

# **Design and Analysis of Broadband Metamaterial Absorbers for Mid Infrared Applications**

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# Abstract

In this study, we present the design and analysis of a mid infrared metamaterial absorber based on a metal dielectric metal (MDM) configuration. The unit cell consists of an outer frame featuring a top triangular section with a cut on the bottom left corner, an L shaped boundary along the sides and bottom, and a central rectangle with an H shaped cavity. Gold (Au) is used as the metallic material, while silicon carbide (SiC) serves as the dielectric layer. The absorption spectrum was computed using the Finite Element Method (FEM) based COMSOL Multiphysics simulation software. The proposed design achieves over 98% absorption of incident light with a bandwidth of  $0.7\ \mu\text{m}$  in TE mode. Additionally, the absorber demonstrates outstanding angular dependent absorption characteristics, maintaining over 90% absorption in the  $3.7\text{-}4.2\ \mu\text{m}$  wavelength range for incident angles ( $\phi$ ) and elevation angles ( $\theta$ ). These properties make the proposed absorber highly suitable for applications such as polarimetric sensing and infrared detection systems.

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## List of Symbols

$\lambda$	Wavelength of electromagnetic radiation
$\vec{E}$	Electric field vector
$\vec{H}$	Magnetic field vector
$\vec{k}$	Wave vector (direction of propagation)
$\vec{S}$	Poynting vector (energy flux / power flow)
$\mu$	Permeability
$\epsilon$	Permittivity
$\nabla$	Nabla operator (used in $\nabla \times$ for curl)
$\tilde{\mu}$	Complex permeability
$\tilde{\epsilon}$	Complex permittivity
$\omega$	Angular frequency
$j$	Imaginary unit
$(-\vec{H})$	Negative magnetic field vector (used in left-handed system)
$(-\vec{k})$	Negative wave vector (used in left-handed system)
$\vec{k}_x$	Transverse component of the wave vector $\vec{k}$
$\vec{k}_y$	Component of the wave vector $\vec{k}$
$\vec{x}$	Displacement from equilibrium position
$m$	Mass (e.g., in SHM context)
$\gamma$	Damping coefficient / scaling factor
$k$	Spring constant
$\vec{F}(t)$	External force as a function of time
$m_e$	Electron mass
$\vec{r}$	Displacement of charge / Position vector
$\Gamma$	Damping factor (in the electron model)
$\omega_0$	Natural frequency
$q$	Electric charge
$\vec{r}(\omega)$	Fourier transform of displacement $\vec{r}$
$\vec{E}(\omega)$	Fourier transform of electric field
$\vec{\mu}(\omega)$	Electric dipole moment in frequency domain
$\vec{P}$	Polarization (volume-averaged dipole moment)
$N$	Number of dipoles per unit volume
$\vec{P}(\omega)$	Polarization in frequency domain
$\chi(\omega) / \chi$	Electric susceptibility
$\omega_p$	Plasma frequency
$\epsilon_r(\omega)$	Relative permittivity in frequency domain
$\eta$	Refractive index
$\mu_r$	Relative permeability

$\epsilon_r$	Relative permittivity
$\eta(\omega)$	Frequency-dependent refractive index
$\eta_o$	Real part of refractive index
$\kappa$	Imaginary part of refractive index / Chirality parameter
$n$	Scalar refractive index
$\vec{D}$	Electric displacement field
$\vec{B}$	Magnetic induction
$\vec{J}$	Electric current density
$\sigma$	Electrical conductivity
$[\epsilon]$	Permittivity tensor
$[\mu]$	Permeability tensor
$[\sigma]$	Conductivity tensor
$\epsilon_x, \epsilon_y, \epsilon_z$	Components of permittivity tensor
$\zeta, \xi$	Bi-isotropic coupling coefficients
$\epsilon_1, \epsilon_2, \epsilon_3$	Nonlinear permittivity coefficients
$\phi$	Azimuthal angle
$\theta$	Angle of incidence
$t_m$	Thickness of metal layer
$t_d$	Thickness of dielectric layer
$S_{11}$	Reflection coefficient parameter
<b>SRR</b>	Split Ring Resonator
<b>SPP</b>	Surface Plasmon Polaritons
<b>LSP</b>	Localized Surface Plasmon
<b>MP</b>	Magnetic Polariton
<b>FWHM</b>	Full Width at Half Maximum
<b>dB</b>	Decibel scale
<b>MNZ</b>	$\mu$ -near-zero materials
<b>SEM</b>	Scanning Electron Microscope
<b>TE</b>	Transverse Electric mode
<b>TM</b>	Transverse Magnetic mode
<b>FEM</b>	Finite Element Method
<b>FDTD</b>	Finite Difference Time Domain
<b>TLM</b>	Transmission Line Method
<b>EBG</b>	Electromagnetic Band Gap
<b>FSS</b>	Frequency Selective Surface
<b>SiC</b>	Silicon Carbide
<b>CAD</b>	Computer-Aided Design
<b>COMSOL</b>	Multiphysics simulation software

# Chapter 1

## INTRODUCTION

### 1.1 What are Metamaterials?

Wikipedia defines metamaterials as: “A metamaterial (from the Greek word *meta*, meaning “beyond” or “after”, and the Latin word *materia*, meaning “matter” or “material”) is a type of material engineered to have a property, typically rarely observed in naturally occurring materials, that is derived not from the properties of the base materials but from their newly designed structures.”

In very simple terms, they are materials that derive their properties from structure rather than the type of material they are composed of. In metamaterials, the molecules that are typically the main type of component of any material are replaced by man-made structures. It have dimensions that depend on the  $\lambda$  of incident the electromagnetic radiation. So, for example, if the visible light is incident, then the dimensions of the metamaterial are of the order of nanometers, and in the case of GHz radiation, the size of the metamaterial may be as large as a few millimeters.

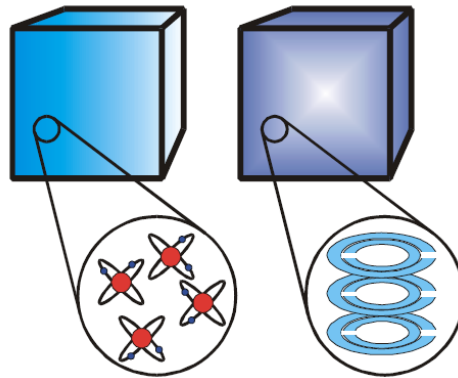


Figure 1.1: On the left we have a normal material made from constituent atoms, and on the right we have a metamaterial made from sub-units which may contain many atoms. Source: [1].

### 1.2 Evolution of Metamaterials

The idea of a metamaterial dates back more than fifty years. The idea was first discussed by Victor Veselago in 1968, who studied the effect of negative permeability and permittivity on wave propagation.[18]. However the term itself is more recent as it originated

in 1999 with the work of Rodger Walser.[19] The realization of the concept was in 1996 when wire structures were used to achieve negative permittivity, then in 1999 split-ring resonators were used to achieve negative permeability. Following this materials with a negative refractive index, i.e. both negative permittivity and negative permeability were constructed.

The area advanced quickly from the mid 1990s to the mid 2010s, which is why this period is referred to as the modern metamaterial era. For instance, construction of graded index metamaterials that allow controlled refraction of electromagnetic waves and can be used for lenses and for cloaking and development of theory of controlling wave propagation through optical transformations via metamaterials also advanced quickly.

By 2010 the concept had been extended to sound waves with the development of acoustic metamaterials and metasurfaces, with structures resembling membranes, coiled-up geometries, and Helmholtz resonators. Then in 2015 the dynamic metamaterials were created that can be for imaging and signal processing.

Metamaterials have been applied to increasingly specialized areas. For example in 2019 monolayers and two dimensional metamaterials were developed for electromagnetic absorbers in the terahertz range, and by 2020 tunnel resonators and chiral metamaterials had been used to manipulate microwaves. Advanced nano-structures such as copper plasmonic structures, and silicon-cored tungsten nanowires were applied to solar energy harvesting in 2021.

The last fifty years have seen metamaterials established as a key technology in the fields of physics, engineering, and materials science, with many widely varied applications.[2]

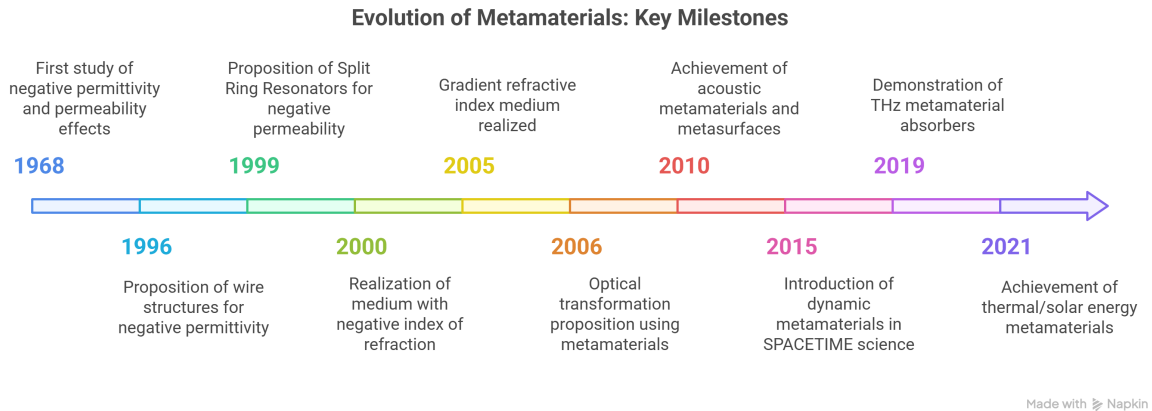


Figure 1.2: Evolution of metamaterial. Source: Image adapted from [2].

### 1.3 Lorentz Oscillator Model

When we discuss about properties of metamaterials, we study their response to electromagnetic radiation (i.e., their response curve). However, in order to study the response curve for metamaterials, we should be first familiar with the response curve of dielectrics. The response curve of ordinary materials can be described by the Lorentz (for dielectrics) and Drude (for metals) models. Both of these are classical models where it is assumed that electrons revolve in orbits around a heavy nucleus and move just like a spring-mass system with damping when subjected to an external field. For a metamaterial, the

combined Drude-Lorentz model describes the effective electromagnetic response of the metamaterial.[20]

When discussing optical response, for conventional materials, we study its permittivity only. This is because the relative permeability at optical frequencies is essentially unity.[21] Conversely, metamaterials allow us to control both the permittivity ( $\epsilon_r$ ) and permeability ( $\mu_r$ ).[22]. This unlocks a whole new range of applications such as super-lens (negative refraction) and perfect absorbers (impedance matching).

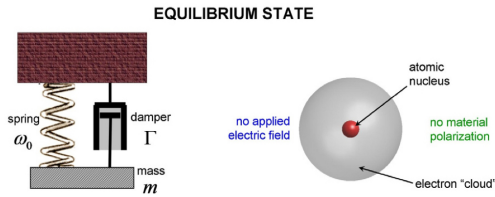


Figure 1.3: The neutral atom is equivalent to the spring-mass system at equilibrium. Source: [3]

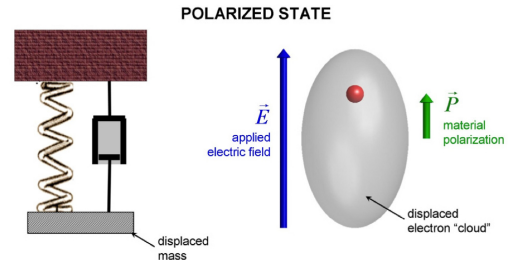


Figure 1.4: The polarized atom is equivalent to the spring-mass system at a non-equilibrium position. Source: EM-PossibleLecture13 [3]

## Mathematical Analysis

A brief summary of the analysis follows. The complete derivation can be found in standard texts.

### 1. General Equation of Simple Harmonic Motion (SHM):

$$m\ddot{\vec{x}} + \gamma\dot{\vec{x}} + k\vec{x} = \vec{F}(t),$$

where  $m$  is the mass,  $\vec{x}$  the displacement,  $\gamma$  the damping coefficient,  $k$  the spring constant, and  $\vec{F}(t)$  the external force.

**2. Equation of Motion for a Bound Charge:** For a charge  $q$  in a time-varying electric field  $\vec{E}$ ,

$$m_e\ddot{\vec{r}} + m_e\Gamma\dot{\vec{r}} + m_e\omega_0^2\vec{r} = -q\vec{E}.$$

### 3. Fourier Transform:

$$\vec{r}(\omega) = -\frac{q\vec{E}(\omega)}{m_e(\omega_0^2 - \omega^2 - j\omega\Gamma)}.$$

### 4. Electric Dipole Moment:

$$\vec{\mu}(\omega) = q\vec{r}(\omega) = \frac{q^2\vec{E}(\omega)}{m_e(\omega_0^2 - \omega^2 - j\omega\Gamma)}.$$

**5. Polarization:** With  $N$  dipoles per unit volume,

$$\vec{P}(\omega) = N\vec{\mu}(\omega).$$

### 6. Material Susceptibility:

$$\chi(\omega) = \frac{\omega_p^2}{\omega_0^2 - \omega^2 - j\omega\Gamma},$$

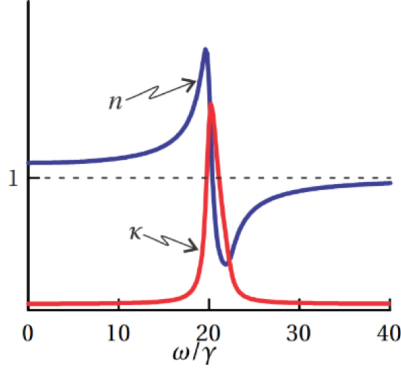
where  $\omega_p^2 = Nq^2/(m_e\epsilon_0)$ .

### 7. Dielectric Function:

$$\tilde{\epsilon}(\omega) = 1 + \chi(\omega) = 1 + \frac{\omega_p^2}{\omega_0^2 - \omega^2 - j\omega\Gamma}.$$

8. **Refractive Index:** For nonmagnetic materials ( $\mu_r = 1$ ),

$$\eta(\omega) = \sqrt{\epsilon_r(\omega)}.$$



The region between 10 and 20 is called the anomalous region, as the real part of the refractive index decreases with an increase in frequency. Conversely, normal dispersion corresponds to regions where the real part increases with frequency. Around  $\omega/\Gamma = 20$ , we see a spike in the imaginary part of the refractive index, indicating maximum absorption (loss). As  $\omega \rightarrow \infty$ ,  $\eta_o \rightarrow 1$  and  $\kappa \rightarrow 0$ , so at high frequencies the overall refractive index tends to unity.

Figure 1.5: Variation of refractive index with  $\omega/\Gamma$ . The region between 10 and 20 is anomalous dispersion, where the real part decreases with increasing frequency. Source: [4]

## Chapter 2

### A Taxonomy of Metamaterials and Their Applications

#### 2.1 Classification of Metamaterials

##### 2.1.1 On the basis of $\mu$ and $\epsilon$

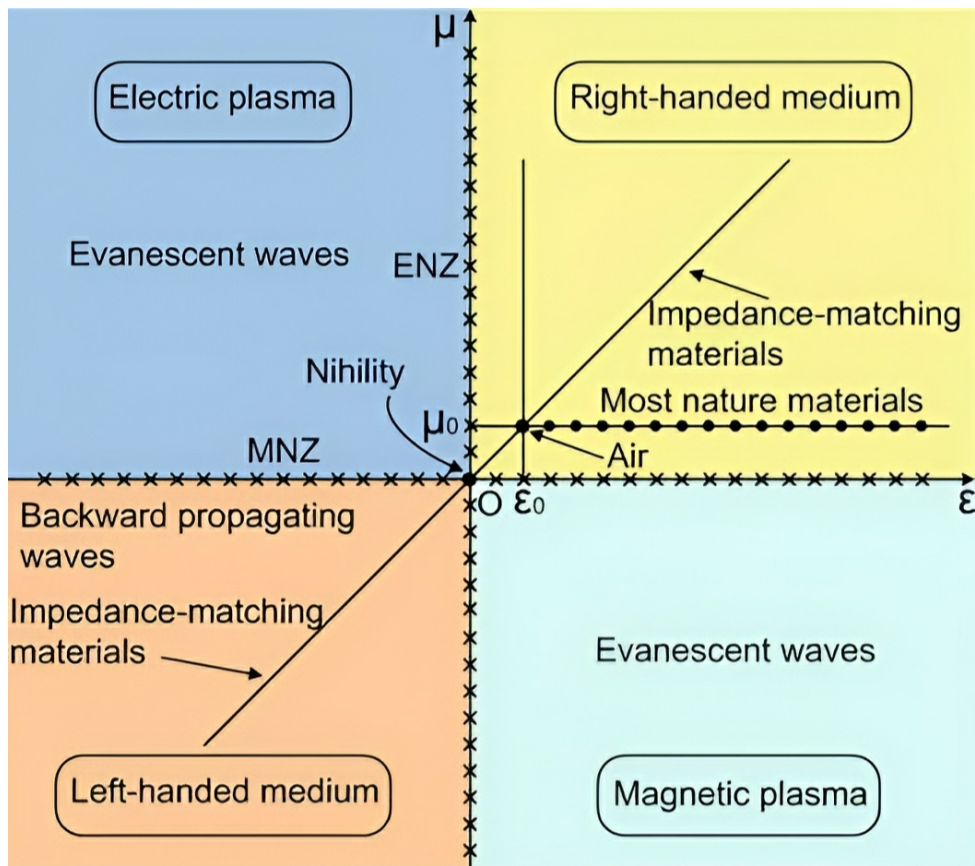


Figure 2.1: Classification of materials in the  $\epsilon$ - $\mu$  domain. Source: Picture from [5]

1. **Double Positive (DPS) Material:** First quadrant where  $\mu > 0$  and  $\epsilon > 0$ . It comprises all right-handed materials (RHM) or ordinary materials, which support forward-propagating waves.

2. **Epsilon Negative (ENG) Material:** Second quadrant, where  $\mu > 0$  but  $\epsilon < 0$ . Electric plasma, which supports evanescent waves, falls under this category.
3. **Mu Negative (MNG) Material:** Fourth quadrant, where  $\mu < 0$  but  $\epsilon > 0$ . Magnetic plasma, which supports evanescent waves, lies in this region. Gyrotropic natural materials in radio frequency have a negative real part of the permeability. Split-ring structures also shows this behavior.
4. **Double Negative (DNG) Material:** Third quadrant where  $\mu < 0$  and  $\epsilon < 0$ . Materials in this quadrant form a left-handed system and support backward-propagating waves (negative  $\vec{k}$ ).

Origin (the point  $\mu = 0, \epsilon = 0$ ) is called **nihility**. The term **MNZ** stands for  $\mu$ -near-zero materials.

## Left-Handed Metamaterials

All ordinary materials are right-handed. For ordinary materials  $\vec{E}$ ,  $\vec{H}$ , and  $\vec{k}$  form a right-handed system meaning the direction of propagation of the wave, represented by  $\vec{k}$ , is perpendicular to both  $\vec{E}$  and  $\vec{H}$  and satisfies the relation:

$$\vec{k} = \vec{E} \times \vec{H},$$

so that  $\vec{E} \perp \vec{H}$ ,  $\vec{H} \perp \vec{k}$ , and  $\vec{k} \perp \vec{E}$ . However, this is not the case in DNG metamaterials. DNG Metamaterials are left-handed in nature.

The reason they are left hand is because  $\mu$  and  $\epsilon$  are negative. This can be shown by substituting the negative values of  $\mu$  and  $\epsilon$  in Maxwell's equations:

$$\nabla \times \vec{E} = -j\omega(-\tilde{\mu})\vec{H}, \quad \nabla \times \vec{H} = j\omega(-\tilde{\epsilon})\vec{E}.$$

Rewriting,

$$\nabla \times \vec{E} = -j\omega\tilde{\mu}(-\vec{H}), \quad \nabla \times (-\vec{H}) = j\omega\tilde{\epsilon}\vec{E}.$$

**The system is left-handed!**

$$\vec{k} \perp \vec{E} \perp (-\vec{H}), \quad -\vec{k} \perp \vec{E} \perp \vec{H}.$$

**$\vec{E}$ ,  $\vec{H}$ , and  $\vec{k}$  form a “left-handed” system.**

An important implication of this is, that the Poynting vector  $\vec{S}(= \vec{E} \times \vec{H})$ , which represents the direction of energy flow, is opposite to the wave vector  $\vec{k}$ . To illustrate this concept, consider the figure 2.2:

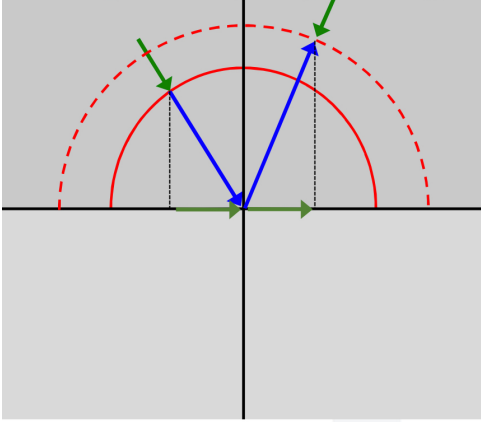


Figure 2.2: Electromagnetic wave refraction at an ordinary material-metamaterial interface, showing wave vector ( $\vec{k}$ ) (blue) and Poynting vector ( $\vec{S}$ ) (green) in the incident region. Source: [3]

1. On the top half, we have the ordinary material, and on the bottom half, we have the metamaterial.
2. On the right side of the normal material,  $\vec{S}$  and  $\vec{k}$  point in the same direction.
3. When  $\vec{k}$  hits the interface, its transverse component ( $\vec{k}_x$ ) should be continuous.
4. Since  $\vec{k}_x$  is the same,  $\vec{k}_y$  must be negative.
5. Causality ensures that the Poynting vector points in the direction of forward energy propagation, even in left-handed materials where the wave vector and energy flow are reversed.

### 2.1.2 On the basis of functional properties

On the basis of electromagnetic response mechanism and application domain, metamaterials can be broadly classified into seven types:

1. Electromagnetic Metamaterials
2. Chiral Metamaterials
3. Terahertz Metamaterials
4. Photonic Metamaterials
5. Tunable Metamaterials
6. Frequency Selective Surface (FSS) based Metamaterials
7. Nonlinear Metamaterials

### Electromagnetic Metamaterials

Metamaterials that are specifically engineered to control and manipulate the amplitude, phase, polarization, frequency, and wave vector of electromagnetic waves. They have many practical applications from optical to microwave, such as band-pass filters, lenses, and microwave couplers. They can be further subdivided into:

1. Single Negative Metamaterials: One of  $\mu$  or  $\epsilon$  is negative.
2. Double Negative Metamaterials: Both  $\mu$  and  $\epsilon$  are negative.
3. Electromagnetic Band Gap (EBG) Metamaterials
4. Bi-isotropic and Bi-anisotropic Metamaterials

The first two have been discussed in the previous section.

**Electromagnetic Band Gap (EBG):** They are typically designed by placing dielectric substrate on a periodic metal patches. It can control the propagation of light by preventing certain frequencies via destructive interference while simultaneously reflecting any incident electromagnetic wave with no phase shift. This is implemented with photonic crystals or left-handed metamaterials. Due to this property, they are widely used to improve antennas quality and in building filters and miniaturized microwave devices.

**Bi-isotropic and Bi-anisotropic Metamaterials:** In isotropic media,  $\vec{D}$ ,  $\vec{B}$ , and  $\vec{J}$  are independent of the field direction.

$$\vec{D} = \epsilon \vec{E}, \quad \vec{B} = \mu \vec{H}, \quad \vec{J} = \sigma \vec{E}$$

where  $\epsilon$ ,  $\mu$ , and  $\sigma$  are scalar. However, In anisotropic media, they depend on direction:

$$\vec{D} = [\epsilon] \vec{E}, \quad \vec{B} = [\mu] \vec{H}, \quad \vec{J} = [\sigma] \vec{E},$$

where  $[\epsilon]$ ,  $[\mu]$ , and  $[\sigma]$  are tensors. Double, single, double positive are based at the presumption of metamaterial that exhibits independent electric as well as magnetic response.

Bi-isotropy introduces coupling between electric and magnetic fields.

$$\vec{D} = \epsilon \vec{E} + \zeta \vec{H}, \quad \vec{B} = \mu \vec{H} + \xi \vec{E}.$$

If  $\epsilon$ ,  $\mu$ ,  $\zeta$ , and  $\xi$  are scalars, the medium is **bi-isotropic**; if they are tensors, it is **bi-anisotropic**. A similar coupling takes place in the electromagnetic metamaterial, where magnetic field produces an electrical polarization, which is known as magneto-electric coupling, and the electric field creates a magnetic polarization.

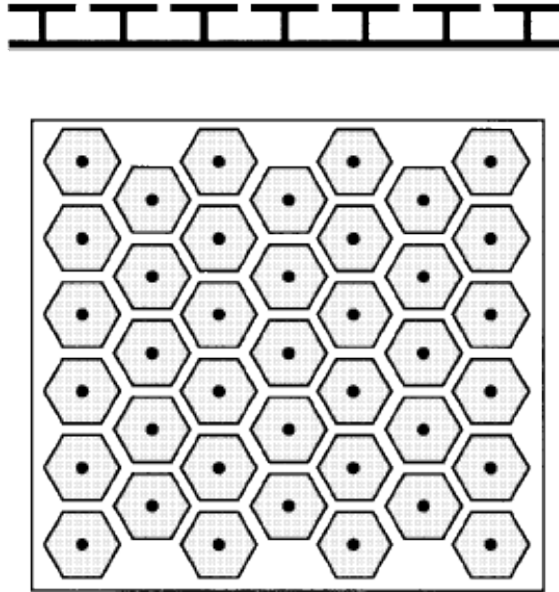


Figure 2.3: Mushroom-type EBG structure Source: [6]

## Chiral Metamaterials

An object is chiral if it lacks geometrical symmetry (rotation or reflection). A chiral metamaterial is built from chiral material that has ability to rotate the plane of polarization of light. The refractive index depends on the chirality parameter  $\kappa$ :

$$n = \pm\sqrt{\varepsilon_r\mu_r} \pm \kappa.$$

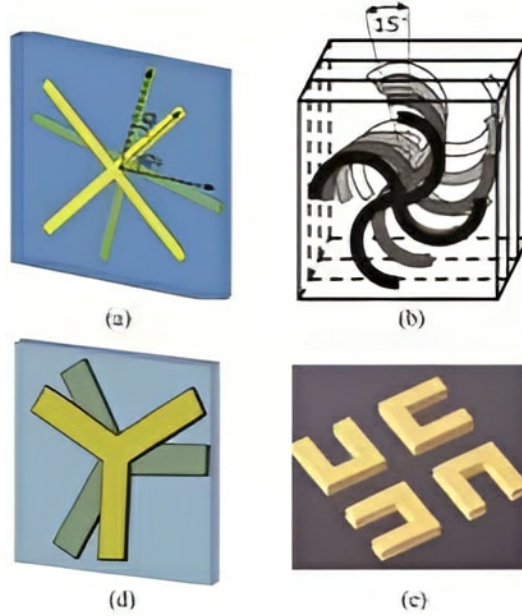


Figure 2.4: Different geometries of chiral metamaterials. Source: [7]

## Terahertz Metamaterials

It operates in the terahertz range (0.1 to 10 THz), where ordinary materials show negligible magnetic response but metamaterials due to their negative values of permeability can exhibit tailored responses. The response depends on the geometry of the structure, which can be **tuned** by altering the dimensions or the geometry to achieve desired response.

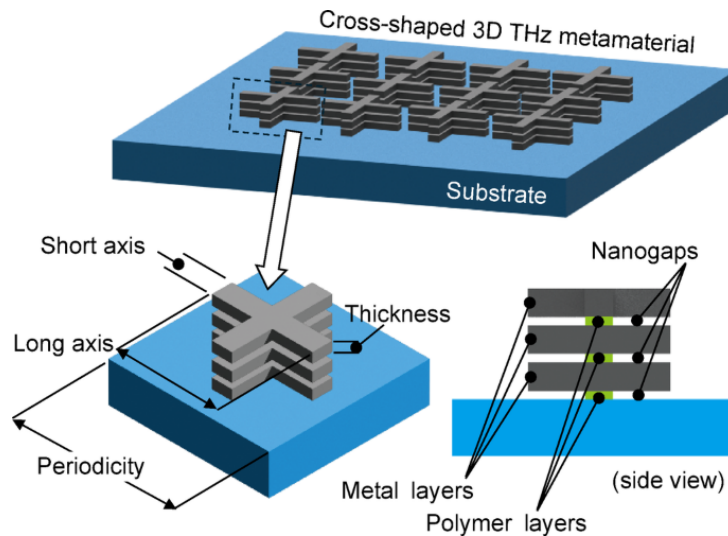


Figure 2.5: 3D THz metamaterial with vertical nanogaps. Source: [8]

## Photonic Metamaterials

It operate at optical frequencies and derive their properties from the structure that is smaller than the interacting wavelength (sub wavelength), unlike photonic crystals, whose optical properties arise from Bragg scattering in a periodic lattice.

## Tunable Metamaterials

Materials whose effective properties (e.g., refractive index or the resonant response) can be dynamically adjusted by external stimuli (electric, magnetic, thermal).

## Frequency Selective Surface (FSS) based Metamaterials

FSS are engineered to selectively reflect, absorb, or transmit waves at specific frequencies. FSS can be composed of two-dimensional planar components in periodic arrays. High-Impedance Surfaces (also known as Artificial Magnetic Conductors) are a class of FSS metamaterials whose metallic patterning supports unique surface-wave currents and impedance characteristics.

## Nonlinear Metamaterials

Metamaterials can be fabricated from the material which exhibit nonlinear response when their internal field strength exceeds the applied external field. The nonlinear constitutive relation is:

$$\vec{D} = \epsilon_1 \vec{E} + \epsilon_2 \vec{E}^2 + \epsilon_3 \vec{E}^3 + \dots$$

## 2.2 Applications

### 2.2.1 Metamaterial Absorbers

Metamaterial absorbers can be engineered to exhibit high absorbance either across a broad wavelength band, at a single designated frequency, or at multiple discrete frequencies. They are designed to have a near-unity absorption coefficient, meaning they can absorb almost all incident electromagnetic waves without reflection or transmission. Absorbance can be calculated using following relation:

$$A(\omega) = 1 - |S_{11}(\omega)|^2 - |S_{21}(\omega)|^2$$

where  $S_{11}$  and  $S_{21}$  are the reflection and transmission coefficients, respectively. When an electromagnetic wave is impinged on to the metamaterial surface, it can be scattered, reflected, or absorbed. The top surface of the metamaterial is made rough to suppress any type of scattering. Similarly, to minimize the transmittance (ideally 0) a metal plate is used as the bottom layer. This works, because electromagnetic radiations cannot pass through metals. Finally, reflectivity is minimized by matching the impedance of the metamaterial to that of free space. This is achieved by altering the dimension of material until effective permeability is equal to effective permittivity ( $\mu_r = \epsilon_r$ ).

$$Z = Z_0 \sqrt{\frac{\mu_0 \mu_r}{\epsilon_0 \epsilon_r}}, \quad Z_0 = \sqrt{\frac{\mu_0}{\epsilon_0}} \approx 377 \, \Omega. \quad (2.1)$$

Apart from impedance matching, the article *Metamaterial Electromagnetic Wave Absorbers*, Watts, Liu, and Padilla (2012) [23] explains there are quite a few more phenomena such as resonance, plasmons, and nanoparticle gratings that can help us build a perfect absorber. Earlier, in resonance, a metal backing is placed at  $\lambda/4$  spacing from the resistive sheet. In transmission line theory, this transforms the short circuit to an open circuit, creating a resonant condition, if the impedance of the resistive sheet matches that of free space.

Modern metamaterial absorbers, utilize a three-layer structure. The uppermost layer usually consists of an Electric Ring Resonator (ERR) along with the ground plane (bottom metal layer), which creates an electric response by coupling strongly to the incident electric field at a certain resonance frequency. The bottom metal layer is spaced apart from the middle layer by a dielectric and creates magnetic coupling via magnetic polaritons, which creates antiparallel currents in the cut wire and the center wire of the ERR. An incident time-varying magnetic field may couple to these antiparallel currents, thus yielding a Lorentz-like magnetic response. This layered configuration takes advantage of both electric and magnetic responses. If instead of an ERR, a cavity-like structure is used, then the structure will exhibit cavity resonance, where the electromagnetic waves get trapped within a specific geometry via multiple reflections. [23]

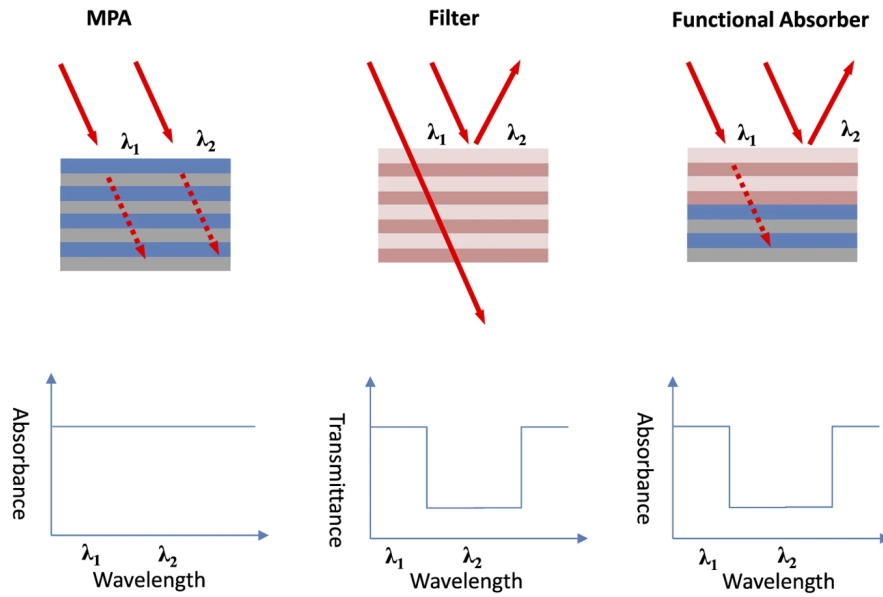


Figure 2.6: Evolution from broadband to spectrally-selective absorption: (left) Metamaterial Perfect Absorber (MPA) absorbs all wavelengths  $\lambda_1$  and  $\lambda_2$ , (center) dielectric filter selectively transmits  $\lambda_1$  while reflecting  $\lambda_2$ , (right) functional absorber integrates both components to achieve wavelength-selective absorption—absorbing  $\lambda_1$  while rejecting  $\lambda_2$ . Source: [9]

## 2.2.2 Superlens

All positive focal length lenses and optical devices have the ability to converge light. However, beyond a certain focal length (the diffraction limit), refractive power cannot reduce the minimum focal spot size producing a blurry image.

Most telescopes, microscopes, cameras and other lens have a circular aperture. Light is diffracted when it is passed through the circular aperture, forming **Airy Disk**, a bright

central spot with concentric rings as depicted in fig 2.6. Any two objects (or light sources) closer than the size of the Airy disk cannot be resolved. Unresolved objects creates **evanescent waves**, which are exponentially decaying waves that carry information about the object. These carry subtle information about the shape of the object. Since they are exponentially decaying, they cannot be captured by a lens with a positive focal length.

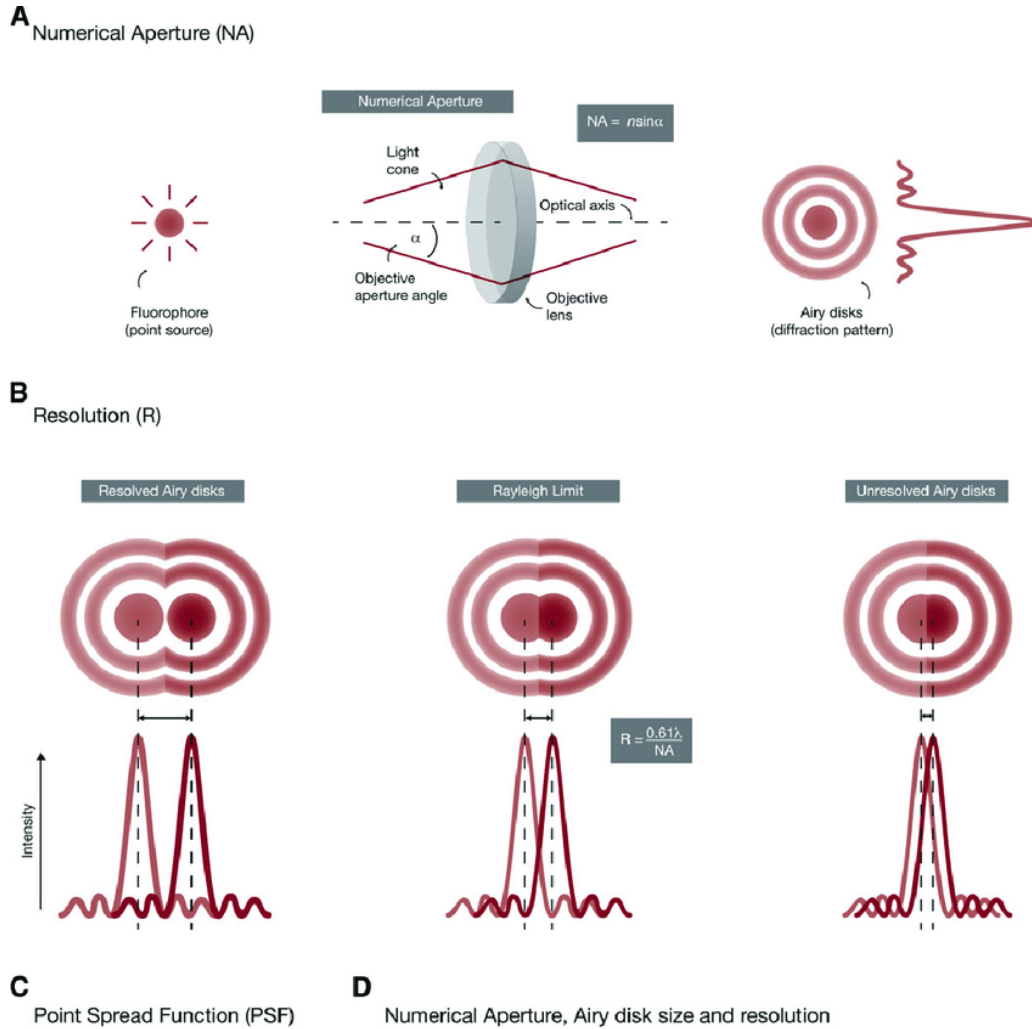


Figure 2.7: Relationship between numerical aperture, diffraction-limited resolution, and the Rayleigh criterion showing resolved, critically resolved, and unresolved Airy disk patterns with corresponding intensity profiles. Source: [10]

However, a **superlens** which is just a lens made from metamaterial can recover these evanescent waves and focus them to form an image with resolution beyond the diffraction limit. This is because metamaterials have negative refractive index, which allows them to bend light in the opposite direction compared to conventional materials.

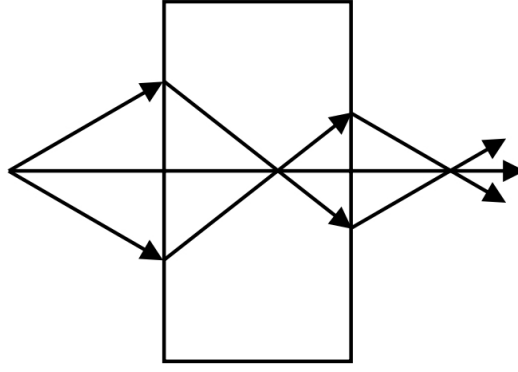


Figure 2.8: Superlens converging light beyond the diffraction limit. Source: [1]

### 2.2.3 Cloaking Device

Theoretical designs use wave bending around objects to render them invisible without distortion.

This is can by accomplished by two methods:

1. **Bending Waves:** Metamaterials can alter the path of electromagnetic waves by artificially controlling the speed and direction of light using negative refractive index metamaterials which has the ability to bend the light backwards and by using graded index material which can slow the speed of the wave.
2. **Scattering Cancellation:** We can also coat the object with a metamaterial that can generate waves in backward direction, which will then cancel out the natural scattering of the object. This is known as scattering cancellation.

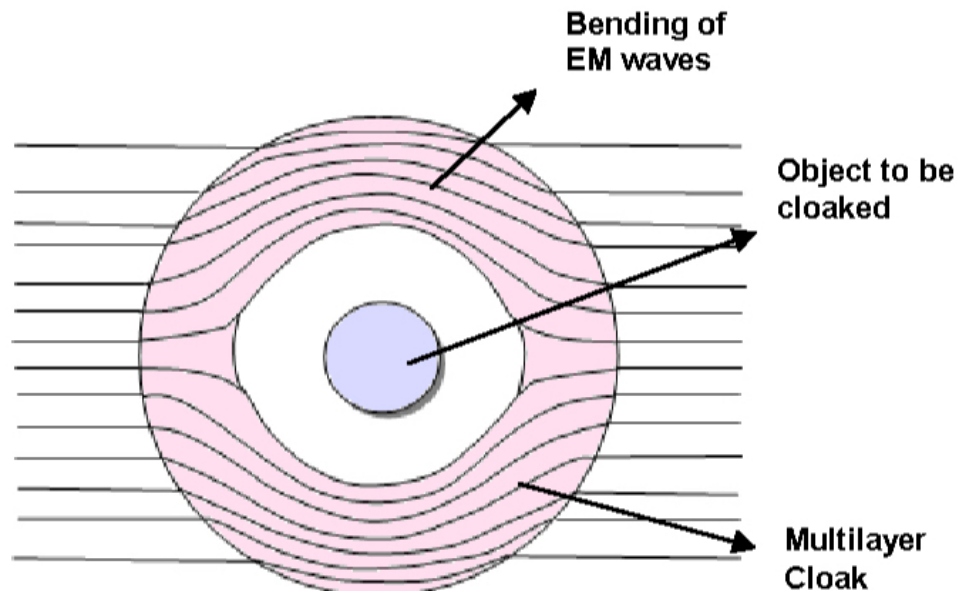


Figure 2.9: Conceptual cloaking device. Source: [11]

### 2.2.4 Antennas

Another key area where metamaterials are employed is in the design and engineering of antennas. Their unique features, such as their periodic structure, high directivity, and electromagnetic band-gaps, help in storing and radiating energy while also drastically reducing the antenna size, mimicking the performance characteristics of larger antennas. They overcome conventional limitations by reducing signal reflection, increasing the bandwidth and the gain of the antenna. There are 4 key types of different antennas:

1. **Zero-Phase-Shift:** These antennas use uniform magnetic field to transmit ultra high radio frequency or WLAN signals without changing their phase.
2. **Gap-Capacitor:** This type of antenna, arranges itself in a way which creates a L-band radar resonance (ZOR) using a narrow capacitive gap, allowing compact, efficient radar operation.
3. **Mushroom Cells:** As the name suggests, these antennas are designed in the shape of a mushroom that enhances WIFI signals by controlling how wave spreads.
4. **High-Permittivity Dipoles:** They are made up of high-permittivity materials to create compact dipole antennas that can operate at lower frequencies. Due to their compact size, they are used in multiple input multiple output (MIMO) cellular towers.

Other applications include seismic protection and sound filtering.

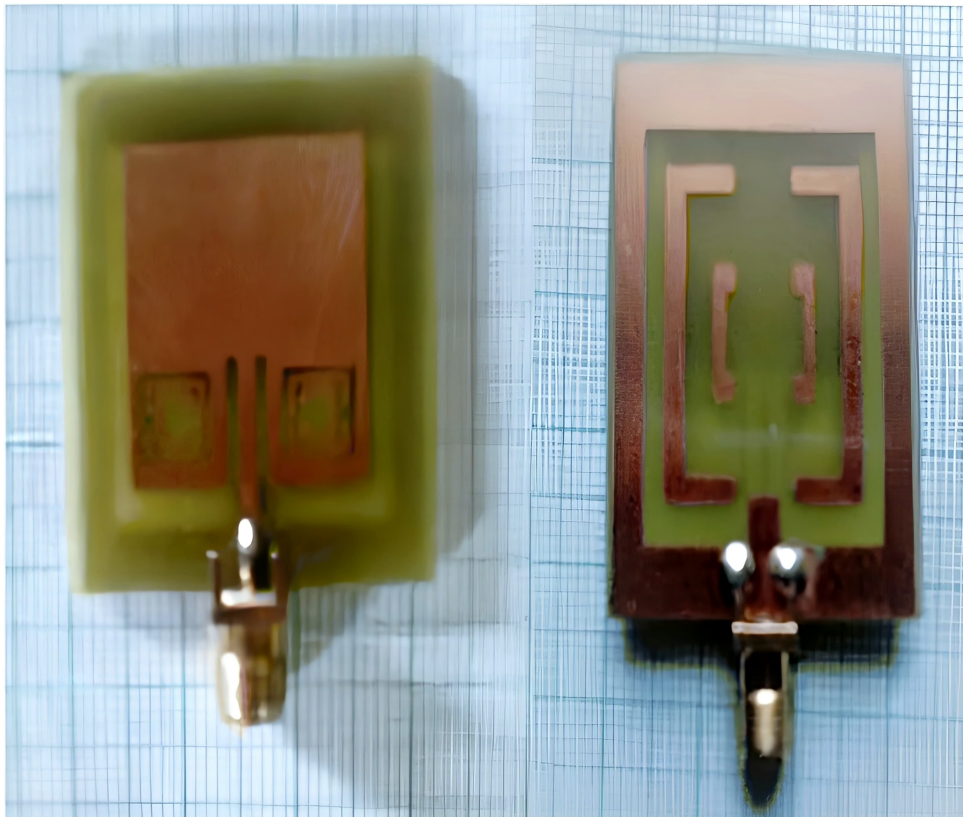


Figure 2.10: Front and back side of a fabricated metamaterial-based rectangular patch antenna designed on FR4 for 2.4 GHz WiFi applications. Source: [12]

## Chapter 3

### LITERATURE REVIEW

In the previous chapter, subsection 2.2.1, general formation mechanism of metamaterials absorbers was discussed. which were impedance matching, transmission line theory and the using a metal layer to minimize transmission (reflection theory). However, for a broadband metamaterial, these mechanisms alone are not sufficient. It along with other mechanism work collectively to create a broader absorption band. In this chapter, a review of various broadband metamaterial absorbers is presented.

### 3.1 Broadband Metamaterial Absorbers Mechanisms

#### 3.1.1 Superposition of Resonance Peaks

This is one of the simplest method to create a broadband metamaterial absorber. The idea is to put together different geometry together such that multiple resonance peaks are superimposed to create a broad absorption band.

In song *et al.* (2018),[13] merged two different geometry, each with a single resonant peak to create a dual-band absorber.

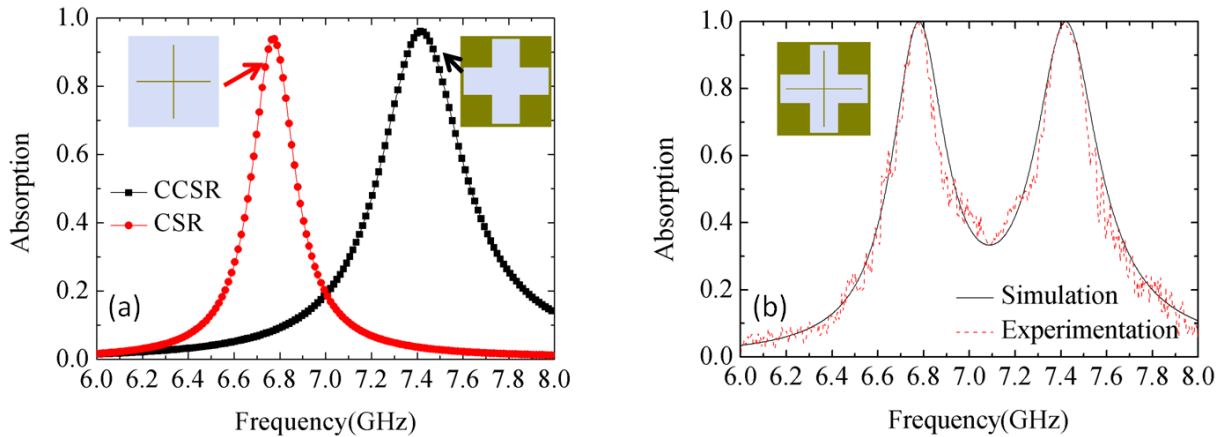


Figure 3.1: Geometry and the absorption performance of each design (left) and the combined geometry and its dual band absorption curve (right). Source: [13]

Another instance where this method was used is in Hamza *et al.*, (2024), where a triple band absorber was created by 4 different geometries, each with a single resonant peak.

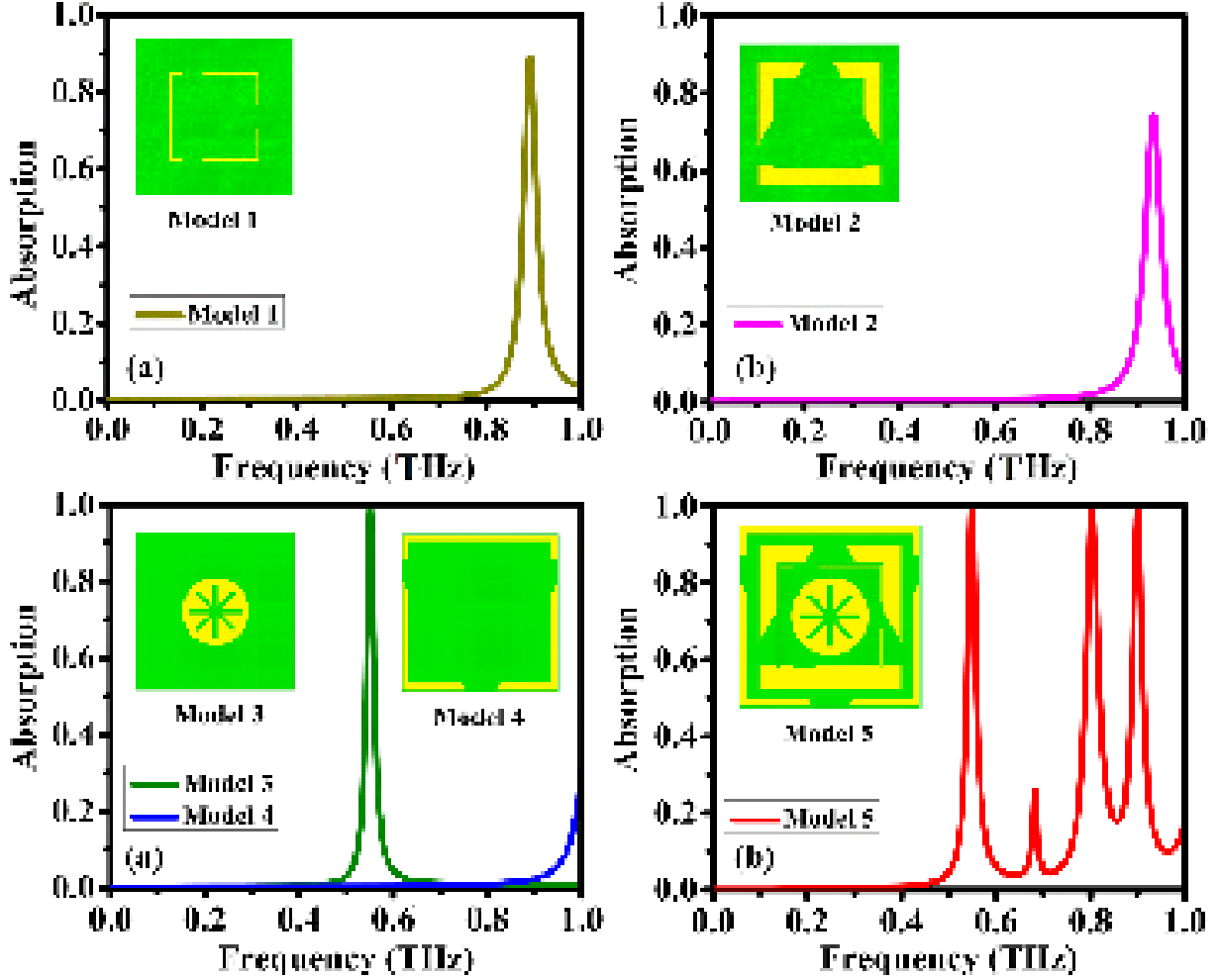


Figure 3.2: Geometry and the absorption performance of each design (model 1, model 2, model 3 and model 4) and the combined geometry (model 5) and it's triple band absorption curve. Source: [14]

This method is simple but it is important to keep in mind that the individual peaks shouldn't destructively superimpose each other. This can negatively impact the absorption performance of the combined geometry. In our proposed structure, which is discussed in the next chapter, this same method is used to create a broadband absorber.

### 3.1.2 Resonance phenomena

It comprises of 3 main phenomena:

- **Magnetic resonance:** In this phenomena, magnetic field induces circulating currents in the surface. The most common way to achieve is to introduce closed loop geometries in your absorber which will naturally induce circular current effectively creating an effective magnetic dipole. The most common shape used to achieve this is the split ring resonator (SRR). The SRR is a closed loop geometry with a gap in it which allows the magnetic field to induce a circulating current. The induced current creates a magnetic dipole which interacts with the incident electromagnetic wave, leading to absorption. Figure 3.1 shows a SRR based metamaterial absorber along with circular currents from H.-L. Huang *et al.*(2017) [24].

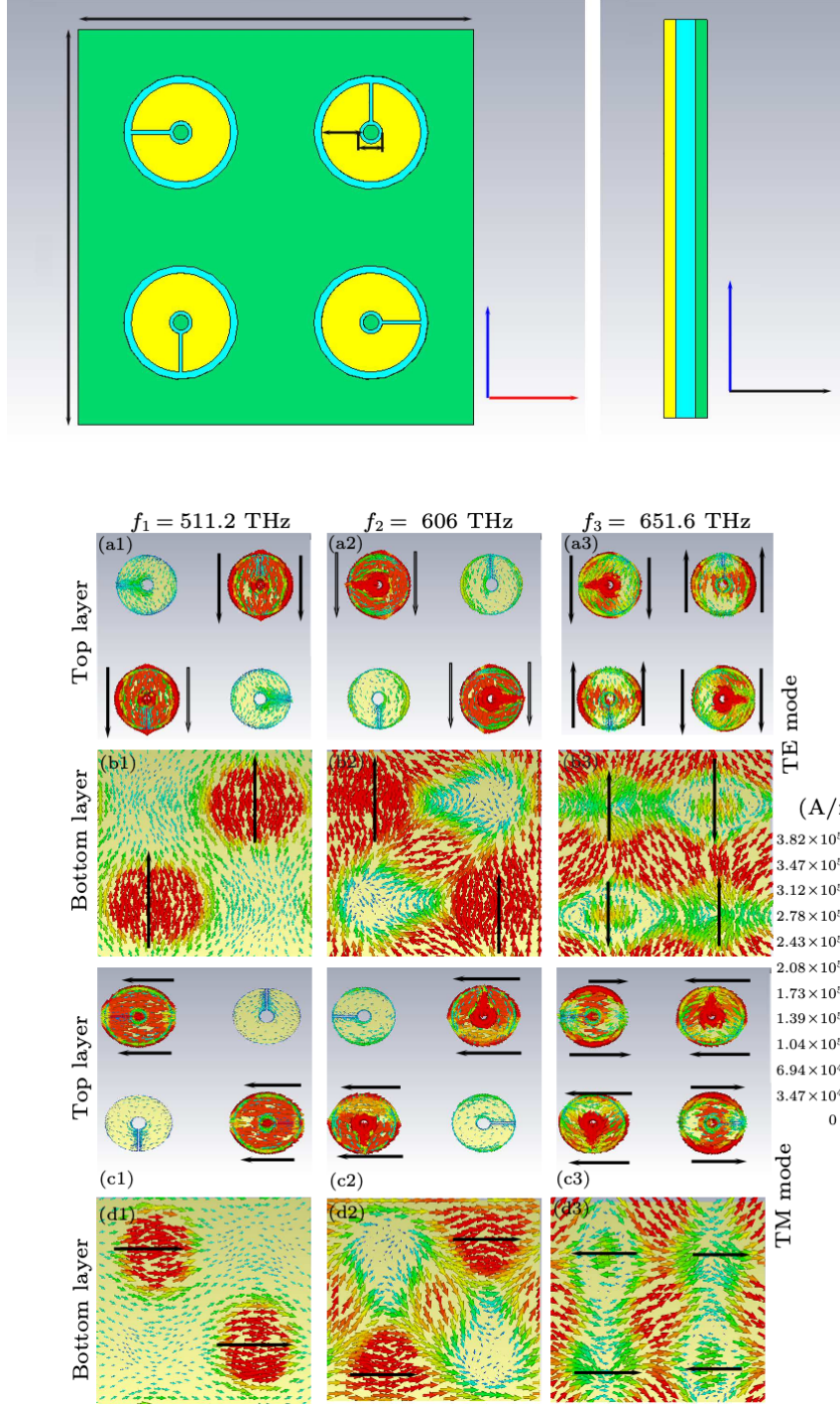


Figure 3.3: SRR geometry showing the existence of magnetic resonance due to circular surface currents. Source [15]

- **Electric resonance:** This phenomena is majorly due to plasmonic effects which occur at the metal dielectric surface. Plasmons are electric dipoles which get excited by the electric field component of the incident electromagnetic wave., resulting in a resonant response. Despite, in many metamaterials, plasmonic effects is a major factor which contribute to a high absorption performance electric resonance can occur in can occur in systems without free electrons, such as dielectrics, molecules, or specific structural designs , where resonant interaction of the electric field takes

place with bound electrons. In plasmonic effects surface plasmon polaritons (SPP) and localized surface plasmons (LSP) are the most common electric resonance phenomena. Surface plasmon polaritons involve coupling between the electric field and electron plasma oscillations at a metal-dielectric interface. Similarly, localized surface plasmons in nanoparticles result from the electric field inducing electron oscillations, leading to absorption through ohmic losses. A surface plasmon is characterized by a electric field hotspot which propogates along the metal dielectric surface while a LSP is characterized by an electric field hotspot which is concentrated in nanoparticles. Figure 3.3, shows a Ultra-broadband metamaterial absorber from Qi *et al.* (2019) [16] is shown where the SPRs was used to achieve a broadband absorption performance and the figure 3.4 shows a triband metamaterial absorbers where LSPs dominate.

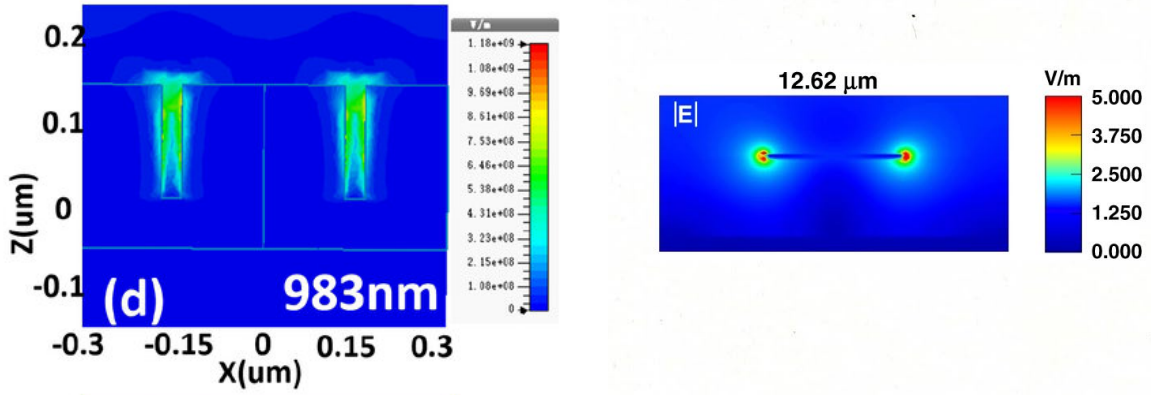
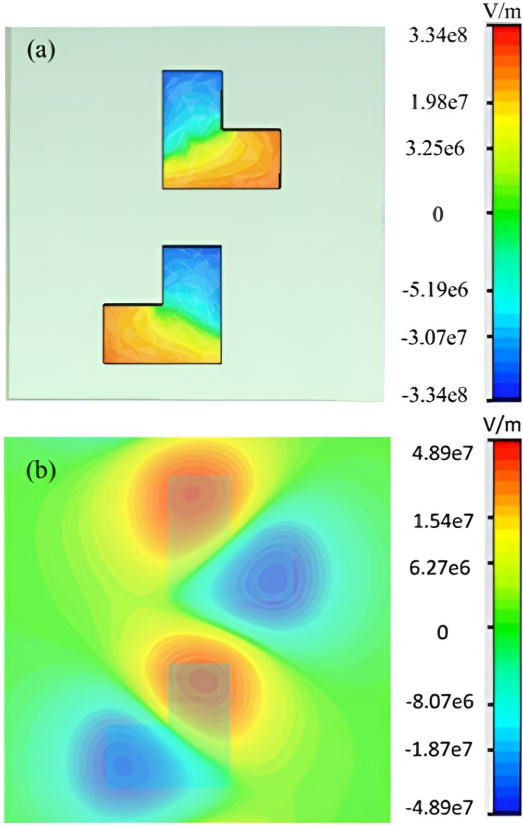
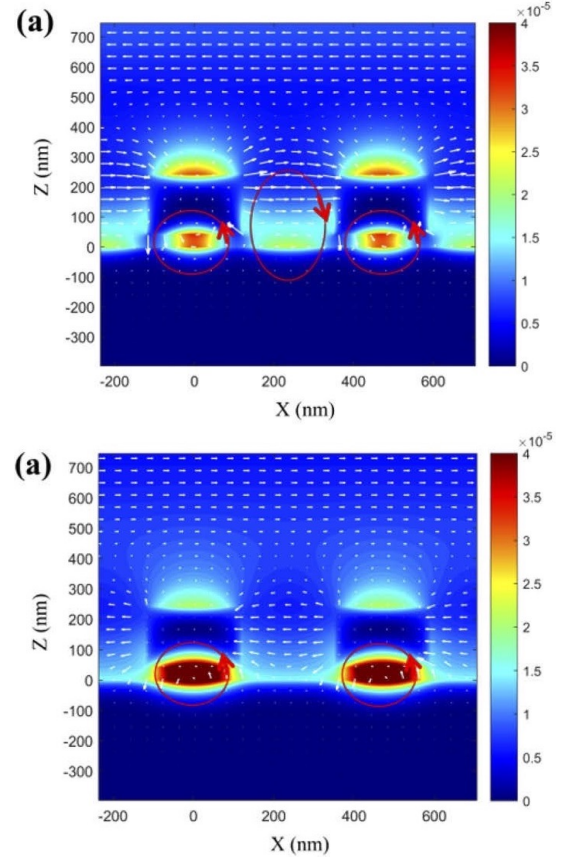


Figure 3.4: Comparison of SPP (left) and LSP (right) based metamaterial absorber geometries and their absorption performance (triple-band curves). Source: [15] [16]

- **Magnetic Polariton (MP)** : This is a similar phenomena to magnetic resonance. The MPs are hybrid quasiparticles formed by the strong coupling of photons with magnetic dipole oscillations in metamaterials. To detect the presence of MPs, electrical field vectors should circulate around the dielectric to form current loops, which induces the diamagnetic response and eventually excite MPs. In figure a MP based metamaterial absorber from Cai *et al.* (2025) is shown where arrows indicate electric field vectors forming circular loops. However, in Yang Bai *et al.*(2015), the same concept is shown presented differently. It indirectly shows MPs by showing opposite phases of electric field at a metal-dielectric-metal surface. The top metal induced a positive charge , while the bottom metal induce a negative induced charge. The opposite happens in the other half of the cycle. Finally, the opposite surface charge oscillations creates a current loop through the dielectric spacer and back through the metals.



(a) Opposite sign of electric of field in the two metal surfaces of the metamaterial hinting existence of magnetic polaritons. Source: [25]



(b) Metamaterial absorber showing the presence of magnetic polaritons by the presence of circular electric field vectors. Source: [26]

### 3.1.3 Material Composition and Structural Configuration

The material composition and structural configuration indirectly determine the absorption mechanism. They themselves don't create a new mechanism but they play a major role in influencing what mechanism will dominate the absorption performance.

1. **Material Composition:** The choice of materials of metamaterial absorbers determine the type of application they will be suited for. According to Faisal *et al.* (2024) [27] demonstrated that highly conductive metals, such as gold and silver, are broadly used for their plasmonic properties. They have a relatively low ohmic losses compared to other metals which is why they are used in building biosensors. The main disadvantage of using gold and silver is that both are expensive which makes cost production high. Also, silver oxidizes easily, so to prevent this a protective layer is applied onto it's surface which suppress it's performance. Aluminum is sometimes used as a substitute for gold and silver because of it's low cost but it has much weaker performance as mentioned by Jia *et al.* (2022) in the journal paper A Simple Metamaterial for High-Performance Spectrum-Selective Absorption in the Visible Region.[28] Other metals such as titanium and nickel which is probed by Zhou *et al.* (2021) [15] have high

thermal stability and a large imaginary part permittivity makes it suitable for applications in stealth and thermophotovoltaics. Similarly, dielectrics can also be classified on the basis of the mechanism of absorption you want to achieve. For example, Wu *et al.* (2023) [29] illustrated low loss dielectrics, such as silicon dioxide (SiO<sub>2</sub>) and silicon nitride (Si<sub>3</sub>N<sub>4</sub>), are often used for achieving high absorption by impedance matching and cavity resonance, while Xu *et al.* (2021) in his journal paper Broadband Solar Absorber Based on Square Ring Cross Arrays of ZnS [30] concluded, high indexed dielectrics such as zinc selenide (ZnS) is used to shift resonance wavelengths.

## 2. Structural Configuration:

For quantifying the absorption performance a dimensionless quantity called quality factor (Q-factor) is used. It represents the ratio of resonant frequency to the full width at half maximum (FWHM) and describes the relationship between the resonance bandwidth and its center frequency according to a theoretical equation.

$$Q = \frac{f_0}{\Delta f}$$

Here  $f_0$  represents the central frequency of the resonant peak and  $\Delta f$  represents the frequency interval between FWHM. A lower value of Q-factor indicates a good absorber. Since, most metamaterials absorbers can be modeled to an equivalent to a LCR circuit, we can equate their Q-factor. In an LCR circuit, we define the Q-factor as:

$$Q = \frac{1}{R} \sqrt{\frac{L}{C}}$$

Here, R represents the equivalent resistance of the absorber, L is the equivalent inductance of the of the absorber, and C represents the equivalent capacitance. The three parameters (R, L, and C) now can be tweaked that will affect the absorption to achieve broadband absorption response. For example, in the paper by Rajni *et al.* (2016) [17], the authors used a SRR geometry where the inductance (L) corresponds to metal traces/rings which acts as current loops, capacitance (C) corresponds to the gaps between metal elements that help in storing electric energy and resistance (R) corresponds to ohmic losses in metals, dielectric losses in substrates and in the metal dielectric metal metamaterial absorber bottom metal plate represents the inductor, the top metal patches and the dielectric spacer represents the capacitor and the total losses in the absorbers represents the resistance.

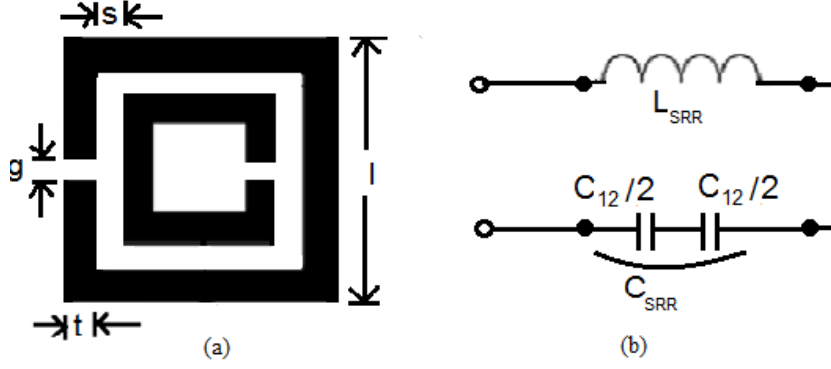


Figure 3.6: Equivalent circuit model of a SRR metamaterial absorber. Source: [17]

In a broadband metamaterial absorber often multiple mechanism work together to achieve a broadband absorption performance.

## 3.2 Wide-Angle, Polarization-Independent Dual-Band Infrared Absorber: L-Shaped Metamaterial

Review by Yang Bai *et al.*

[25] In this section, a brief review of paper is presented which discusses geometry, mechanism and the shortcomings. Our work is an extension of this work, where we create a broadband absorber.

In this paper, the authors proposed a metal dielectric metal double L shaped dual-band metamaterial absorber.

The author first designed a single L shaped metamaterial absorber as shown in figure 3.7.

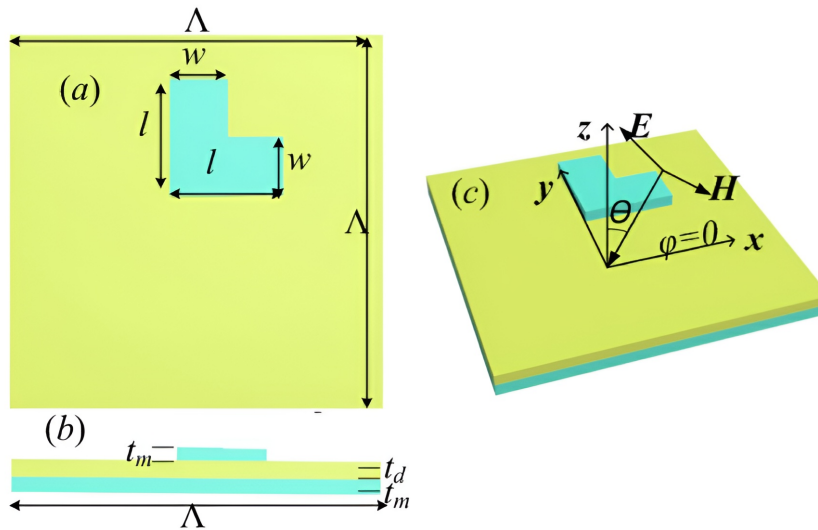


Figure 3.7: Single L-shaped metamaterial absorber geometry and the absorption performance for TE and TM modes.

However, in the TE case, it's absorption performance dipped when  $\theta$  was varied because magnetic polaritons weren't effectively excited.

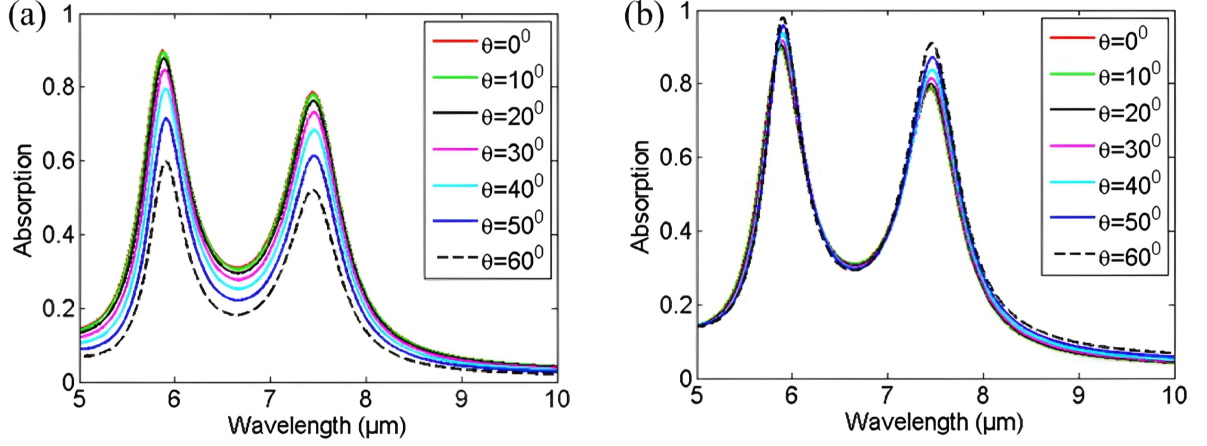


Figure 3.8: TE mode (left) shows reduced stability at  $\phi = 60^\circ$ ; TM mode (right) shows stability for all  $\phi$ .

The author modified the single L structure by a doubly L structure.

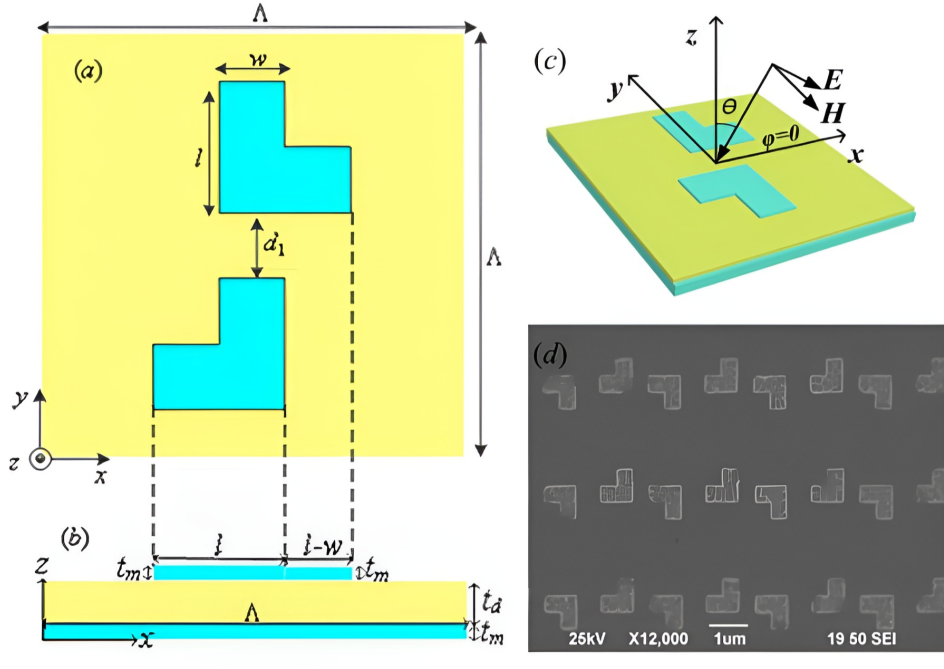


Figure 3.9: (a) Top view, (b) Side view, (c) Light incidence on the L-shaped metamaterial, (d) SEM image of the fabricated L-shaped absorber.

Here,  $t_m$ ,  $t_d$  represent the thickness of metal and dielectric, respectively. The substrate is silica carbide (SiC) and the bottom layer and L-shaped patches are made of gold, modeled by the Drude model for dielectric function.

## Results

The absorption spectra along with real and imaginary parts of impedance were plotted.

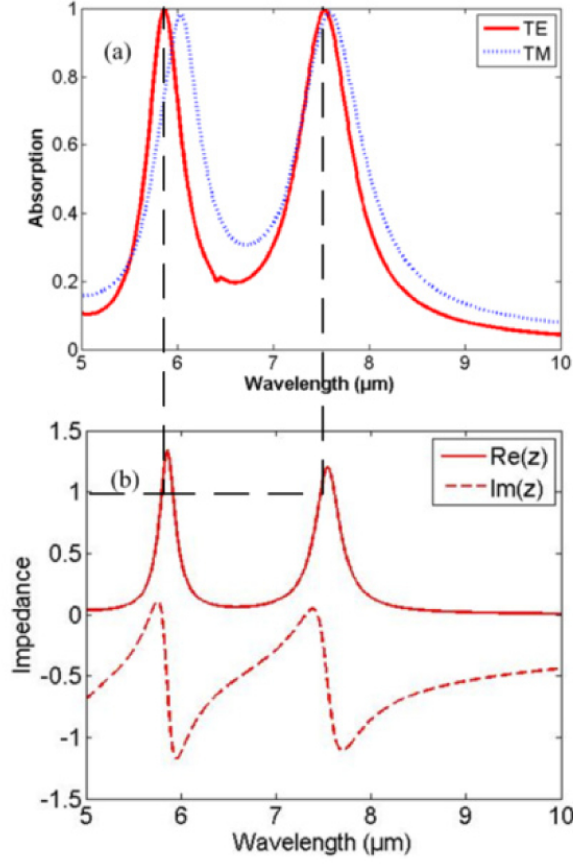


Figure 3.10: Absorption spectra and impedance for TE and TM modes at  $\theta = 45^\circ$  and  $\phi = 0^\circ$ .

Then the stability of the absorber was tested by varying the angle of incidence  $\theta$  and azimuthal angle  $\phi$ . in both TE and TM modes.

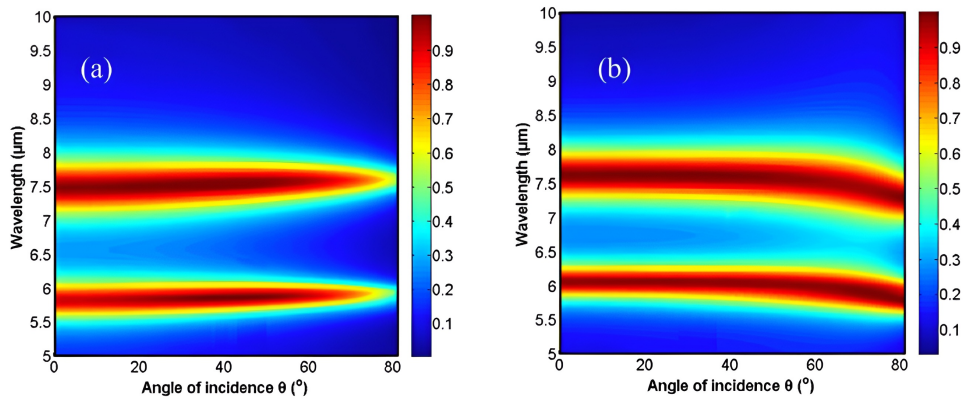


Figure 3.11: Electric field distribution for TE mode (left) and TM mode (right) for varying  $\theta$  at  $\phi = 45^\circ$ .

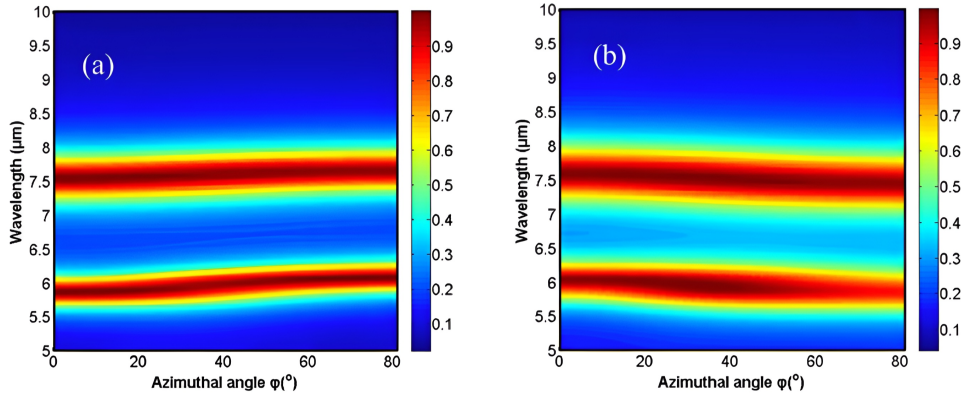
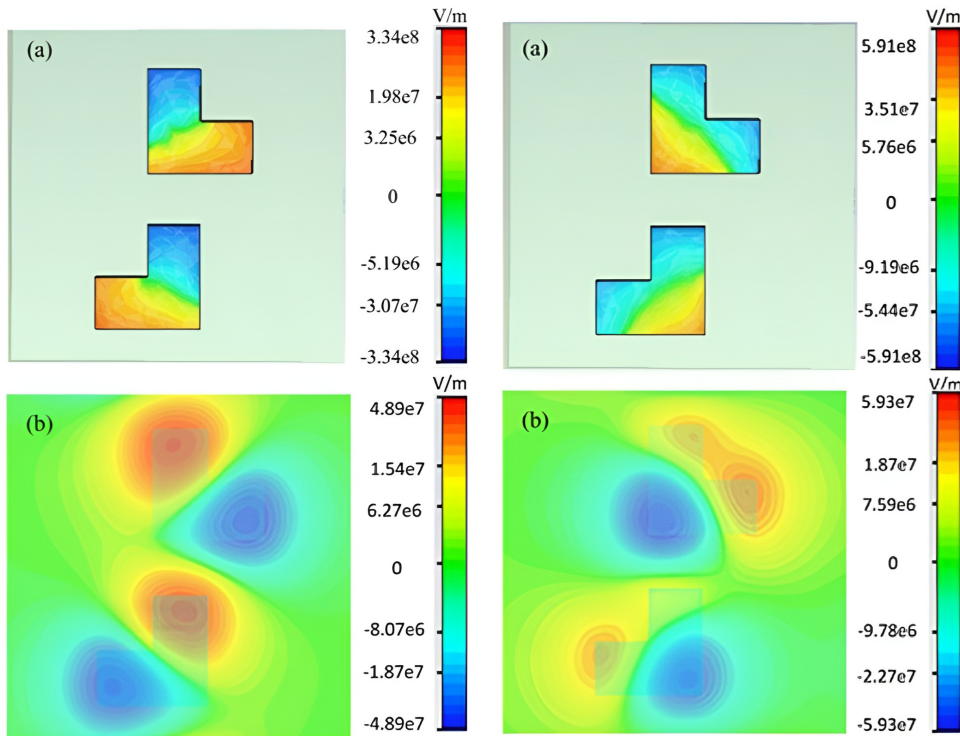


Figure 3.12: Electric field distribution for TE mode (left) and TM mode (right) for varying  $\phi$  at  $\theta = 0^\circ$ .

As shown in the figures 3.11 and 3.12, with the new double L structure the structure were polarize insensitive at the resonant peaks.

To understand the mechanisms behind it, the z component of electric field at both metal interfaces for both resonant wavelength were plotted.



(a) Electric field distribution at  $\lambda = 7.5 \mu\text{m}$  (b) Electric field distribution at  $\lambda = 5.86 \mu\text{m}$

Figure 3.13: Opposite phases of the electric field at the two metal interfaces for the two resonant wavelengths confirms the existence of magnetic polaritons.

Finally, an equivalent LCR circuit model was proposed to explain the absorption performance of the double L structure.

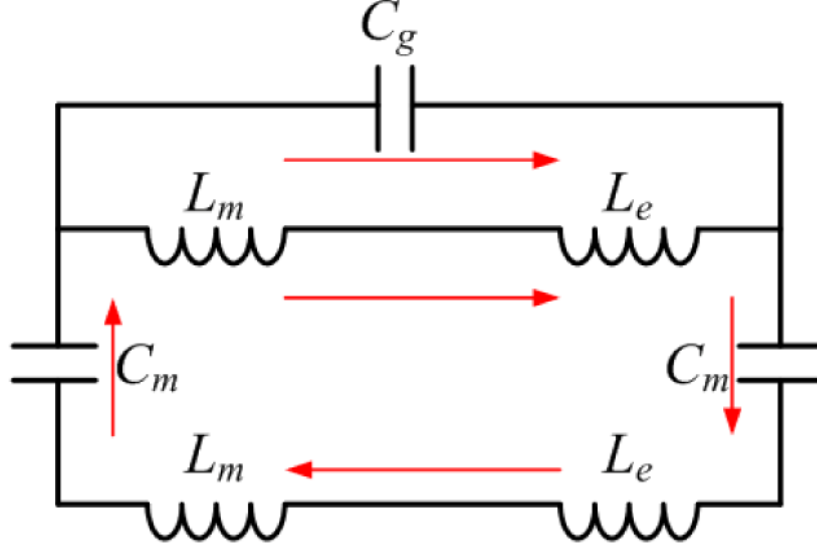


Figure 3.14: Equivalent LCR circuit model for the double L-shaped metamaterial absorber.

The key **advantages** of this design were it was such simple yet effective design. It showed near perfection absorption performance at both TE and TM modes and was also polarize insensitive. The major **disadvantage** of the proposed structure was that it was a dual band absorber, so it is only suited for niche applications and not much suited for practical applications. Also, the thickness of gold used was high (100 nm) which makes the manufacturing cost high making production at scale difficult.

## Chapter 4

# ABSORBER GEOMETRY AND MODELING

### 4.1 Comsol Multiphysics

First to learn the basics of Comsol Yang Bai *et al.* work's was replicated and simulated. A.1. Comsol Multiphysics is a simulation software that help us simulate various physical phenomena such as electrodynamics , heat transfer , fluid dynamics. It has a built in CAD (Computer-Aided Design) module that allow us to create a model from scratch and also allow us to perform advanced numerical calculations on our model .

Then in the next step the initial designs of metamaterial absorber were created and simulated which are shown in A.2 in the appendix.

The starting point for the proposed structure was a design inspired by Yang Bai *et al.* [25]. As mentioned in the previous chapter, despite its drawback, this design significantly improves its bandwidth while maintaining near unity performance.

### 4.2 Metamaterial Absorber Design

Figure 4.1 and 4.2 illustrates the schematic of the top-down view of proposed design of the metamaterial absorber. Each geometric entity was meticulously introduced to enhance the overall absorption efficiency of the material via an iterative procedure. The figure 4.3 shows the side view of the unit cell, and it demonstrates that the unit cell is a tri-layer metal - dielectric - metal(MDM) configuration. Gold layers (basal and geometric entities ) are shown in yellow color. The intermediate dielectric layer is made from silicon carbide (SiC), shown in grey color. The colors used in the diagram are not true to the actual color of the material.

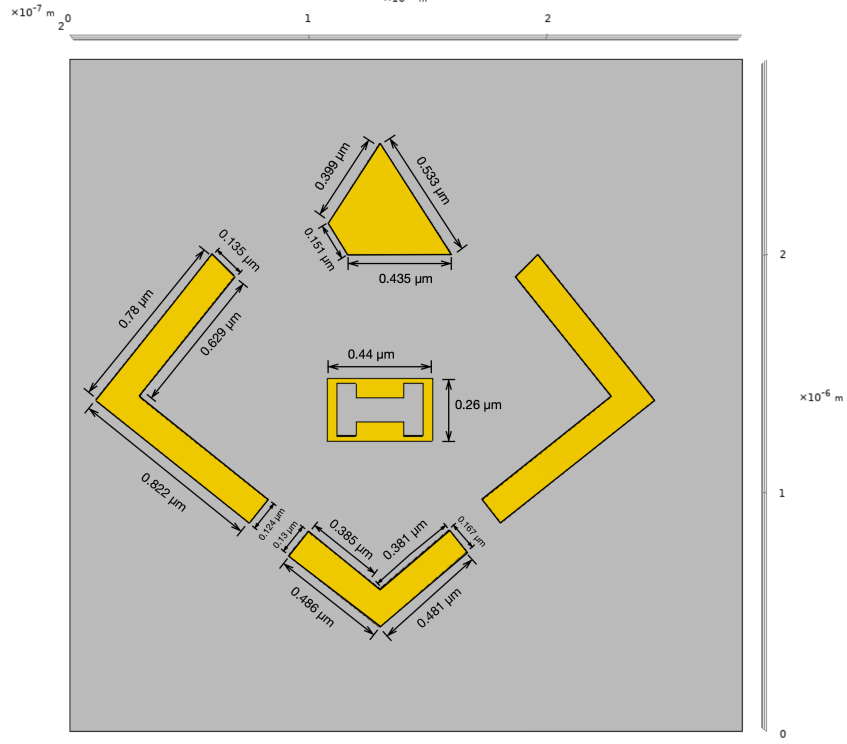


Figure 4.1: Top-view schematic of the metamaterial unit cell showing the geometric parameters with their dimensions. The structure consists of an outer triangular element, L-shaped arms, and central H-shaped cavity on the top gold layer.

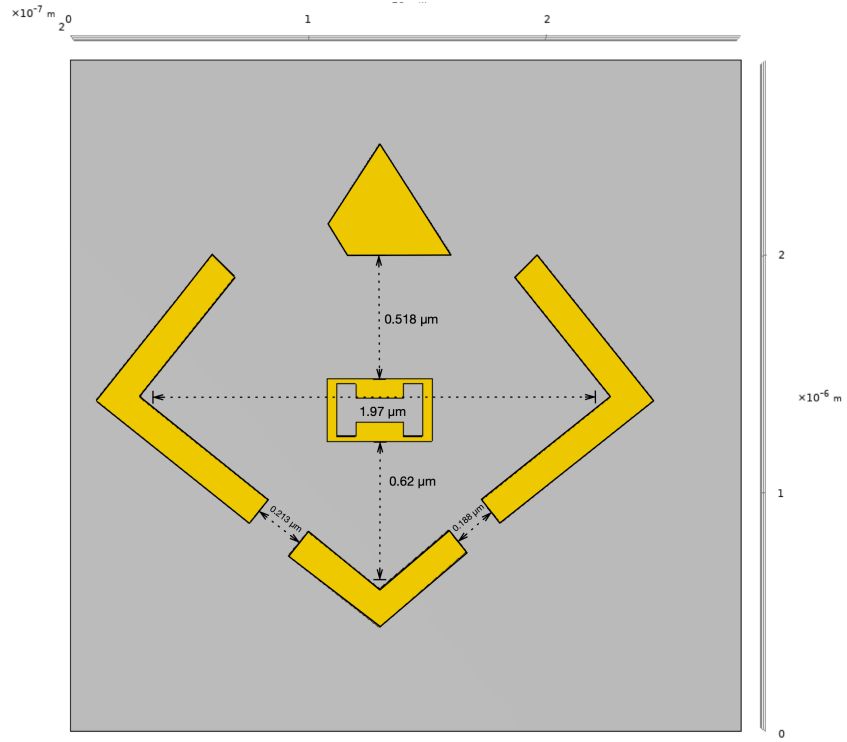


Figure 4.2: Top-view schematic of the metamaterial unit cell showing spatial relationships between metamaterial components.

Despite its high cost, gold is the preferred choice as the metal for many metamaterials because it exhibits surface plasmon resonance (SPR)<sup>[31]</sup> phenomena where its electrons undergo collective oscillations when a specific wavelength of light is incident, making it ideal for plasmonic applications especially in the infrared regime. To characterize its optical response, we have adopted the Drude-Lorentz model for metals, where the dielectric function is given by:<sup>[32]</sup>

$$\epsilon(\omega) = 1 - \frac{\omega_{p,D}^2}{\omega^2 - i\omega\gamma_D} + \frac{F\omega_{p,L}^2}{\omega_0^2 - \omega^2 + i\omega\gamma_L}^{-1}$$

$\omega_{p,D} = 1.2 \times 10^{16}$  rad/s is the plasma frequency for the Drude (free-electron) term.<sup>[25]</sup>

$\gamma_D = 10.5 \times 10^{13}$  rad/s is the damping (collision) frequency for the Drude term.<sup>[25]</sup>

$\omega_{p,L} = \omega_{p,D}$  is the plasma frequency associated with the Lorentz (resonant) term.

$\omega_0 = 0$  is the resonance frequency of the Lorentz oscillator

$\gamma_L = \gamma_D$  is the damping coefficient for the Lorentz resonance.

$F = 1$  is the oscillator strength factor for the Lorentz term.

The choice of SiC as the dielectric spacer was due to its relatively high refractive index<sup>[33]</sup> and high absorptive losses<sup>[34]</sup> within the mid-infrared range, so that it could improve the metamaterial's general performance properties. The value of the dielectric constant  $\epsilon$  for SiC is taken to be 10.8 and with a loss tangent dissipation factor  $\tan \delta$  equal to 0.003.<sup>[25]</sup>

The thicknesses of each gold layer ( $t_m$ ) and the dielectric layer ( $t_d$ ) are  $0.05 \mu\text{m}$  and  $0.27 \mu\text{m}$  respectively. The thickness is chosen to be such that it minimizes the cost of production by enabling utilization of fabrication techniques like Nanoimprint Lithography instead of more precise fabrication techniques such as Electron Beam Lithography (EBL), which is not only exponentially more expensive but also more time consuming, making it less suitable for production at scale. The thickness is large enough that it ensures structural robustness, ensuring it is not too fragile while also minimizing the material consumption, lowering the cost of material consumption relative to other already existing designs which have a thickness greater than  $0.6 \mu\text{m}$ .

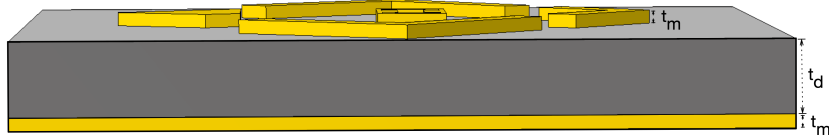


Figure 4.3: Side-view schematic of the Metal-Dielectric-Metal (MDM) metamaterial absorber showing layer thicknesses. Gold layers (yellow) with thickness  $t_m = 0.05 \mu\text{m}$  sandwich the SiC dielectric layer (grey) with thickness  $t_d = 0.27 \mu\text{m}$ .

The numerical simulation was performed in Comsol Multiphysics<sup>®</sup> v6.1 in the Electromagnetic Waves, Frequency Domain module. Floquet-Bloch periodic conditions are used in  $\vec{x}$  and  $\vec{y}$  directions to produce infinite arrays of unit cells. This condition

<sup>1</sup>This Drude-Lorentz model will effectively reduce to Drude model for metal.

enforces a phase change relation, requiring that the solution on one boundary equals that on the opposite boundary multiplied by a complex phase. This factor makes it ideal for modeling wave propagation in periodic media. The formula for the phase change relation can be written as:<sup>[35]</sup>

$$E(\vec{r} + \vec{a}) = E(\vec{r})e^{i\vec{k}\cdot\vec{a}}$$

Here:

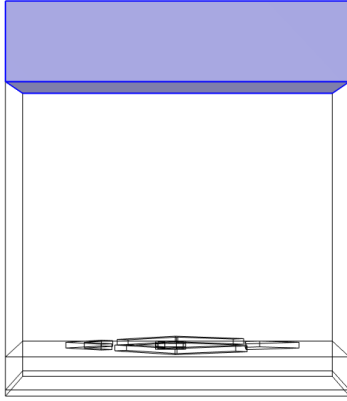
$E(\vec{r})$ : Electric field at position  $\vec{r}$

$\vec{a}$ : Lattice vector (translation vector in the periodic structure)

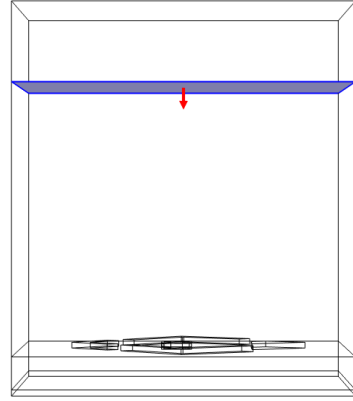
$\vec{k}$ : Wavevector

$e^{i\vec{k}\cdot\vec{a}}$ : Complex phase factor imposed by the periodic boundary condition

A Perfectly Matched Layer (PML) is also implemented atop the structure to absorb outgoing radiations that could inflate absorption values.<sup>[36]</sup> The thickness of it is set to  $0.44\mu\text{m}$  with scaling factor equal to  $1/\cos\theta$ . Pardiso solver was chosen since it excels at providing robust calculations.<sup>[37]</sup> A quadratic discretization scheme and a fine mesh with refinement for conductive edges were employed so that there is a good balance of accuracy, while keeping the load on processor optimal and calculations do not take excessive time. An excitation port was set up parallel to X-Z plane to impinge metamaterial structure with transverse component of electric field at an incident angle ( $\phi = 0^\circ$ ) and elevation angle  $\theta = 45^\circ$ .



(a) Implementation of the Perfectly Matched Layer (PML) in the COMSOL simulation with thickness  $0.44\mu\text{m}$  and scaling factor  $1/\cos\theta$ . The PML absorbs outgoing radiation to prevent artificial inflation of absorption values due to boundary reflections.



(b) Excitation port configuration parallel to the X-Z plane used to impinge the metamaterial structure with the transverse component of the electric field at azimuthal angle  $\phi = 0^\circ$  and elevation angle  $\theta = 45^\circ$ . The port enables precise control of electromagnetic wave parameters for performance evaluation.

Finally a parametric sweep is computed for the range  $3.3 - 4.4\mu\text{m}$  with a step size  $= 3.33 \times 10^{-8}\text{m}$  to find the spectral dependence of absorption ( $S_{21}$ ) and reflection coefficient ( $S_{11}$  in db scale) using the formula:

$$A(\lambda) = 1 - S_{11}$$

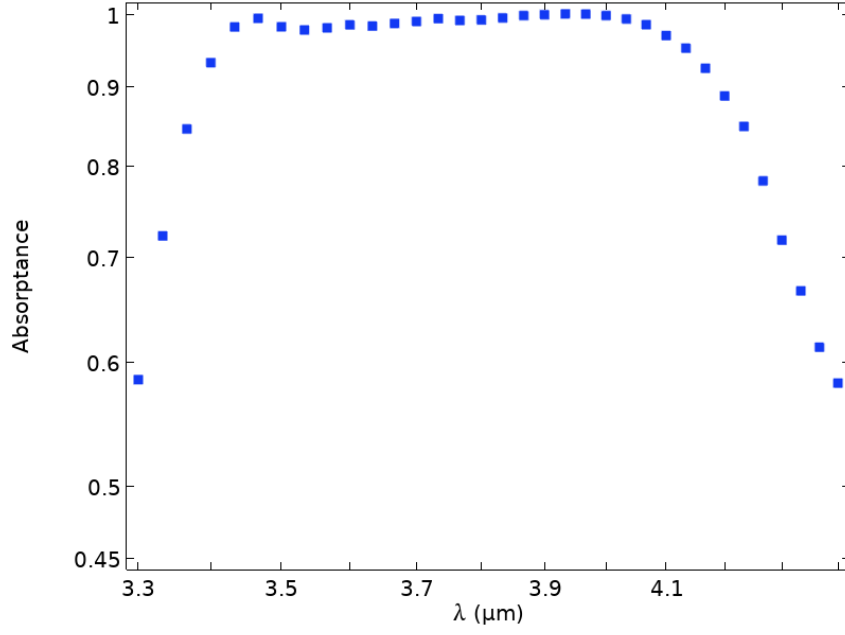
## Chapter 5

### RESULTS and DISCUSSION

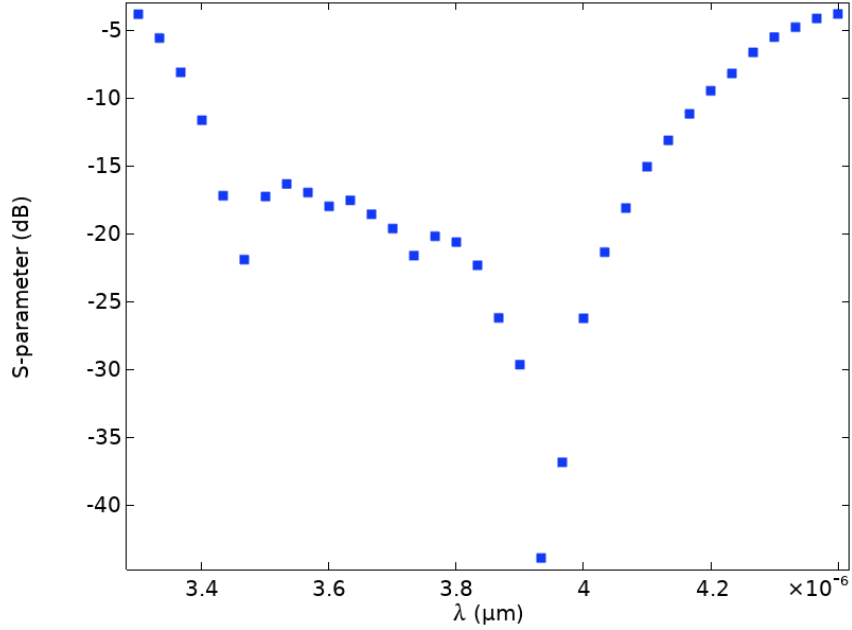
Figure 5.1 (a) and (b) shows the absorption spectrum ( $S_{21}$  parameter) and the reflection coefficient ( $S_{11}$  in dB scale) at  $\phi = 0^\circ$  and  $\theta = 45^\circ$ . It was observed that the structure was able to achieve average absorption over 98% with a bandwidth of  $0.7\mu m$  ( $3.4 - 4.1\mu m$ ) in the TE mode. The peak absorbance achieved in this bandwidth was  $\approx 99.99\%$  at  $\lambda \approx 3.932\mu m$ . The broadband nature of the absorber is quantified using the effective quality factor via resonance bandwidth from the absorption graph:

$$Q_{\text{eff}} = \frac{\lambda_0}{\Delta\lambda} = \frac{3.75\mu m}{0.7\mu m} = 5.36 \quad (5.1)$$

where  $\lambda_0 = \frac{3.4+4.1}{2} = 3.75\mu m$  is the central wavelength of the absorption band and  $\Delta\lambda$  is the bandwidth of the absorption spectrum which is equal to  $4.1\mu m - 3.4\mu m = 0.7\mu m$ . This low Q-factor confirms efficient wideband operation, critical for applications such as thermal imaging and radiative cooling.



(a) Absorption spectrum of the metamaterial structure showing over 98% average absorption at incident angles  $\phi = 0^\circ$  and  $\theta = 45^\circ$ .



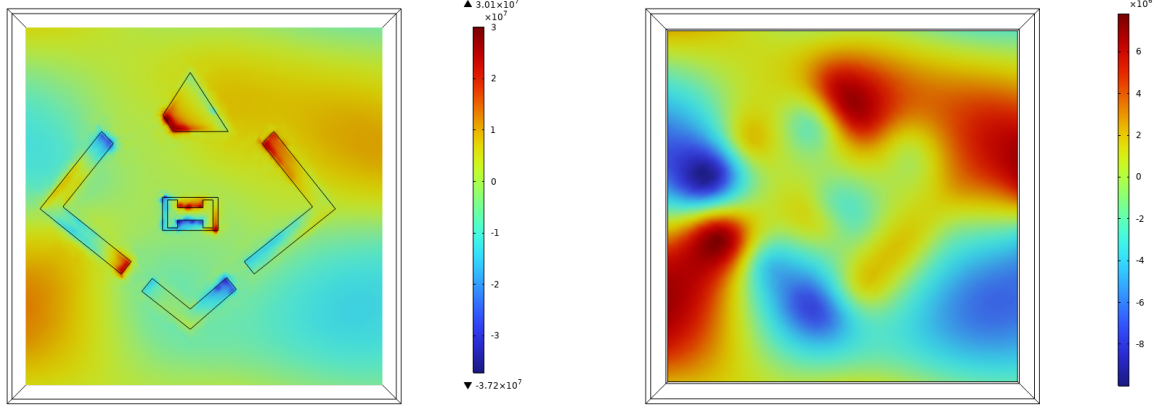
(b) Reflection coefficient ( $S_{11}$ ) spectrum in dB scale at  $\phi = 0^\circ$  and  $\theta = 45^\circ$ .

Figure 5.1: (a) Absorption spectrum and (b) Reflection coefficient spectrum of the metamaterial absorber, both measured at  $\phi = 0^\circ$  and  $\theta = 45^\circ$ .

### 5.0.1 Resonance Mechanisms and Field Localization

To investigate the underlying mechanisms behind the high absorption, electromagnetic field distributions were analyzed. The exceptional absorption performance arises from a hybrid resonance mechanism rather than one dominant resonance.

Figure 5.2 (a) and (b) shows colormaps of  $\vec{E}_Z$  of the top and bottom metal layers at resonance wavelength of  $3.932\mu m$ . The top and bottom layers exhibited opposite signs hinting the presence of magnetic polaritons. The opposite polarity pattern in the top layer and bottom layer indicated the presence of magnetic resonance.

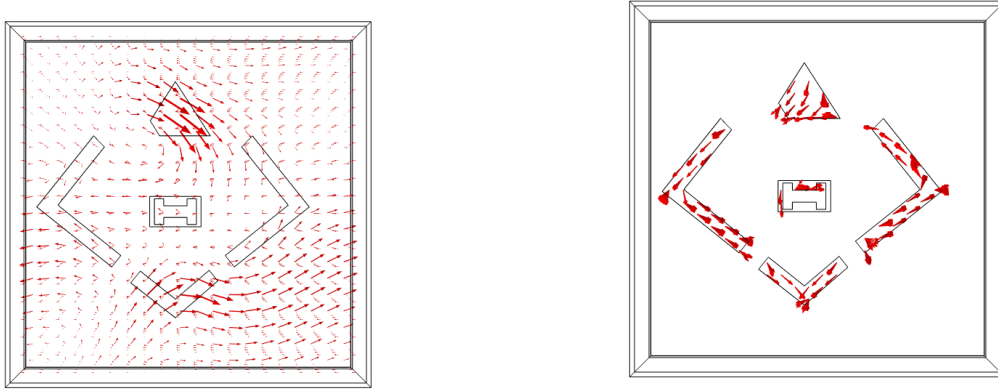


(a) Electric field distribution ( $E_z$ ) in the top gold layer at  $\lambda = 3.932 \mu m$ .

(b) Electric field distribution ( $E_z$ ) in the bottom gold layer at  $\lambda = 3.932 \mu m$ .

Figure 5.2: Electric field distribution ( $E_z$ ) (a) in the top gold layer and (b) in the bottom gold layer at resonance wavelength ( $\lambda = 3.932 \mu m$ ).

To confirm this conclusively, Fig.4 presents an arrow plot of volume current density ( $J$ ) and the magnetic field ( $H$ ). The current in the individual elements was linear however collectively current forms a circular loop. Similarly, the magnetic field also forms circular vortex. Both of these results are a hallmark of the magnetic polaritons.



(a) Magnetic field ( $H$ ) at resonance wavelength ( $\lambda = 3.932 \mu m$ ).

(b) Current arrow plot at resonance wavelength ( $\lambda = 3.932 \mu m$ ).

Figure 5.3: (a) Magnetic field ( $H$ ) and (b) Current arrow plot at resonance wavelength ( $\lambda = 3.932 \mu m$ ) showing circular loop and vortex that confirm the presence of magnetic polaritons contributing to the absorber's high performance.

Additionally, we investigated the localized surface plasmon (LSP) contribution by analyzing electromagnetic hotspots in the top metal layer. Fig 7 shows the plot of

$|\vec{E}|$  at resonance wavelength of  $3.932\mu\text{m}$  revealing localized hotspots predominantly at the edges and corners of our metallic structure, particularly at the triangle corners, L-shaped boundaries, and H-shaped cavity regions. This field localization pattern is the characteristic signature of LSPs, confirming their significant contribution to the absorption mechanism through electromagnetic energy concentration at sub wavelength scales. By confirming LSPs, surface plasmon polaritons (SPP) mediated effects can be conclusively ruled out as the dominant mechanism which are propagating electromagnetic modes bound to the metal dielectric interface with evanescent decay perpendicular to that interface.

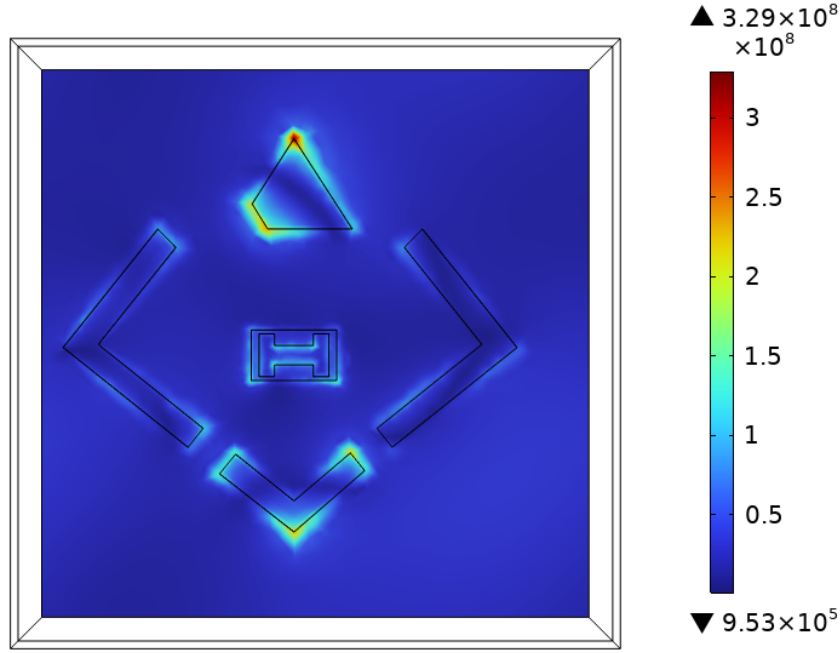


Figure 5.4: Electric field magnitude ( $|\vec{E}|$ ) at resonance wavelength ( $\lambda = 3.932\mu\text{m}$ ) showing localized hotspots at edges and corners of the metal structure, confirming the presence of LSPs.

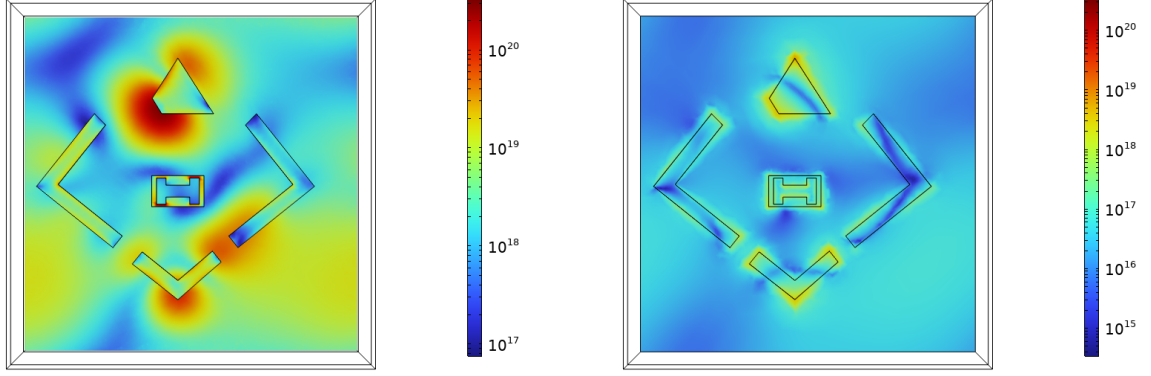
### 5.0.2 Power Dissipation and Loss Mechanisms

The COMSOL variable  $Q_h$  represents the volumetric power dissipation density (in  $\text{W}/\text{m}^3$ ) arising from both ohmic and dielectric losses in an electromagnetic simulation. Mathematically, it is represented by :

$$Q_h = \underbrace{\frac{1}{2} \sigma |\mathbf{E}|^2}_{\text{Ohmic loss}} + \underbrace{\frac{1}{2} \omega \varepsilon_0 \varepsilon'' |\mathbf{E}|^2}_{\text{Dielectric loss}} \quad (5.2)$$

A volume integration of the same was computed across the metal and dielectric layers to quantitative analyze power dissipation, which revealed that 89.1% of total losses (14.5 W) occur in the metallic layers, compared to 10.9% (1.79 W) in the dielectric spacer. This 8.9:1 ratio confirms that ohmic losses dominate the absorption mechanism, consistent with plasmonic systems. The physical reason associated with

high ohmic losses is primarily due to complex permittivity which encodes electron scattering losses in metals. The minimal dielectric contribution ensures broadband performance by avoiding narrowband resonance damping. Fig. 5.5 qualitatively quantify the power dissipation by plotting the  $Q_h$  in the metal and dielectric layers.



(a) Power dissipation density in the metal layer showing dominant ohmic losses. (b) Power dissipation density in the dielectric layer with lower losses.

Figure 5.5: Power dissipation density in (a) metal layer showing dominant ohmic losses, and (b) dielectric layer with lower losses.

### 5.0.3 Impedance Matching and Eigenfrequency Analysis

Real and imaginary parts of impedance ( $Z$ ) of the structure were calculated and plotted in Fig. 5.6 for the same wavelength range using the following relations:

$$Z_{real} = Re\left(\frac{1 + S_{11}}{1 - S_{11}}\right), Z_{imag} = Im\left(\frac{1 + S_{11}}{1 - S_{11}}\right)$$

It can be seen the real part of impedance ( $Z_{real}$ )  $\approx 1 - 1.2$  while imaginary part ( $Z_{imag}$ ) is oscillating btw  $\pm 0.2$ , which is close to 0. . This near-unity real impedance with negligible imaginary component demonstrates excellent impedance matching to free space ( $Z_o = 1$ ), further enhancing absorption.

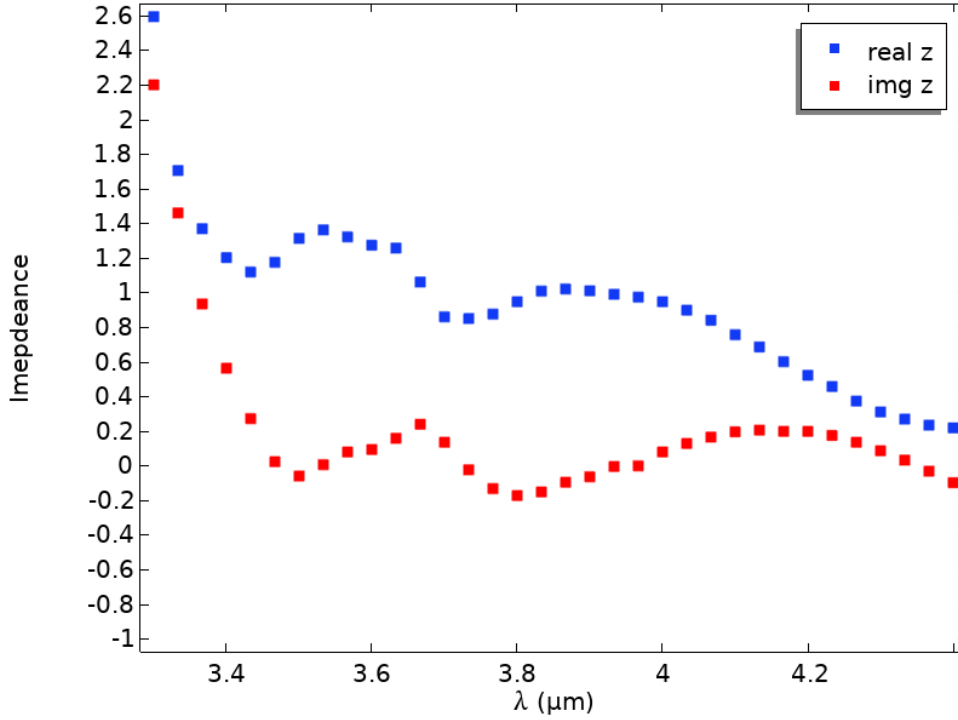


Figure 5.6: Real and imaginary parts of normalized impedance ( $Z$ ) across the operating wavelength range.

Additionally, an Eigenfrequency analysis was performed in COMSOL Multiphysics to determine the natural resonant modes of our structure. In an absorbing resonant system, the eigenfrequency are complex values complex and can be expressed as  $\omega = \omega' + i\omega''$  where  $\omega'$  is the real part and  $\omega''$  is the imaginary part. It quantifies the the damping rate of an oscillator by calculating quality factor ( $Q$ ). It is calculated using the following relation:

$$Q = \frac{\omega'}{2|\omega''|} \quad (5.3)$$

The higher- $Q$  modes ( $Q \geq 10$ ) likely contribute to specific spectral features but have less impact on the overall broadband response. Table 1 represent the eigenfrequency, frequency, and the corresponding quality factor of the structure. A few For example, the eigenfrequency at 72.902 THz has an imaginary component of 6.089 THz, yielding:

$$Q_{72.902 \text{ THz}} = \frac{72.902 \text{ THz}}{2 \times 6.089 \text{ THz}} = \frac{72.902}{12.178} = 5.9857 \quad (5.4)$$

Similarly, for the 82.326 THz mode with an imaginary component of 9.169 THz:

$$Q_{82.326 \text{ THz}} = \frac{82.326 \text{ THz}}{2 \times 9.169 \text{ THz}} = \frac{82.326}{18.338} = 4.4892 \quad (5.5)$$

The results reveal multiple resonant modes within our operating band (3.4-4.1  $\mu\text{m}$ ), with  $Q$ -factors ranging from 4.48 to 38.3. This close correlation between the absorption-derived  $Q$ -factor (5.36) and the eigenfrequency analysis  $Q$ -factors (5.9 and 4.4) confirms that these low- $Q$  modes are the dominant contributors to the broadband absorption behavior.

Table 5.1: Eigenfrequencies, Frequencies, and Quality Factors

Eigenfrequency (THz)	Frequency (THz)	Quality factor (1)
66.608+1.4454i	66.608	23.041
71.047+4.3745i	71.047	8.1206
72.902+6.0897i	72.902	5.9857
74.699+2.7434i	74.699	13.614
76.896+1.2444i	76.896	30.897
78.096+1.2928i	78.096	30.204
81.389+1.1169i	81.389	36.437
82.326+9.1694i	82.326	4.4892
83.982+1.2523i	83.982	33.532
85.325+1.2481i	85.325	34.183
85.713+1.1194i	85.713	38.287
87.187+2.6780i	87.187	16.278

### 5.0.4 Angular Stability Analysis

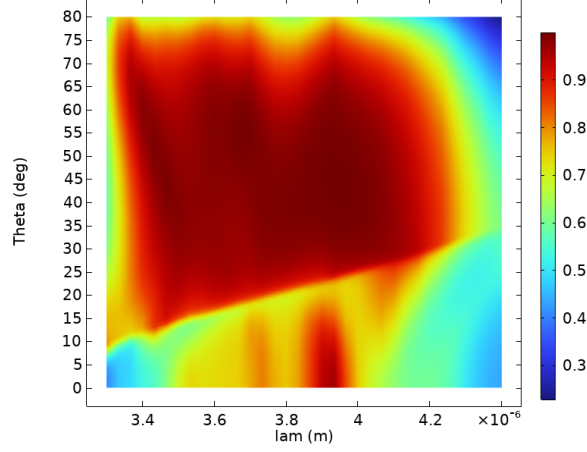
We assessed the angular stability of our structure by presenting a 2 dimensional heat map of the absorption spectrum for different elevation angles  $\theta$  (Fig 5.7 (a )) and incident angle  $\phi$  (Fig 5.7 (b)). Figure number 5.7 shows majority of the graph is dominated by the red and orange color indicating high absorption for majority of elevation angles  $\theta$ . The peak absorption is represented by dark red absorbed across 3 separate wavelength ranges from 3.3 to 3.5  $\mu m$  for  $\theta = 35^\circ$  to  $50^\circ$ , 3.55 to 3.7  $\mu m$  for  $\theta = 45^\circ$  to  $62^\circ$  and 3.85 to 4.0  $\mu m$  for  $\theta = 35^\circ$  to  $60^\circ$ . The absorption performance dips for small elevation angles ( $\theta = 0^\circ$  to  $25^\circ$ ) except for 3 small patches specially the one which spans across 3.85 to 3.95  $\mu m$  wavelength range. Similarly, the absorption performance starts dips for large elevation angles ( $\theta = 70^\circ$  to  $90^\circ$ ) which is shown in yellow green color. The absorption performance is also stable for incident angles ( $\phi$ ) up to  $45^\circ$ . The high absorption shows a parabola profile. In particular, at  $\lambda = 3.33 \mu m$ , the absorption shows a consistent high performance reaching maximum at  $\phi = 35^\circ$ . As wavelength increases stability increases with maximum stability achieved in centre ( $\lambda = 3.85 \mu m$ ), where the high absorption is stable upto  $\phi = 45^\circ$ . On the further increasing the wavelength, the stability diminishes, returning to a maximum stable angle of  $\phi = 35^\circ$  at  $\lambda = 4.10 \mu m$ . Absorption performance degrades at high angles ( $\theta > 50^\circ$ ) except in the middle region, wavelength range of 3.75 – 4.0  $\mu m$  where the proposed structure still shows high absorption upto  $\phi = 75^\circ$ .

Table 5.2: Elevation-angle ( $\theta$ ) Dependence of Absorption

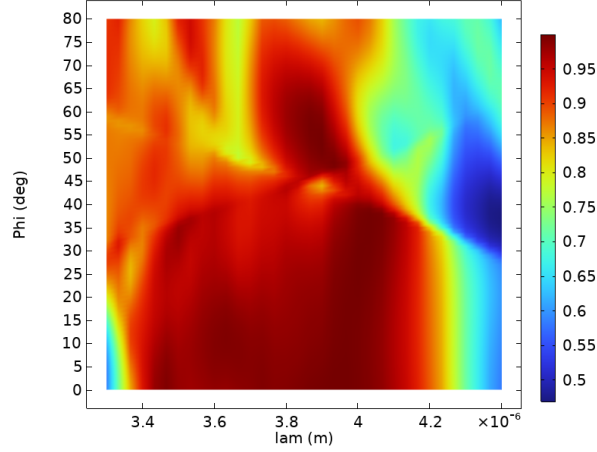
$\theta$ range	Absorption level	Wavelength band(s) ( $\mu m$ )	Notes
$0^\circ$ – $25^\circ$	Low (dips)	—	Except small patches at 3.85–3.95
$35^\circ$ – $50^\circ$	High (peak)	3.30–3.50	Dark-red hotspots
$45^\circ$ – $62^\circ$	High (peak)	3.55–3.70	Dark-red hotspots
$35^\circ$ – $60^\circ$	High (peak)	3.85–4.00	Dark-red hotspots
$70^\circ$ – $90^\circ$	Low (dips)	—	Yellow-green regions
$> 50^\circ$	Mixed (mostly low)	3.75–4.00	High absorption up to $\phi = 75^\circ$ in mid-bar

Table 5.3: Incident-angle ( $\phi$ ) Stability of High Absorption

$\lambda$ ( $\mu\text{m}$ )	Stable $\phi$ range	Peak $\phi$	Notes
3.33	up to $35^\circ$	$35^\circ$	Monotonic rise, maximum at $35^\circ$
3.85	up to $45^\circ$	$45^\circ$	Broadest angular stability
4.10	up to $35^\circ$	$35^\circ$	Stability diminishes beyond this point



(a) Absorption spectra for different elevation angles ( $\theta$ ) at fixed incident angle ( $\phi = 0^\circ$ ).



(b) Absorption spectra for different incident angles ( $\phi$ ) at fixed elevation angle ( $\theta = 45^\circ$ ).

Figure 5.7: Absorption spectra of the metamaterial absorber for (a) different elevation angles ( $\theta$ ) at fixed incident angle ( $\phi = 0^\circ$ ) and (b) different incident angles ( $\phi$ ) at fixed elevation angle ( $\theta = 45^\circ$ ).

## Chapter 6

### CONCLUSION AND FUTURE SCOPE

In this paper, a metamaterial structure is designed and simulated with novel geometry that is simpler complex geometry like fractal designs. The top metal layer comprises of an outer frame formed by a triangle at the top with a cut on the bottom left corner, an L-shaped boundary on the sides and bottom, and a central rectangle with an H-shaped cavity. The structure was able to achieve over 98% average absorption across a  $0.7\ \mu\text{m}$  bandwidth in the mid-infrared region ( $3.4\text{--}4.1\ \mu\text{m}$ ) with a peak absorption of  $\approx 99.99\%$  at  $\lambda \approx 3.932\ \mu\text{m}$ . The primary reasons for high absorption were impedance matching, existence of magnetic polaritons and presence of localized surface plasmons (LSPs) at structural hotspots such as triangle corners and H-cavity edges. The absorber also demonstrated decent angular-dependent absorption characteristics, maintaining over 90% absorption in the  $3.4\text{--}4.1\ \mu\text{m}$  wavelength range for incident angles ( $\phi$ ) up to  $40^\circ$  and elevation angles ( $\theta$ ) from  $30^\circ$  to  $65^\circ$ . However, the performance degraded for incident angles  $> 40^\circ$  and extreme elevation angles. Eigenfrequency analysis further confirmed the dominance of low- $Q$  resonant modes in sustaining broadband response, while power dissipation studies revealed that over 89% of the absorption losses originated from ohmic dissipation in metallic layers, consistent with plasmonic behavior. The high absorption efficiency, broadband response, and angular stability make the proposed absorber highly suitable for applications such as thermal emission and infrared detection systems. The proposed design also addresses practical implementation challenges by utilizing fabrication-friendly dimensions and efficient material usage, making it a significant step toward real-world metamaterial absorber applications. Furthermore, the proposed structure bridges the performance gap between narrowband and ultra broadband metamaterial absorbers by achieving average absorption while maintaining a moderate bandwidth. As mentioned in the introduction, this work is currently limited to numerical design and simulation; experimental validation is beyond its scope and will be pursued in future work.

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## Appendix A

### A.1 Replication of Yang Bai *et al.* Work

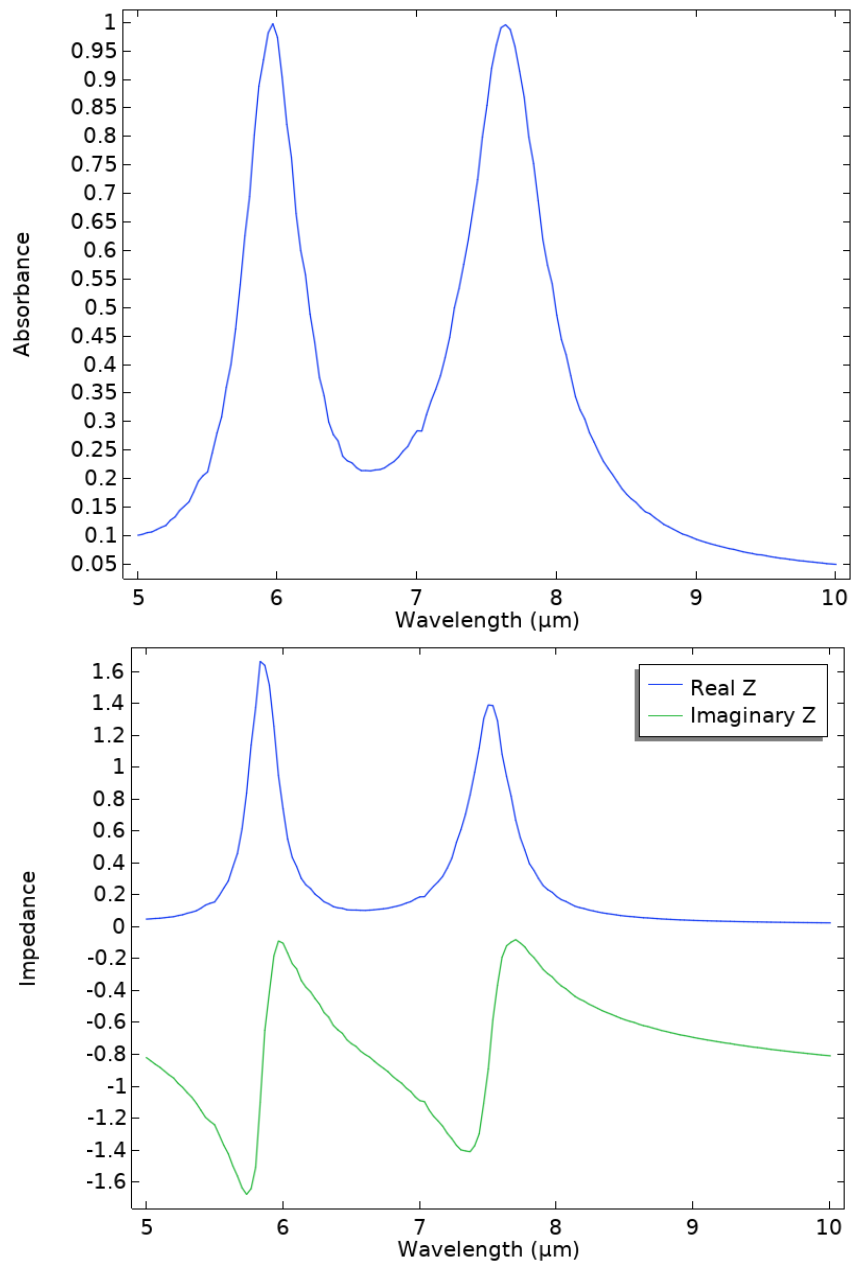


Figure A.1: Replication of Yang Bai *et al.* work in Comsol Multiphysics.

## A.2 Initial Designs of Metamaterial Absorber

### 1. Nested L shape :

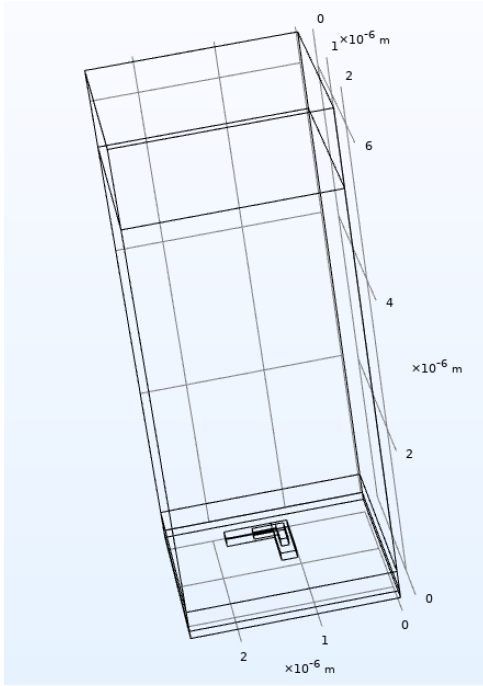


Figure A.2: Side view of the nested L structure.

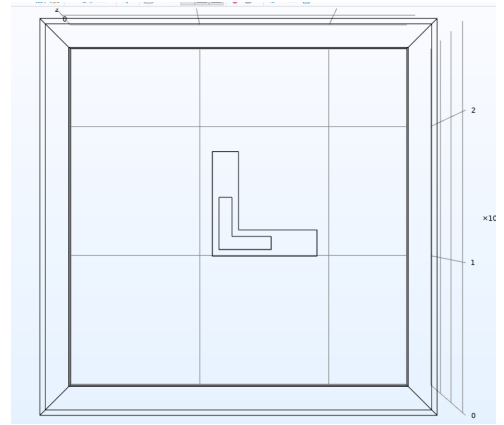


Figure A.3: Top view of the nested L structure.

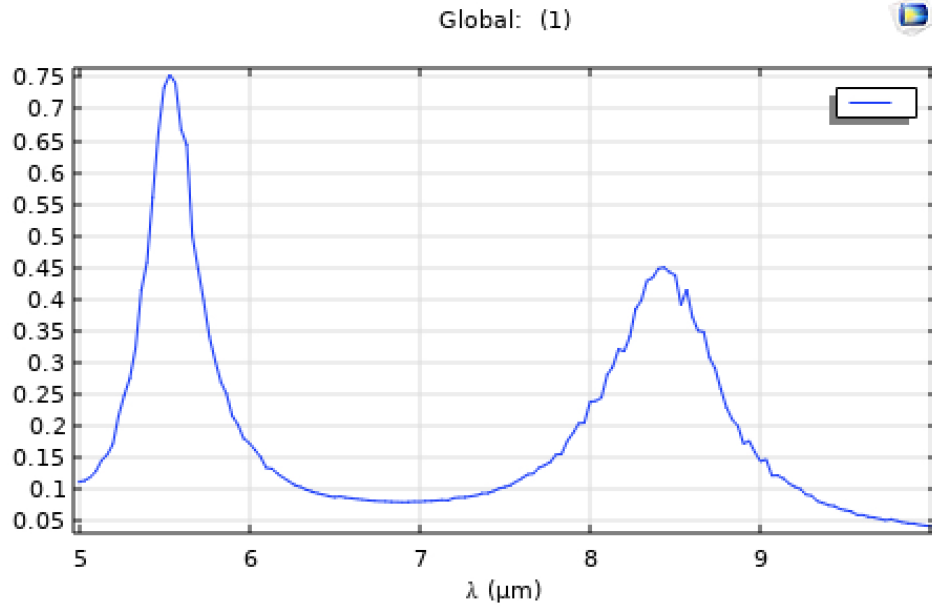


Figure A.4: Absorption curve of the nested L structure, showing two peaks. The max absorbtion is 75%

## 2. Hexagon-Nested L shape:

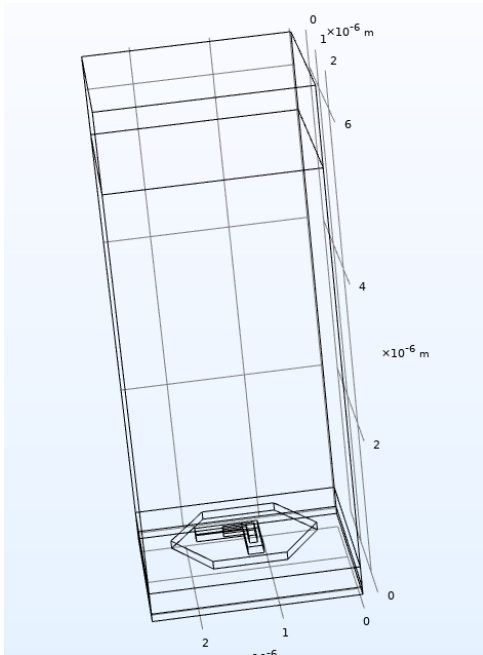


Figure A.5: Side view of the Hexagon nested L structure.

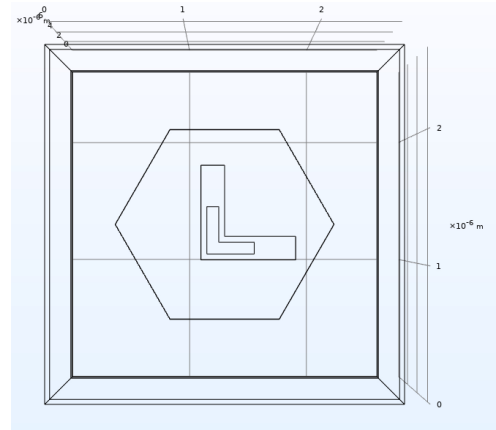


Figure A.6: Top view of the Hexagon nested L structure.

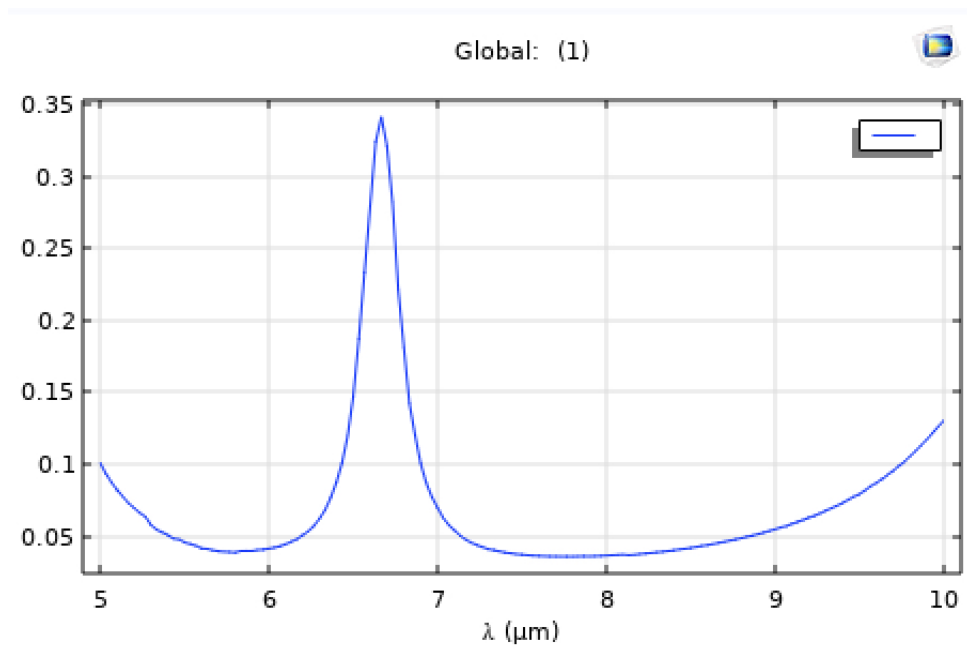


Figure A.7: Absorption curve of the Hexagon Nested L structure, showing only 1 peak. with almost no absorbtion.

### 3. Double I structre

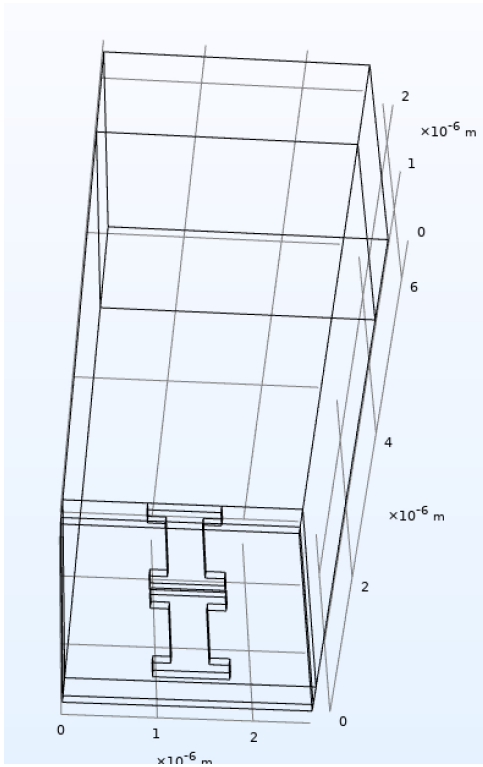


Figure A.8: Side view of the double I structure.

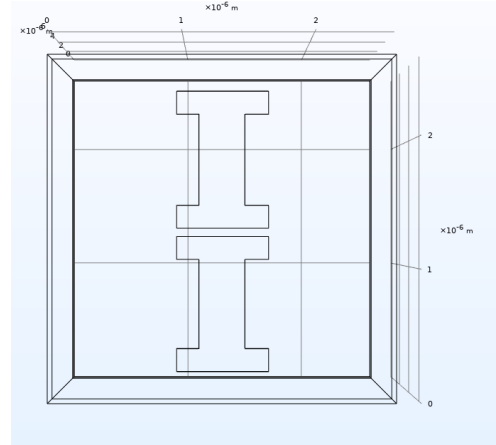


Figure A.9: Top view of the double I structure.

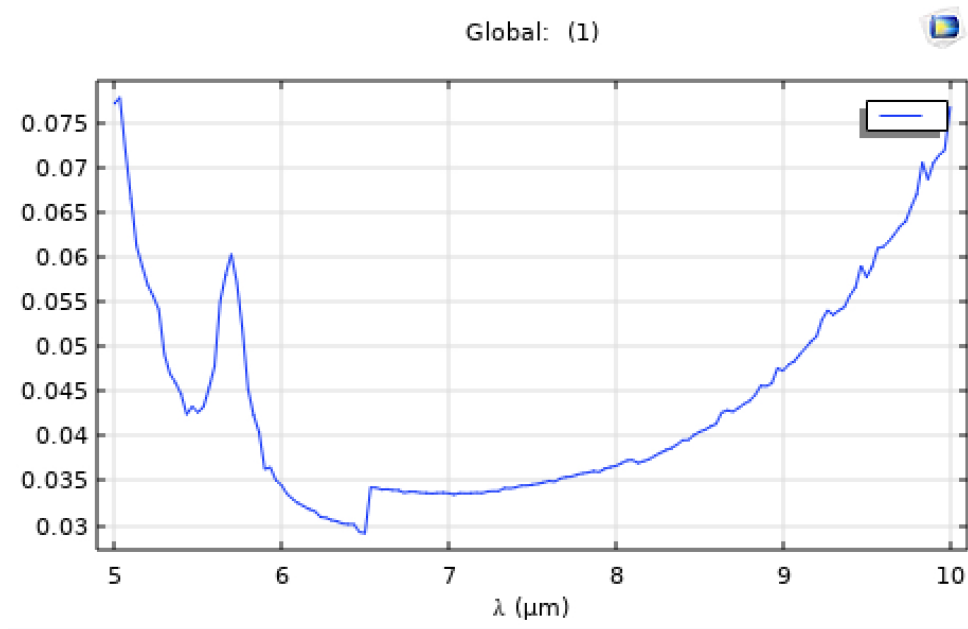


Figure A.10: Absorption curve of the double I structure, showing 1 only peak. with almost no absorbtion.

#### 4. Double D structure :

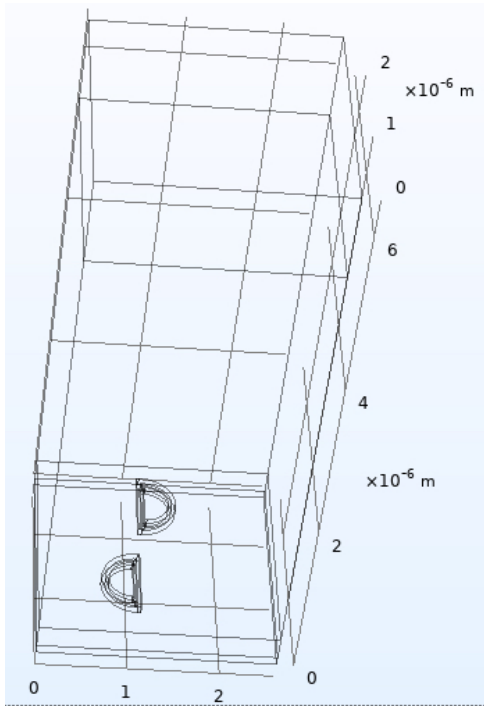


Figure A.11: Side view of the double D structure.

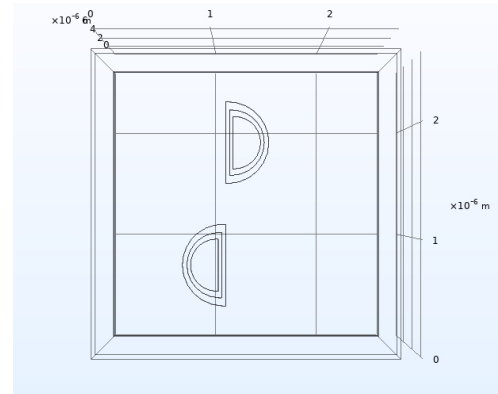


Figure A.12: Top view of the double D structure.

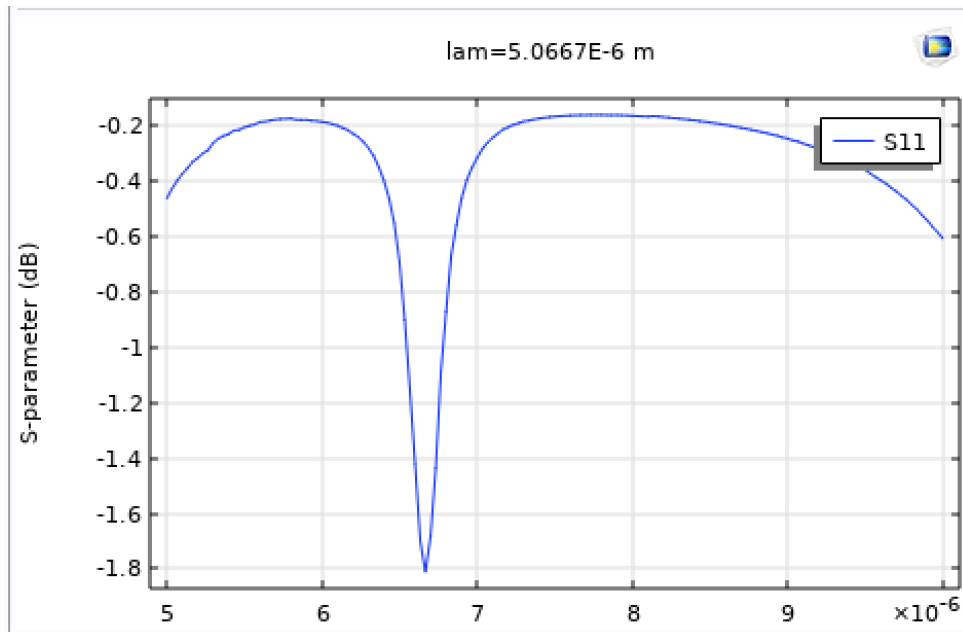


Figure A.13: Reflection curve (S11 parameter in dB scale) of the double D structure, showing only 1 peak. with almost no absorbtion.

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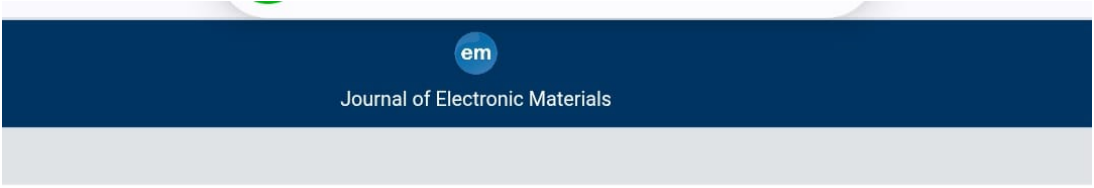
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