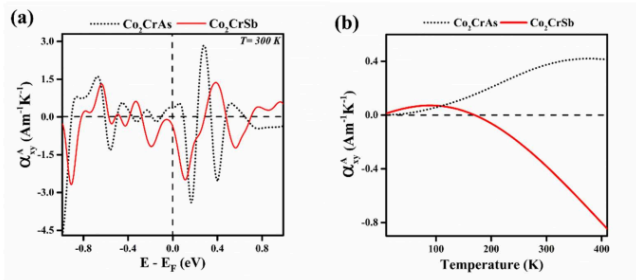


Figure 9: (a) Anomalous Nernst conductivity with varying energy in the vicinity of Fermi level at room temperature (300 K) and (b) Anomalous Nernst conductivity with the varying temperature at E_F for both Co_2CrAs and Co_2CrSb Heusler alloys.

For potential room-temperature applications, the ANC was further evaluated from equation 3 at $T = 300$ K, plotted in Fig. 6(a). At the E_F , Co_2CrAs and Co_2CrSb exhibit

ANC values of 0.37 and 0.38 $\text{Am}^{-1}\text{K}^{-1}$, respectively. Upon shifting the E_F to -0.99 eV for Co_2CrAs and -0.90 eV for Co_2CrSb , the ANC reaches maximum values of -4.71 and -2.68 $\text{Am}^{-1}\text{K}^{-1}$, respectively. These values are approximately 13 and 7 times larger than those at the E_F . The enhanced ANC observed in these Heusler alloys is comparable to previously reported results for other ferromagnetic Heusler compounds [12,19,50,57–59].

We further computed the temperature dependence of the ANC at the E_F , as shown in Fig. 6(b). For Co_2CrAs , the ANC increases monotonically with temperature, reaching 0.37 $\text{Am}^{-1}\text{K}^{-1}$ at 300 K. However, Co_2CrSb maintains comparable larger values than Co_2CrAs throughout the investigated temperature range and exhibits a parabolic behaviour, attaining a maximum of 0.82 $\text{Am}^{-1}\text{K}^{-1}$ at 400 K. The observed variation of ANC with increasing temperature can be attributed to the interplay between thermal broadening effects and sharply peaked features in the Berry curvature [60]

CHAPTER 4

CONCLUSIONS AND FUTURE SCOPE

4.1 Conclusion

The present study explored anomalous transport phenomena in the new Co-based ferromagnetic Heusler alloys, Co_2CrAs and Co_2CrSb , by utilizing the Density functional theory, followed by green function approach. These are half-metallic systems, stable in the $L2_1$ structural phase, and possess a net magnetic moment of value $5 \mu_B$. The total and projected density of states revealed that the d orbitals of Co and Cr atoms and the p orbitals of As/Sb atom are mainly contributed to both spin channels and in the conduction and valence bands near the E_F . The spin-orbital coupling removes the degeneracy of degenerate electronic bands, in which those lying at the E_F contribute to the resultant Berry curvature. The observed net non-zero Berry curvature in both alloys further leads to the large AHC and ANC results. We observed the AHC value at $T=0$ K about 584.38 Scm^{-1} and -668.99 Scm^{-1} for Co_2CrAs and Co_2CrSb Heusler alloy, respectively. Further, the ANC at low temperature appears to be very small, but at room temperature, we observed large values -4.71 and $-2.68 \text{ Am}^{-1}\text{K}^{-1}$ for Co_2CrAs and Co_2CrSb Heusler alloy, respectively. The variation in the ANC with the temperature is the consequence of the collective effect of thermal banding and sharply peaked Berry curvature. Our findings for anomalous transport led by the Berry curvature in the new Co-based ferromagnetic Heusler alloys, making them a potential candidate for thermoelectric and new emerging quantum technological applications.

4.2 Future Scope

This work presents theoretical understanding of the AHC and the ANC of Co_2CrAs and Co_2CrSb and opens many doors for future research. The theory people can explore the effect of external parameter as atomic disorder on electronic structure and chemical doping. This type of change can shift the Fermi energy level and can enhance Berry curvature, AHC and ANC. In other hand Experimentalist can synthesis and do characteristic of Co_2CrAs and Co_2CrSb to confirm theoretical prediction. X-ray diffraction (XRD), transport measurements, scanning electron microscopy (SEM), and magnetic characterization experimental techniques can be used to investigate structural stability, magnetic properties, and anomalous Hall and Nernst responses. In addition future studies can explore topological phase transitions, nodal line structures, Weyl nodes, and symmetry-breaking mechanisms in Co-based Heusler alloys. In an application perspective, experimentalist can investigate Heterostructure fabrication and thin film Growth for Practical Application in sensor, spintronics and quantum technology.

Recently, Artificial Intelligence (AI) and Machine Learning (ML) techniques are useful in material science. ML can predict electronic, magnetic, and topological properties of many Heusler compounds using material databases. This reduce computational cost and accelerate the discovery of materials having large anomalous Hall and Nernst Conductivity. Furthermore, deep learning can be used to identify new Heusler compounds with desirable Berry curvature. Such approaches will provide a faster way toward discovering next-generation materials for quantum, spintronic, and thermoelectric applications.

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