# EXISTENCE OF TOPOLOGICAL PHASE IN $RbCd_4As_3$ : A FIRST PRINCIPLES STUDY

A PROJECT REPORT

SUBMITTED IN PARTIAL FULFILLMENT OF THE REQUIREMENTS FOR THE AWARD OF THE DEGREE OF

## MASTER OF SCIENCE IN PHYSICS

Submitted by

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Under the supervision of

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project would not have been successful.

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## **Abstract**

In this work, we report topological phase in the layered arsenide  $RbCd_4As_3$  using first-principles calculations. We find that  $RbCd_4As_3$ , have topological band inversion at  $\Gamma$  point, which verifies the topological nature. Also, a small spin-orbit band gap of 0.1559 eV is observed at  $\Gamma$  point. Further verification of the topological nature is carried out by calculating the  $Z_2$  topological invariants. The parity product of valance bands shows non-zero value of  $Z_2$  topological invariant. Surface density of state (SDOS) study shows existence of Dirac cone near the Fermi level. Conducting surface states near the Fermi level, as observed in SDOS, confirm the topological non-trivial nature of  $RbCd_4As_3$ .

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#### LIST OF ABBREVIATIONS AND SYMBOLS

- 1. PDOS: Partial Density of States
- 2. DOS: Density of States
- 3. E F: Fermi Energy
- 4. TRIM: Time Reversal Invariant Momenta
- 5. SOC: Spin-Orbit Coupling
- 6. TRS: Time Reversal Symmetry
- 7. TI: Topological Insulators
- 8. TCI: Topological Crystalline Insulators
- 9. TSM: Topological Semi-Metal
- 10. TM: Topological Material
- 11. BZ: Brillion Zone
- 12. MLWF: Maximally Localized Wannier Function
- 13. DFT: Density Functional Theory
- 14. VASP: Vienna ab-initio simulation tool
- 15. PAW: Projector Augmented Wave Formalism
- 16. GGA: Generalized Gradient Approximation
- 17. PBE: Perdew-Burke Ernzehrof
- 18. E-CF: Exchange-Correlation Function
- 19. LDA: Local Density Approximation
- 20. ARPES: Angle-Resolved Photo-emission Spectroscopy
- 21. g: Genus Number
- 22. (v0: v1, v2, v3): Z<sub>2</sub> Invariant
- 23. a1, a2, a3: Reciprocal Primitive Lattice Vectors

## Chapter 1

## INTRODUCTION

# 1.1 Topology

The branch of Topology deals with the attributes of a topological space under continuous deformations excluding wear and tear. A famous example is of a coffee mug and a donut. Since both have only one hole, they can be transformed into one another by stretching. This hole is an example of a topological invariant. A **Topological Invariant** is a parameter that remains constant in a topological space during a topological transformation.



FIGURE 1. Example of a Donut being topologically transformed into a Coffee Mug. Both are topologically equivalent since both have genus number = 1. [1]

The theorem governing this concept is the **Gauss-Bonnet Theorem**. If we integrate a closed surface curvature over its surface, then we get a topological invariant.

For a Torus or a sphere, the following equation is the Gauss-Bonnet Theorem Equation,

$$\int_{M} \kappa dA = 2\pi \chi = 2\pi (2 - 2g) \tag{1}$$

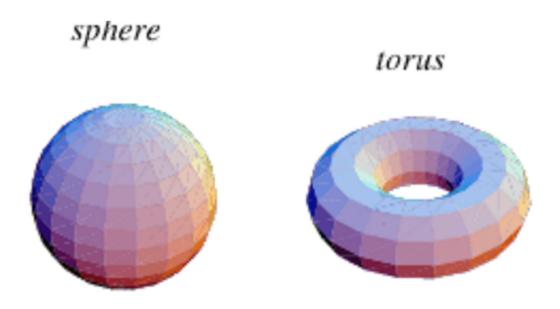


FIGURE 2. Sphere and Torus for which the above equation 1 depicts Gauss Bonnet Theorem [2]

In equation I, g depicts the **Genus Number** which is the number of Holes in this case, g = 0 for the sphere and g=1 for the torus. The number of holes in a topological object is always an integer. We can further understand genus number by the following image:

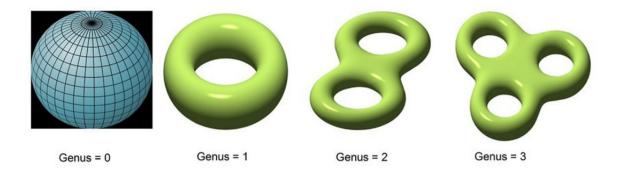


FIGURE 3. Value of g (Genus Number) for different topological surfaces, where, g depicts the number of holes. [2]

[1]

## 1.2 Topological Insulators

Condensed Matter Physics is the study of different states of matter based on the arrangement of electrons and atoms. Phases of matter transition into one another due to the phenomenon of *spontaneous symmetry breaking*. Symmetry is the property of matter that is invariant during transformations. Topological insulators also have these symmetries. Now, the band structure is formed when orbitals come close enough to expand and form an electronic band structure with an energy band gap in insulators. We can say that *all conventional insulators are topologically equivalent to each other* as they can be transformed into one another without losing the energy gap between the bands. This is what makes them different from trivial Insulators.

The electrons move in a circular motion due to the existence of a magnetic field in their vicinity. Though, electron bounces off the edges near the boundary forming half circles as shown in Figure 4.

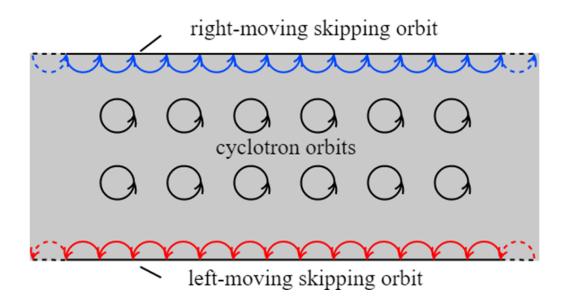


FIGURE 4. Electrons bouncing off near the edge are called the Dirac Fermions in Quantum and Skipping Orbits in Classically. The bulk electrons are in cyclotron orbits due to the presence of a magnetic field. [3]

These orbits are called **Skipping Orbits** in Classical Mechanics and **Dirac Fermions** in Quantum Mechanics. The electrons move in one direction and thus are not slowed down or obstructed by the flow of electrons in the opposite direction. At this point, **The Bulk Boundary Correspondence** comes into play which states that the bulk and boundary are connected. The *Chern Number*, n, also called the Bulk Invariant, is 0 for the insulating bulk and 1 for the Quantum Hall State. This chern number is equal to the chiral edge states of the boundary.

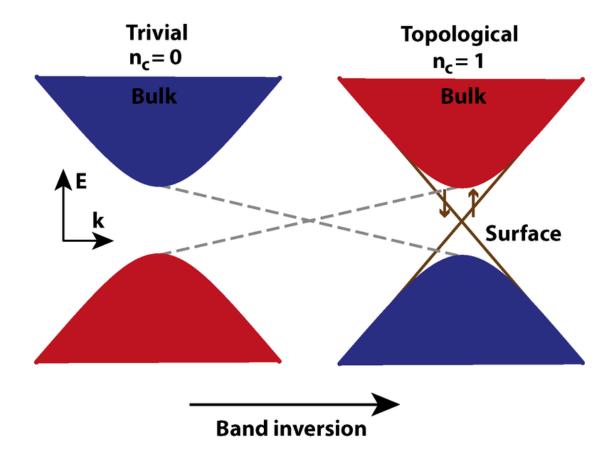


FIGURE 5. Comparison of the Band Structure of a Trivial Insulator and a Topological Insulator. The crossing across the two bands depicts the conducting edge in two-dimensional and surface states in three-dimensional samples. [4]

In Figure 5, we can see the crossing between conduction band (CB) and valence band (VB) which allows an easy pathway for the electrons to move. This edge state allows electrons to flow without dissipation, and thus the topological insulators can conduct electricity without closing the energy band gap. Also, these edge states are topologically protected, i.e. they are not distorted by deformations, just like the number of holes is protected under continuous deformation. Thus, the edge states given by the Chern number are topological invariants, which is verified by the Bulk-Boundary theorem.

# Chapter 2

#### **OUR WORK AND MOTIVATION**

Topological Materials (TMs) have a broad application in Spintronics [5], Quantum Computing [6], Chemical Catalysis [7], and Thermoelectric Materials [8]. The phenomena exhibited by these materials such as magnetoresistance [9], chiral anomaly [10], and Weyl Fermion quantum transport [11] are increasing their popularity amongst the research community.

TMs can be divided into several categories such as Topological Semi-metals (TSM), Topological insulators (TI), Topological Crystalline Insulators (TCI), and many more. TSMs show gapless electronic states exhibiting crossing of VB and CB near the level of Fermi energy  $(E_F)$  [12]. They can be categorized into several categories such as Dirac Semi-metals, Weyl semimetals, Nodal line semimetals, and more [13-16] based on the degeneracy, co-dimension, dispersion, and origin of the band crossing. TIs have insulating bulk and gapless boundary states (2D) and gapless surface states (3D) [17-19]. Non-trivial TIs have an odd number of surface Dirac cones whereas an even number of cones makes them trivial. The non-triviality preserve Time Reversal Symmetry (TRS) and leads to some exotic properties. Other Symmetries such as crystal symmetries also conserve the quantum phenomenon in a TI and such TIs are termed as Topological Crystalline Insulators (TCIs). There are different types of TCIs that exhibit mirror symmetry as in the SnTe family [20,21] and Rotational Symmetry [22] as observed in  $\alpha - Bi_4Br_4$  [23].

ARPES experimental study and Density Functional Theory (DFT) analysis of  $NaCd_4As_3$  show that it has TCI characteristics at room temperature which converts to TI upon lowering the temperature [24]. Thus, the TCI conve happens due to the broken mirror symmetry[24]. Besides,  $NaCd_4As_3$  have been reported as a part of two Zintl Phases series namely,  $DCd_4Q_3$  and  $DZn_4Q_3$  (D = Na, K, Rb, Cs; Q = As, P), in which respective elements have been used to compose 12 complex structures including layered arsenide like  $NaCd_4As_3$ ,  $NaZn_4As_3$ ,  $NaCd_4As_3$ ,  $KCd_4As_3$ , and  $RbCd_4As_3$  [25,26]. There are structural similarities found in these layered arsenides as established by X-ray Diffraction (XRD) [25,26]. Moreover, the stable crystal structure of  $RbCd_4As_3$  has been experimentally synthesized and the calculations of the Band Energy Structure and its properties have been reported without considering the interaction between the spin and the orbital angular momentum (SOC) [25]. However, including spin-orbit interaction in band structure calculation has immoderate shifts in the topology of a material as observed in  $Bi_2Se_3$  [27]. Even the strength of the spin-orbit interaction can be enhanced by various methods like chemical doping [28], applying a magnetic field [29], or increasing hydrostatic pressure [30].

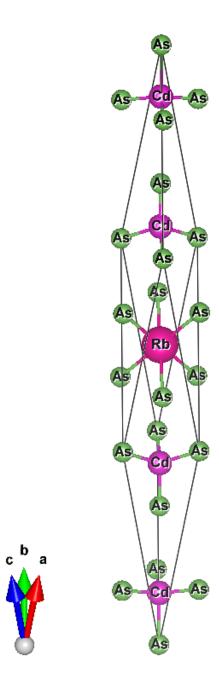


FIGURE 6.  $RbCd_4As_3$ 

Thus, the experimental observation of topological phase transition in  $NaCd_4As_3$  and the similarity of structure with  $RbCd_4As_3$ , makes it interesting to study the electronic and topological properties of  $RbCd_4As_3$  [24-26] under the effect of SOC.

Hence, we have probed the topological structure of the material  $RbCd_4As_3$  using the first-principle calculations and found that  $RbCd_4As_3$  shows a topological phase with SOC. Further, the topological nature is also verified by surface states visualized in (001) plane.

## Chapter 3

#### COMPUTATIONAL METHODOLOGY

To evaluate the band structure properties of  $RbCd_4As_3$ , we used the DFT calculations [31,32] as accoutered in Vienna ab-initio simulation tool (VASP) [33] such that the calculations are carried out with the projector augmented wave formalism(PAW) [34]. To include the exchangecorrelation function as in PAW formalism, we used the method of first order correction in electron density, i.e., the Generalized Gradient Approximation (GGA). Further, we have used the most common functional of GGA, which is the Perdew-Burke Ernzehrof (PBE) [35,36] considering the spin-orbit coupling. The structural relaxation of  $RbCd_4As_3$  is performed using the strict energy convergence criteria of  $1 \times 10$ -6 eV. To calculate structural properties and the electronic band structure, the limit of kinetic energy is set at 520 eV. To sample a Brillion Zone (BZ) in rhombohedral structure, a 7x7x3 size Gamma-centered k-mesh is used. Fermi level is broadened with a width of 0.001 eV using Gaussian smearing. We used 0.001 eV/A force for each atom to obtain the relaxed atomic structure of a unit cell. Using maximally localized Wannier Functions [37], for tight-binding models to produce the band structure under the influence of the spin-orbit interplay constructed by Wannier90 code [38]. Besides, we used the respective Wannier tools to evaluate the resultant tight-binding Hamiltonian to finally obtain the surface states of  $RbCd_4As_3$  [39].

# 3.1 Density Functional Theory (DFT)

To deepen our understanding of many-body systems such as more than one electron atom, we imply an approximation technique called the Density Functional Theory (DFT) [40]. It is feasible to solve Schrodinger equation for a one-electron system but not for a multi-electron system. Thus, we take some approximations like:

## 3.1.1 Born-Oppenheimer Approximation

This assumes respective atomic nucleus to be fixed since the its motion is not as fast as an electron, rather relatively much slower.

## 3.1.2 Hohenberg-Kohn Theorem

According to this concept, if we consider the n = 0 state energy, then it will be the function of another function, i.e. a Functional of the electron density because to evaluate the ground state properties like the energy, momentum, and others, one can exploit electron density.

#### **Exchange-Correlation Function (E-CF)**

Electrons interact with each other via coulomb charge and their spins. All this quantum mechanical information is stored in the E-CF.

The Kohn-Sham Equations of DFT are as follows[41]:

$$[-0.5\nabla^2 + p_{ext}(x) + p_H(x) + P_{XC}(x)]\varphi_i(x) = \epsilon_i \varphi_i(x)$$
(1)

where,  $-\frac{1}{2}\nabla^2$  denotes Kinetic Energy,  $p_{ext}(x)$  depicts potential applied externally,  $p_H(x)$  is a quantity named after a scientist, Hartree Potential, and  $P_{XC}(x)$  is the E-C Potential .

The E-CP is given be the formula:

$$P_{XC}(x) = \frac{\delta E_{XC}}{\delta m(r)} \tag{2}$$

There are multiple Exchange-Correlation Functionals with different accuracy and feasibility as shown in the following figure:

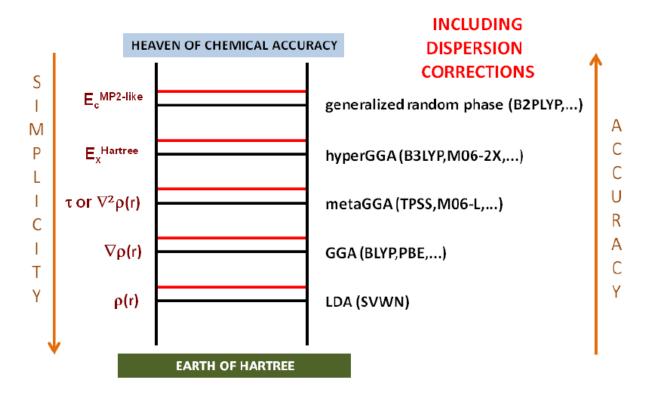


FIGURE 7. Jacobs ladder approach for the systematic improvement of DFT functionals[42]

The simplest is the Hartree approximation with the lowest accuracy. As we move up the ladder the accuracy increases towards more practical approximations. Here, **LDA** is the *Local* 

Density Approximation. It takes only the electron density as a functional. It conserves the most time but is the least accurate. Next is the **GGA** Approximation which is the *Generalised Gradient Approximation*. It includes the first-order correction for Electron Density. It takes up more time than LDA but still, it is extremely fast. This is the method that we have used. Its governing equation is as follows[35]:

$$E_{EX}^{GGA} = \int \epsilon_{EX}^{GGA}(n, \nabla n) d^3r$$
 (3)

We have the PBE functional of the GGA Functional which is the popular choice for accurate and simple calculations in Solid State Physics[36]. In this, The parameters of the functionals are not empirically determined. Similarly, other Exchange-Correlation Functionals are MetaGGA [43,44], which takes the doubly corrected electron density, hyperGGA, and generalized random phase.

For all DFT Packages, the input of atomic positions is required. This task is done by using multiple molecule editing software like VESTA, Avogadro, etc. We have used VESTA for our molecule[45].

# Chapter 4

## RESULTS AND DISCUSSION

We investigate the alkali metal layered arsenide  $RbCd_4As_3$  band structure for its topological nature.  $RbCd_4As_3$  is experimentally synthesized in space group  $R\overline{3}m$  (166) in the rhombohedral phase. We took the lattice parameters a (4.4752 Å) and c (36.946 Å) from the reported experimental study [25]. For this study, we used the primitive structure to avoid band-folding with atomic positions as shown in Fig. 7(a). To understand our system, we need to evaluate the available modes for electrons around the nucleus, which is given by the projected density of states (PDOS). For our molecule  $RbCd_4As_3$ , the DOS can be seen in Fig. 7(b). We observe that in the valence band, the DOS majorly consists of p-orbitals of As near the fermi-level whereas the s-orbital of Cd vanishes. On the contrary, in the conduction band, both orbitals have similar contributions near 0 eV.

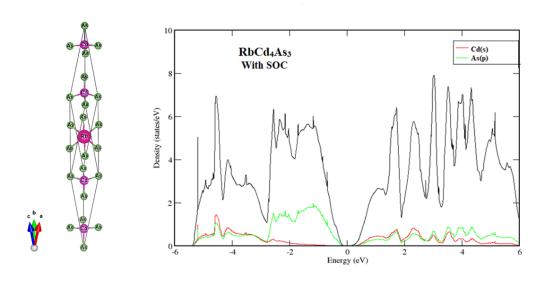


FIGURE 8. (a) Primitive Structure of  $RbCd_4As_3$ ; (b) Projected Density of States (PDOS) of  $RbCd_4As_3$  with consideration of contribution from Cd and As. The  $E_F$  is set to 0 eV

The calculation for electronic band for the cases where SOC is considered and where it isn't can be seen in Fig. 8. The band calculation is executed taking a specific path out which some points follow the equation S + Q = -S, where S is the Specific point which is extremely

To further investigate  $RbCd_4As_3$  topology, we calculate the parity of the system at TRIM points. For 3D systems,  $Z_2$ -invariants are  $(\nu_0: \nu_1, \nu_2, \nu_3)$  whose values are governed by the following equations, as suggested by Kane and Mele [18,46,47]:

$$(-1)^{\nu_0} = \Pi_i \delta_i \tag{1}$$

$$(-1)^{\nu_{i=1,2,3}} = \prod_{m_{j\neq i} \& m_{i=1} \delta_{m_1 m_2 m_3}}$$
 (2)

Where  $\Pi_i$   $\delta_i$  denotes the parity products for filled valence bands at all TRIM points and the index value gives the class. These equations are applicable only for systems with inversion symmetry and Time Reversal Symmetry (TRS). There are eight TRIM points that can be calculated using equation (3)[18,46,47].

$$G_{i=m_1m_2m_3} = \frac{m_1a_1 + m_2a_2 + m_3a_3}{2} \tag{3}$$

Here,  $m_1, m_2, m_3$  can take values as 0 and 1 and they are multiplied by the reciprocal lattice points respectively. The nature or strength of the topological insulator can be determined by the value of  $\nu_0$  calculated using equation (1). For  $\nu_0=1$ , is the sign that the molecule being considered is a good TI, whereas for  $\nu_0=0$ , it is trivial or weak in nature. The values of  $\nu_1, \nu_2$ , and  $\nu_3$ , given by equation (2) are used to distinguish between a weak TI and a trivial insulator. The parity for valence bands at all TRIM points for band structure calculations with spin-orbit coupling is shown in Table 1. It can be observed that the product of all TRIM points is (-). The value of the  $Z_2$  index  $\nu_0$  as calculated from equation (1) comes out to be 1. This verifies that  $RbCd_4As_3$  have strong topological nature.

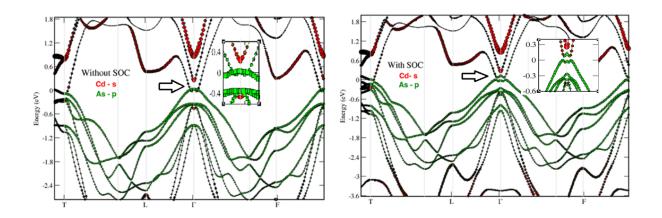


FIGURE 9. Band structures of  $RbCd_4As_3$  (a) without the SOC effect and (b) with SOC. Red spheres show the contribution of Cd's s-orbital and green spheres show the contribution of the p-orbital of As atom to the bands near the  $E_F = 0$  eV.

TRIM Points	Parity
Γ	-
3L	-
3F	-
Т	+
Resultant	-

TABLE 1. Band Structure Parities at TRIM points of 1st BZ of  $RbCd_4As_3$  for primitive structure with SOC.

Additionally, Bloch Energies of  $RbCd_4As_3$  are utilized to get the maximally localized wannier function (MLWF) as shown in Fig. 8(b). Since the MLWFs we obtained are not dependent on the basis set used to obtain Bloch states [38], we can use them to calculate band structure in wannier space and verify the band structure obtained from Bloch states. The calculated band structure in wannier space can be observed in Fig. 9(a).

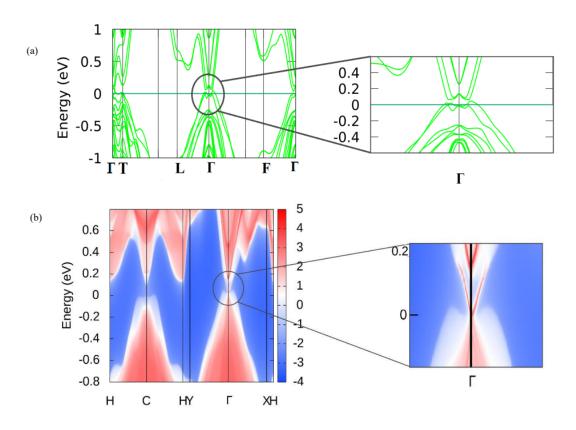


FIGURE 10. (a) Band Structure of  $RbCd_4As_3$  in wannier space with band gap induced at  $\Gamma$  due to spin-orbit coupling. Magnified image of the band gap induced at  $\Gamma$  point is shown. (b) Surface Density of States for (001) surface of  $RbCd_4As_3$  calculated with spin-orbit coupling. Formation of a single Dirac cone is seen at  $\Gamma$ .

In the Fig.9(a), a small spin-orbit energy band-gap is seen at the symmetric point  $\Gamma$ . This is observed in the wannier band structure and perfectly coincides with Bloch structure, thus verifying it (Fig.8(b)). Further, we used MLWFs to perform surface state calculations for (001) surface of  $RbCd_4As_3$  taking into account the Green's impulse response. From our first-principle calculations, we derive a Hamiltonian to have the information of surface states. This is facilitated by a Tight-Binding Model. The resulting Surface Density of States (SDOS) forms only one cone (Dirac) at  $\Gamma$  as shown in Fig.9(b). This is in agreement with the spin-orbit band gap observed in Fig. 8(b) and Fig. 9(a). The presence of conducting surface state on (001) plane of  $RbCd_4As_3$  is validated by looking at these figures due to odd number of Dirac cones. The existence of topological band inversion and conducting surface state along with a surface Dirac cone near the Fermi level shows that  $RbCd_4As_3$  has non-trivial topological nature.

A topological insulator can generally be good thermoelectric material.  $RbCd_4As_3$  is a Zintl compound and on preliminary transport calculations Zintl Compounds are suggested to be good thermoelectric materials [8]. Besides,  $RbZn_{43}$  is also a member of this family and is proven to be a thermoelectric material [25]. Another member of this family is  $NaCd_4As_3$ , which is shown to have the desired value of variables that supports the thermoelectricity. These variables are electrical conductivity and Seebeck coefficient [25] and the existence of a topological phase is also seen with it[24], indicating a strong possibility of possessing thermoelectric properties. Hence, it would be worthwhile to investigate  $RbCd_4As_3$  and other materials of this family for having thermoelectric properties for which our study can be used.

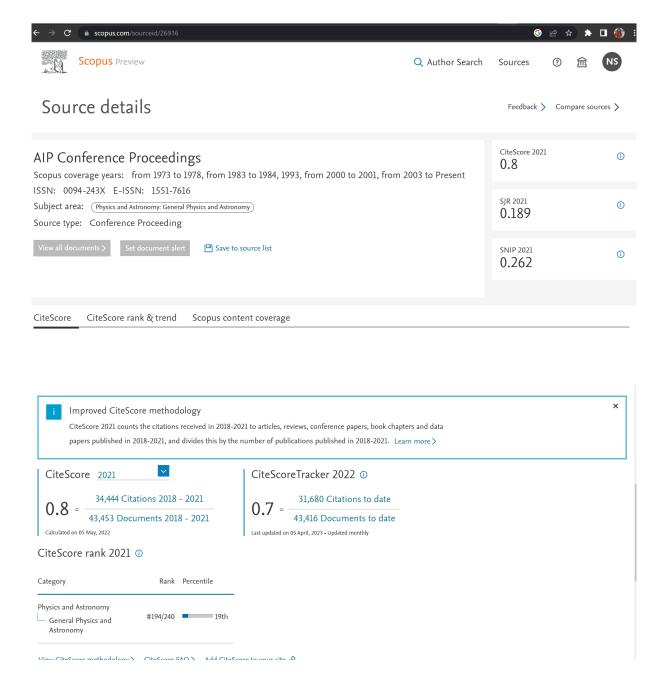
## Chapter 5

#### CONCLUSION

Topological properties for the alkali metal layered arsenide  $RbCd_4As_3$  have been studied using the DFT approximation. Also, stable rhombohedral structure with space group 166 is considered to study the band structure of  $RbCd_4As_3$ . We have observed a single band inversion at  $\Gamma$ -point under the consideration of the SOC and small spin momentum and orbit momentum interaction band gap of 0.1559 eV. The orbital contribution during the inversion can be attributed to the respective atoms Cadmium (s) and Arsenic (p). Besides, the  $Z_2$  values are determined to verify topological phase. The multiplication result of parities computed at multiple TRIM points has shown that  $Z_2$  index  $\nu_0 = 1$ . This has suggested that  $RbCd_4As_3$  is topologically non-trivial. The Surface density of the state has also verified the existence of a single Dirac cone and conducting surface state in  $RbCd_4As_3$ . The band inversion and surface state study of  $RbCd_4As_3$  have confirmed its topologically non-trivial nature. We hope that future experimental studies will verify its topological nature as the surface state can be observed with the help of Angle-Resolved Photo-emission Spectroscopy (ARPES).

# Chapter 6

## PROOF OF SCOPUS INDEXING



### **Bibliography**

- [1] D. Thimmesch, "These 3D Printed Porcelain Coffee Mugs & Donuts are Clever Topology-Related Joke", <a href="https://www.scribbr.com/ieee/ieee-website-citation/#:~:text=To%20write%20an%20IEEE%20reference,or%20removed%20in%20the%20future">https://www.scribbr.com/ieee/ieee-website-citation/#:~:text=To%20write%20an%20IEEE%20reference,or%20removed%20in%20the%20future</a>. (4/24, 2023)
- [2] Y. Tibrewal, "Interesting Shapes: Why is a doughnut equivalent to a coffee mug?", <a href="https://tomrocksmaths.com/2021/08/09/interesting-shapes-why-is-a-doughnut-equivalent-to-a-coffee-mug/">https://tomrocksmaths.com/2021/08/09/interesting-shapes-why-is-a-doughnut-equivalent-to-a-coffee-mug/</a> (4/24, 2023)
- [3] Topology course team, Copyright 2021, TU Delft, CC-BY-SA 4.0 (materials) & BSD (code), "Where do the pumped electrons come from and go to?", <a href="https://topocondmat.org/w3\_pump\_QHE/QHEedgestates.html">https://topocondmat.org/w3\_pump\_QHE/QHEedgestates.html</a> (4/24, 2023)
- [4] M. Hakl, "Magneto-optics of relativistic-like electrons in 3D solids", <a href="https://www.researchgate.net/figure/An-illustration-of-two-types-of-the-insulator-with-different-band-orderings-trivial\_fig1\_322927285">https://www.researchgate.net/figure/An-illustration-of-two-types-of-the-insulator-with-different-band-orderings-trivial\_fig1\_322927285</a>, (4/24, 2023)
- [5] S. A. Yang, "Dirac and Weyl materials: Fundamental aspects and some spintronics applications," *SPIN*, vol. 6, no. 2. 2016. doi: 10.1142/S2010324716400038.
- [6] C. Nayak, S. H. Simon, A. Stern, M. Freedman, and S. das Sarma, "Non-Abelian anyons and topological quantum computation," *Rev Mod Phys*, vol. 80, no. 3, 2008, doi: 10.1103/RevModPhys.80.1083.
- [7] C. R. Rajamathi *et al.*, "Weyl Semimetals as Hydrogen Evolution Catalysts," *Advanced Materials*, vol. 29, no. 19, 2017, doi: 10.1002/adma.201606202.
- [8] Sangeeta, R. Kumar, and M. Singh, "Realizing high thermoelectric performance in p-type RbZn4P3 Zintl compound: a first-principles investigation," *J Mater Sci*, vol. 57, no. 23, 2022, doi: 10.1007/s10853-022-06953-y.
- [9] F. F. Tafti, Q. D. Gibson, S. K. Kushwaha, N. Haldolaarachchige, and R. J. Cava, "Resistivity plateau and extreme magnetoresistance in LaSb," *Nat Phys*, vol. 12, no. 3, 2016, doi: 10.1038/nphys3581.
- [10] X. Huang *et al.*, "Observation of the chiral-anomaly-induced negative magnetoresistance: In 3D Weyl semimetal TaAs," *Phys Rev X*, vol. 5, no. 3, 2015, doi: 10.1103/PhysRevX.5.031023.
- [11] A. A. Zyuzin and A. A. Burkov, "Topological response in Weyl semimetals and the chiral anomaly," *Phys Rev B Condens Matter Mater Phys*, vol. 86, no. 11, 2012, doi: 10.1103/PhysRevB.86.115133.
- [12] J. Li, Z. Zhang, C. Wang, H. Huang, B. L. Gu, and W. Duan, "Topological semimetals from the perspective of first-principles calculations," *J Appl Phys*, vol. 128, no. 19, 2020, doi: 10.1063/5.0025396.
- [13] H. Gao, J. W. F. Venderbos, Y. Kim, and A. M. Rappe, "Topological Semimetals from First Principles," *Annu Rev Mater Res*, vol. 49, 2019, doi: 10.1146/annurev-matsci-070218-010049.
- [14] S. M. Young, S. Zaheer, J. C. Y. Teo, C. L. Kane, E. J. Mele, and A. M. Rappe, "Dirac semimetal in three dimensions," *Phys Rev Lett*, vol. 108, no. 14, 2012, doi: 10.1103/PhysRevLett.108.140405.
- [15] H. Weng, C. Fang, Z. Fang, B. Andrei Bernevig, and X. Dai, "Weyl semimetal phase in noncentrosymmetric transition-metal monophosphides," *Phys Rev X*, vol. 5, no. 1, 2015, doi: 10.1103/PhysRevX.5.011029.
- [16] A. A. Burkov, M. D. Hook, and L. Balents, "Topological nodal semimetals," *Phys Rev B Condens Matter Mater Phys*, vol. 84, no. 23, 2011, doi: 10.1103/PhysRevB.84.235126.

- [17] B. A. Bernevig, T. L. Hughes, and S. C. Zhang, "Quantum spin hall effect and topological phase transition in HgTe quantum wells," *Science* (1979), vol. 314, no. 5806, 2006, doi: 10.1126/science.1133734.
- [18] C. L. Kane and E. J. Mele, "Z<sub>2</sub> Topological Order and the Quantum Spin Hall Effect," *Phys Rev Lett*, vol. 95, no. 14, 2005.
- [19] M. Z. Hasan and C. L. Kane, "Colloquium: Topological insulators," *Rev Mod Phys*, vol. 82, no. 4, 2010, doi: 10.1103/RevModPhys.82.3045.
- [20] T. H. Hsieh, H. Lin, J. Liu, W. Duan, A. Bansil, and L. Fu, "Topological crystalline insulators in the SnTe material class," *Nat Commun*, vol. 3, 2012, doi: 10.1038/ncomms1969.
- [21] Y. Tanaka *et al.*, "Experimental realization of a topological crystalline insulator in SnTe," *Nat Phys*, vol. 8, no. 11, 2012, doi: 10.1038/nphys2442.
- [22] C. Fang and L. Fu, "New classes of topological crystalline insulators having surface rotation anomaly," *Sci Adv*, vol. 5, no. 12, 2019, doi: 10.1126/sciadv.aat2374.
- [23] C.-H. Hsu *et al.*, "Purely rotational symmetry-protected topological crystalline insulator α-Bi<sub>4</sub>Br<sub>4</sub>," *2D Mater.*, vol. 6, no. 3, 2019.
- [24] Y. Y. Wang *et al.*, "Magnetotransport properties and topological phase transition in NaCd4As3," *Phys Rev B*, vol. 102, no. 11, 2020, doi: 10.1103/PhysRevB.102.115122.
- [25] H. He, C. Tyson, and S. Bobev, "ChemInform Abstract: Eight-Coordinated Arsenic in the Zintl Phases RbCd4As3 and RbZn4As3: Synthesis and Structural Characterization.," *ChemInform*, vol. 42, no. 44, 2011, doi: 10.1002/chin.201144013.
- [26] C. Grotz, M. Baumgartner, K. M. Freitag, F. Baumer, and T. Nilges, "Polymorphism in zintl phases ACd4Pn3: Modulated structures of NaCd4Pn3 with Pn = P, As," *Inorg Chem*, vol. 55, no. 15, 2016, doi: 10.1021/acs.inorgchem.6b01233.
- [27] D. West, Y. Y. Sun, H. Wang, J. Bang, and S. B. Zhang, "Native defects in second-generation topological insulators: Effect of spin-orbit interaction on Bi<sub>2</sub>Se<sub>3</sub>," *Phys Rev B*, vol. 86, no. 12, 2012.
- [28] A. B. Maghirang *et al.*, "Predicting two-dimensional topological phases in Janus materials by substitutional doping in transition metal dichalcogenide monolayers," *NPJ 2D Mater Appl*, vol. 3, no. 1, 2019, doi: 10.1038/s41699-019-0118-2.
- [29] J. Macy *et al.*, "Magnetic field-induced non-trivial electronic topology in Fe3–xGeTe2," *Appl Phys Rev*, vol. 8, no. 4, 2021, doi: 10.1063/5.0052952.
- [30] M. Singh, R. Kumar, and R. K. Bibiyan, "Pressure-induced topological phase transition in XMR material YbAs: a first-principles study," *Eur Phys J Plus*, vol. 137, no. 5, May 2022, doi: 10.1140/epjp/s13360-022-02841-1.
- [31] A. K. Rajagopal and J. Callaway, "Inhomogeneous electron gas," *Phys Rev B*, vol. 7, no. 5, 1973, doi: 10.1103/PhysRevB.7.1912.
- [32] W. Kohn and L. J. Sham, "Self-consistent equations including exchange and correlation effects," *Physical Review*, vol. 140, no. 4A, 1965, doi: 10.1103/PhysRev.140.A1133.
- [33] G. Kresse and J. Furthmüller, "Efficient iterative schemes for ab initio total-energy calculations using a plane-wave basis set," *Phys Rev B Condens Matter Mater Phys*, vol. 54, no. 16, 1996, doi: 10.1103/PhysRevB.54.11169.
- [34] D. Joubert, "From ultrasoft pseudopotentials to the projector augmented-wave method," *Phys Rev B Condens Matter Mater Phys*, vol. 59, no. 3, 1999, doi: 10.1103/PhysRevB.59.1758.
- [35] J. P. Perdew, K. Burke, and M. Ernzerhof, "Generalized gradient approximation made simple," *Phys Rev Lett*, vol. 77, no. 18, 1996, doi: 10.1103/PhysRevLett.77.3865.

- [36] J. P. Perdew *et al.*, "Atoms, molecules, solids, and surfaces: Applications of the generalized gradient approximation for exchange and correlation," *Phys Rev B*, vol. 46, no. 11, 1992, doi: 10.1103/PhysRevB.46.6671.
- [37] N. Marzari and D. Vanderbilt, "Maximally localized generalized Wannier functions for composite energy bands," *Phys Rev B Condens Matter Mater Phys*, vol. 56, no. 20, 1997, doi: 10.1103/PhysRevB.56.12847.
- [38] A. A. Mostofi *et al.*, "An updated version of wannier90: A tool for obtaining maximally-localised Wannier functions," *Comput Phys Commun*, vol. 185, no. 8, 2014, doi: 10.1016/j.cpc.2014.05.003.
- [39] Q. S. Wu, S. N. Zhang, H. F. Song, M. Troyer, and A. A. Soluyanov, "WannierTools: An open-source software package for novel topological materials," *Comput Phys Commun*, vol. 224, 2018, doi: 10.1016/j.cpc.2017.09.033.
- [40] R. G. Parr and Y. Weitao, "Density-Functional Theory of Atoms and Molecules (International Series of Monographs on Chemistry)," *Breslow*, *R*, 1994.
- [41] J. Toda, "Density functional treatment of interactions and chemical reactions at surfaces", <a href="https://www.researchgate.net/figure/Jacobs-ladder-approach-for-the-systematic-improvement-of-DFT-functionals-according-to\_fig1\_235990497">https://www.researchgate.net/figure/Jacobs-ladder-approach-for-the-systematic-improvement-of-DFT-functionals-according-to\_fig1\_235990497</a>, 04/24, 2023
- [42] Z. H. Yang, H. Peng, J. Sun, and J. P. Perdew, "More realistic band gaps from meta-generalized gradient approximations: Only in a generalized Kohn-Sham scheme," Phys Rev B, vol. 93, no. 20, 2016, doi: 10.1103/PhysRevB.93.205205.
- [43] J. Sun, A. Ruzsinszky, and J. Perdew, "Strongly Constrained and Appropriately Normed Semilocal Density Functional," Phys Rev Lett, vol. 115, no. 3, 2015, doi: 10.1103/PhysRevLett.115.036402.
- [44] K. Momma and F. Izumi, "VESTA3 for three-dimensional visualization of crystal, volumetric and morphology data", Journal of Applied Crystallography, vol. 44, no. 6, 2011, doi: 10.1107/S0021889811038970
- [45] L. Fu and C. L. Kane, "Topological insulators with inversion symmetry," *Phys Rev B Condens Matter Mater Phys*, vol. 76, no. 4, 2007, doi: 10.1103/PhysRevB.76.045302.
- [46] L. Fu, C. L. Kane, and E. J. Mele, "Topological insulators in three dimensions," *Phys Rev Lett*, vol. 98, no. 10, 2007, doi: 10.1103/PhysRevLett.98.106803.

# Existence of Topological Phase in RbCd<sub>4</sub>As<sub>3</sub>: A First Principles Study

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**Abstract.** In this work, we report topological phase in the layered arsenide RbCd<sub>4</sub>As<sub>3</sub> using *first-principles* calculations. We find that RbCd<sub>4</sub>As<sub>3</sub>, have topological band inversion at  $\Gamma$  point, which verifies the topological nature. Also, a small spin-orbit band gap of 0.1559 eV is observed at  $\Gamma$  point. Further verification of the topological nature is carried out by calculating the  $Z_2$  topological invariants. The parity product of valance bands shows non-zero value of  $Z_2$  topological invariant. Surface density of state (SDOS) study shows existence of Dirac cone near the Fermi level. Conducting surface states near the Fermi level, as observed in SDOS, confirm the topological non-trivial nature of RbCd<sub>4</sub>As<sub>3</sub>.

#### INTRODUCTION

Topological Materials (TMs) have a broad application in Spintronics<sup>1</sup>, Quantum Computing<sup>2</sup>, Chemical Catalysis<sup>3</sup>, and Thermoelectric Materials<sup>4</sup>. The phenomena exhibited by these materials such as magnetoresistance<sup>5</sup>, chiral anomaly <sup>6</sup>, and Weyl Fermion quantum transport <sup>7</sup> are increasing their popularity amongst the research community. TMs can be divided into several categories such as Topological Semi-metals (TSM), Topological insulators (TI), Topological Crystalline Insulator (TCI) and many more. TSMs show gapless electronic states exhibiting crossing of valence and conduction bands near the Fermi level  $(E_F)^8$ . They can be categorised into several categories such as Dirac Semi-metals, Weyl semimetals, nodal line semimetals, and more<sup>9–12</sup> based on the degeneracy, co-dimension, dispersion, and origin of the band crossing.

TIs have an insulating bulk and gapless boundary states (2D) and gapless surface states (3D)<sup>13–15</sup>. Non–trivial TIs have odd number of surface Dirac cones whereas even number of cones make them trivial. The non-triviality preserve Time Reversal Symmetry (TRS) and leads to some exotic properties. Another class of TIs in which surface states are protected by crystal symmetries instead of TRS named as topological crystalline insulators (TCIs). There are different types of TCIs which exhibit mirror symmetry as in SnTe family<sup>16,17</sup> and Rotational Symmetry<sup>18</sup> as observed in α-Bi<sub>4</sub>Br<sub>4</sub><sup>19</sup>. ARPES experimental study and Density Functional Theory (DFT) analysis of NaCd<sub>4</sub>As<sub>3</sub> show that it has TCI characteristics at room temperature which converts to TI upon lowering the temperature<sup>20</sup>. This happens due to the broken mirror symmetry leading to a topological phase transition from TCI to TI<sup>20</sup>. Besides, NaCd<sub>4</sub>As<sub>3</sub> have been reported as a part of two Zintl Phases series namely, ACd<sub>4</sub>Pn<sub>3</sub> and AZn<sub>4</sub>Pn<sub>3</sub> (A = Na, K, Rb, Cs; Pn = As, P), in which 12 complex compounds have been synthesized from respective elements including layered arsenide like NaCd<sub>4</sub>As<sub>3</sub>, NaZn<sub>4</sub>As<sub>3</sub>, NaCd<sub>4</sub>As<sub>3</sub>, KCd<sub>4</sub>As<sub>3</sub>, and RbCd<sub>4</sub>As<sub>3</sub><sup>21,22</sup>. There are structural similarities found in these layered arsenide as established by X-ray Diffraction (XRD) <sup>21,22</sup>. Moreover, the stable crystal structure of RbCd<sub>4</sub>As<sub>3</sub> have been experimentally synthesized and its electronic structure calculations using the linear muffin-tin orbital (LMTO) method have been reported without considering the effect of spin orbit coupling (SOC)<sup>21</sup>. However, including spin-orbit interaction in band structure calculation can have drastic effects on the properties (topological) of a material as

observed in Bi<sub>2</sub>Se<sub>3</sub><sup>23</sup>. Even the strength of the spin-orbit interaction can be enhanced by various methods like chemical doping<sup>24</sup>, applying magnetic field<sup>25</sup>, or increasing hydro-static pressure<sup>26</sup>.

Thus, the experimental observation of topological phase transition in NaCd<sub>4</sub>As<sub>3</sub> and the similarity of structure with RbCd<sub>4</sub>As<sub>3</sub>, makes it interesting to study the electronic and topological properties of RbCd<sub>4</sub>As<sub>3</sub><sup>20–22</sup> under the effect of SOC. Hence, we have probed the topological structure of the material RbCd<sub>4</sub>As<sub>3</sub> using the *first-principle* calculations and found that RbCd<sub>4</sub>As<sub>3</sub> shows topological phase with SOC. Further the topological nature is also verified by surface states visualised in (001) plane.

#### **COMPUTATIONAL DETAILS**

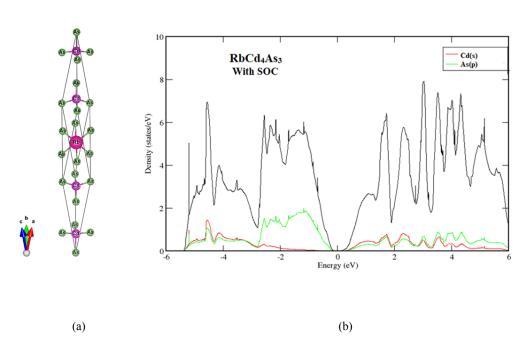
To evaluate the structural and electronic properties of RbCd<sub>4</sub>As<sub>3</sub>, we used the Density Functional Theory (DFT) calculations<sup>27,28</sup> as implemented in Vienna ab-initio simulation package (VASP)<sup>29</sup> with projector augmented wave formalism (PAW)<sup>30</sup>. To include the exchange-correlation function as in PAW formalism, we used the Generalized gradient approximation (GGA) of Perdew-Burke Ernzehrof (PBE)<sup>31,32</sup> with spin-orbit coupling. The structural relaxation of RbCd<sub>4</sub>As<sub>3</sub> is performed using the strict energy convergence criteria of 1 × 10<sup>-6</sup> eV . To calculate structural properties and the electronic band structure, the kinetic energy cut-off of 520 eV is used. For a sampling of Brillion Zone (BZ) in rhombohedral structure, a 7x7x3 size Gamma centered k-mesh is used. Fermi level is broadened with a width of 0.001 eV using Gaussian smearing. All atoms in the unit cell are relaxed with the force of 0.001 eV/A per atom. Using maximally localized Wannier Functions<sup>33</sup>, for tight-binding models to produce the band structure under effect of spin orbit coupling (SOC) constructed by Wannier90 code<sup>34</sup>. The resultant tight binding Hamiltonian is used to calculate the surfaces states of RbCd<sub>4</sub>As<sub>3</sub> using Wannier tools<sup>35</sup>.

#### **RESULTS AND DISCUSSION**

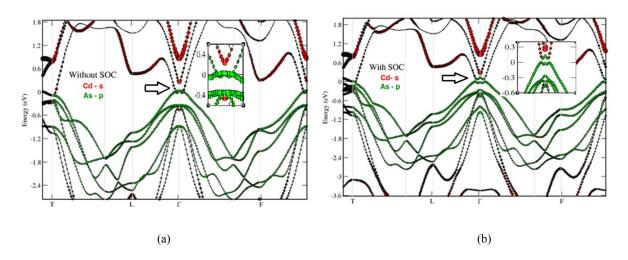
We investigate the electronic structure of the alkali metal layered arsenide RbCd<sub>4</sub>As<sub>3</sub> for topological nature. RbCd<sub>4</sub>As<sub>3</sub> is experimentally synthesized in space group  $R\overline{3}m$  (166) in the rhombohedral phase. We took the lattice parameters a (4.4752 Å) and c (36.946 Å) from the reported experimental study<sup>21</sup>. For this study, we used the primitive structure to avoid band-folding with atomic positions as shown in Fig. 1(a). To understand our system, we have plotted the projected density of states (PDOS) or atom-resolved density of states for RbCd<sub>4</sub>As<sub>3</sub> in Fig. 1(b). We observe that in the valence band the DOS majorly consists of *p-orbitals* of As near the fermi level whereas the *s-orbital* of Cd vanishes. On the contrary, in the conduction band both orbitals have similar contribution near the fermi level.

The band structure calculation with and without SOC is shown in Fig. 2. The band structure calculation is performed along high symmetry path  $\Gamma$ , T, H<sub>2</sub>, H<sub>0</sub> L, S<sub>0</sub>, S<sub>2</sub>, and F out of which  $\Gamma$ , T, L, and F are the Time reversal Invariant Momenta (TRIM) points. Under the effect of SOC, RbCd<sub>4</sub>As<sub>3</sub> shows topological band inversion at  $\Gamma$  high symmetry point. A small spin orbit band gap of 0.1559 eV is also observed at  $\Gamma$  point. The orbital contribution of Cd(s-orbital) and As(p-orbital) is observed mainly near  $E_F$  (Fig. 2) and can also be verified with the help of projected density of states (PDOS) as shown in Fig. 1(b). The spin orbit band gap can also be observed in PDOS of RbCd<sub>4</sub>As<sub>3</sub> as shown in Fig. 1(b). From Fig. 2(b) it can be verified that at  $\Gamma$  point inverted contribution of s-orbital of Cd and p-orbital of As (Fig. 2(b) inset) show topological inversion and hence non-trivial nature can be seen. No other inversion is observed

on high symmetry points which confirm the existence of single Dirac cone in  $RbCd_4As_3$  and hence its topological nature.



**FIGURE 1.** (a) Primitive Structure of RbCd<sub>4</sub>As<sub>3</sub>; (b) Projected Density of States (PDOS) of RbCd<sub>4</sub>As<sub>3</sub> with consideration of contribution from *s-orbital* of Cd and *p-orbital* of As. The Fermi level is set to 0 eV.



**FIGURE 2.** Band structures of RbCd<sub>4</sub>As<sub>3</sub> (a) without the SOC effect and (b) with SOC. Red spheres show the contribution of *s-orbital* of Cd atom and green spheres show the contribution of *p-orbital* of As atom to the bands near the Fermi level. The Fermi level is set to 0 eV.

To further investigate the topological character of RbCd<sub>4</sub>As<sub>3</sub>, we calculate the parity of the system at TRIM points. For 3D systems there are four  $Z_2$ -invariants namely ( $v_0$ :  $v_1$ ,  $v_2$ ,  $v_3$ ) whose values are governed by the following equations as suggested by Kane and Mele<sup>14,36,37</sup>:

$$(-1)^{\mathsf{v}_0} = \prod_i \delta_i \tag{1}$$

$$(-1)^{v_{i=1,2,3}} = \prod_{m_{i\neq i} \& m_{i=1}} \delta_{m_1 m_2 m_3}$$
 (2)

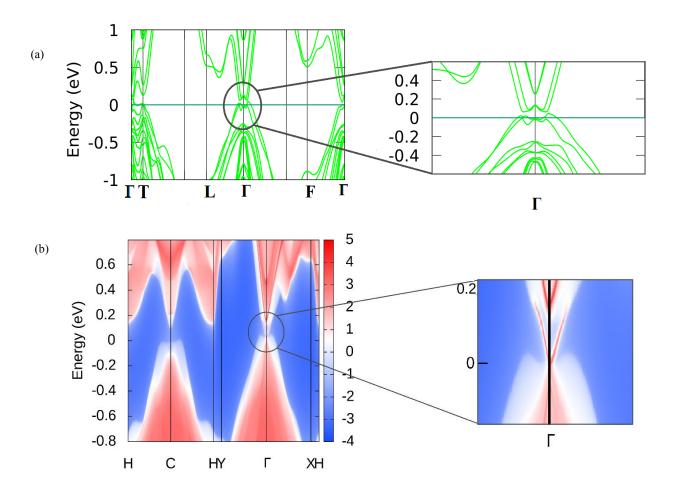
Where,  $\prod_i \delta_i$  denotes the parity products for filled valence bands at all TRIM points and the index value gives the class. These equations are applicable only for systems with inversion symmetry and Time Reversal Symmetry (TRS). There are eight TRIM points which can be calculated using the equation (3)<sup>14,36,37</sup>.

$$G_{i=m_1m_2m_3} = \frac{m_1a_1 + m_2a_2 + m_3a_3}{2} \tag{3}$$

Here,  $m_j=0$ , 1 and  $a_1$ ,  $a_2$ ,  $a_3$  are the reciprocal primitive lattice vectors. The nature or strength of the topological insulator can be determined by the value of  $v_0$  calculated using equation (1). For  $v_0=1$ , the system is a strong topological insulator and for  $v_0=0$ , it is trivial or weak in nature. The values of  $v_1$ ,  $v_2$ ,  $v_3$ , given by equation (2) are used to distinguish between a weak TI and trivial insulator. The parity for valence bands at all TRIM points for band structure calculations with spin orbit coupling is shown in table 1. It can be observed that the product of all TRIM point is (-). The value of the  $Z_2$  index  $v_0$  as calculated from equation (1) comes out to be 1. This verifies that RbCd<sub>4</sub>As<sub>3</sub> have strong topological nature.

**TABLE 1.** Parities of all the occupied bands at TRIM points of first BZ of RbCd<sub>4</sub>As<sub>3</sub> in primitive structure with spin-orbit coupling.

TRIM Points	Parity
Γ	-
3L	-
3F	-
T	+
Total	-



**FIGURE 3.** (a) Band Structure of RbCd<sub>4</sub>As<sub>3</sub> in wannier space with band gap induced at  $\Gamma$  due to spin-orbit coupling. Magnified image of the band gap induced at  $\Gamma$  point is shown. (b) Surface Density of States for (001) surface of RbCd<sub>4</sub>As<sub>3</sub> calculated with spin-orbit coupling. Formation of a single Dirac cone can be observed at  $\Gamma$  point.

Additionally, we calculate maximally localized wannier function (MLWF) from the Bloch energy bands of RbCd<sub>4</sub>As<sub>3</sub> shown in Fig. 2(b). Since, the MLWFs are independent of the basis set used to obtain the bloch states<sup>34</sup>, we can use them to calculate band structure in wannier space and verify the band structure obtained from Bloch states. The calculated band structure in wannier space can be observed in Fig. 3(a). The wannier band structure of RbCd<sub>4</sub>As<sub>3</sub> (Fig.3(a)) exhibits a spin orbit band gap at  $\Gamma$ -point and perfectly coincides with the Bloch band structure, thus verifying it (Fig.2(b)). Further, we used MLWFs to perform surface state calculations for (001) surface of RbCd<sub>4</sub>As<sub>3</sub> using the green's function approach. From our *first-principle* calculations, we derive a tight-binding model Hamiltonian to calculate the surface states. The resulting Surface Density of States (SDOS) forming a single Dirac cone at  $\Gamma$ -point is shown in Fig.3(b). This is in agreement with the spin orbit band gap observed at  $\Gamma$  point in Fig. 2(b) and Fig. 3(a). The presence of odd number of Dirac cones on the (001) surface of RbCd<sub>4</sub>As<sub>3</sub> confirms the presence of conducting surface state on (001) plane of RbCd<sub>4</sub>As<sub>3</sub>. The existence of topological band inversion and conducting surface state along with a surface Dirac cone near Fermi level shows that RbCd<sub>4</sub>As<sub>3</sub> has non-trivial topological nature. A topological insulator

can generally be good thermoelectric material. RbCd<sub>4</sub>As<sub>3</sub> is a Zintl compound and on preliminary transport calculations Zintl Compounds are suggested to be good thermoelectric materials<sup>21</sup>. Besides, RbZn<sub>4</sub>P<sub>3</sub> is also a member of this family and is proven to be a thermoelectric material<sup>4</sup>. Another member of this family is NaCd<sub>4</sub>As<sub>3</sub>, which is shown to have a favorable combination of electrical conductivity and Seebeck coefficient<sup>21</sup> along with existence of a topological phase<sup>20</sup>, indicating a strong possibility of possessing thermoelectric properties. Hence, it would be worthwhile to investigate RbCd<sub>4</sub>As<sub>3</sub> and other materials of this family for having thermoelectric properties for which our study can be used.

#### **CONCLUSION**

The topological properties of the alkali metal layered arsenide RbCd<sub>4</sub>As<sub>3</sub> have been studied based on the *first-principles* density functional theory calculations. The stable rhombohedral structure with space group 166 is considered to study the band structure of RbCd<sub>4</sub>As<sub>3</sub>. We have observed a single band inversion at  $\Gamma$ -point under the consideration of spin-orbit coupling effect and a small spin-orbit band gap of 0.1559 eV. The orbital contribution during the inversion can be attributed to *s-orbital* of Cd and *p-orbital* of As. We have also calculated the Z<sub>2</sub> topological invariants to verify the topological phase. The product of parities of all occupied bands have shown that the value of Z<sub>2</sub> index  $v_0 = 1$ . This have suggested that RbCd<sub>4</sub>As<sub>3</sub> is topologically non-trivial. The Surface density of state have also verified the existence of single Dirac cone and conducting surface state in RbCd<sub>4</sub>As<sub>3</sub>. The band inversion and surface state study of RbCd<sub>4</sub>As<sub>3</sub> have confirmed its topologically non-trivial nature. We hope that the future experimental studies will verify its topological nature as the surface state can be observed with the help of Angle Resolved Photoemission Spectroscopy (ARPES).

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#### REFERENCES

- 1. S.A. Yang, SPIN **6**, 1640003 (2016).
- 2. C. Nayak, S.H. Simon, A. Stern, M. Freedman, and S. das Sarma, Rev Mod Phys 80, 1083-1159 (2008).
- 3. C.R. Rajamathi, U. Gupta, N. Kumar, H. Yang, Y. Sun, V. Süß, C. Shekhar, M. Schmidt, H. Blumtritt, P. Werner, B. Yan, S. Parkin, C. Felser, and C.N.R. Rao, Advanced Materials **29**, 1606202 (2017).
- 4. Sangeeta, R. Kumar, and M. Singh, J Mater Sci 57, 10691–10701 (2022).
- 5. F.F. Tafti, Q.D. Gibson, S.K. Kushwaha, N. Haldolaarachchige, and R.J. Cava, Nat Phys 12, 272–277 (2016).
- 6. X. Huang, L. Zhao, Y. Long, P. Wang, D. Chen, Z. Yang, H. Liang, M. Xue, H. Weng, Z. Fang, X. Dai, and G. Chen, Phys Rev X 5, 031023 (2015).
- 7. A.A. Zyuzin and A.A. Burkov, Phys Rev B Condens Matter Mater Phys 86, 115133 (2012).
- 8. J. Li, Z. Zhang, C. Wang, H. Huang, B.L. Gu, and W. Duan, J Appl Phys 128, 191101 (2020).

- 9. H. Gao, J.W.F. Venderbos, Y. Kim, and A.M. Rappe, Annu Rev Mater Res 49, 153-183 (2019).
- S.M. Young, S. Zaheer, J.C.Y. Teo, C.L. Kane, E.J. Mele, and A.M. Rappe, Phys Rev Lett 108, 140405 (2012).
- 11. H. Weng, C. Fang, Z. Fang, B. Andrei Bernevig, and X. Dai, Phys Rev X 5, 011029 (2015).
- 12. A.A. Burkov, M.D. Hook, and L. Balents, Phys Rev B Condens Matter Mater Phys 84, 235126 (2011).
- 13. B.A. Bernevig, T.L. Hughes, and S.C. Zhang, Science (1979) 314, 1757-1761 (2006).
- 14. C.L. Kane and E.J. Mele, Phys Rev Lett 95, 146802 (2005).
- 15. M.Z. Hasan and C.L. Kane, Rev Mod Phys 82, 3045-3067 (2010).
- 16. T.H. Hsieh, H. Lin, J. Liu, W. Duan, A. Bansil, and L. Fu, Nat Commun 3, 982 (2012).
- 17. Y. Tanaka, Z. Ren, T. Sato, K. Nakayama, S. Souma, T. Takahashi, K. Segawa, and Y. Ando, Nat Phys 8, 800–803 (2012).
- 18. C. Fang and L. Fu, Sci Adv 5, eaat2374 (2019).
- 19. C.-H. Hsu, X. Zhou, Q. Ma, N. Gedik, A. Bansil, V.M. Pereira, H. Lin, L. Fu, S.-Y. Xu, and T.-R. Chang, 2D Mater. 6, 031004 (2019).
- 20. Y.Y. Wang, C. Zhong, M. Li, W.L. Zhu, W.J. Hou, W.H. Song, Q.X. Dong, Y.F. Huang, S. Zhang, Z.A. Ren, S. Wang, and G.F. Chen, Phys Rev B **102**, 115122 (2020).
- 21. H. He, C. Tyson, and S. Bobev, ChemInform 42, 8375–8383 (2011).
- 22. C. Grotz, M. Baumgartner, K.M. Freitag, F. Baumer, and T. Nilges, Inorg Chem 55, 7764-7776 (2016).
- 23. D. West, Y.Y. Sun, H. Wang, J. Bang, and S.B. Zhang, Phys Rev B 86, 121201(R) (2012).
- 24. A.B. Maghirang, Z.Q. Huang, R.A.B. Villaos, C.H. Hsu, L.Y. Feng, E. Florido, H. Lin, A. Bansil, and F.C. Chuang, NPJ 2D Mater Appl 3, 35 (2019).
- 25. J. Macy, D. Ratkovski, P.P. Balakrishnan, M. Strungaru, Y.C. Chiu, A. Flessa Savvidou, A. Moon, W. Zheng, A. Weiland, G.T. McCandless, J.Y. Chan, G.S. Kumar, M. Shatruk, A.J. Grutter, J.A. Borchers, W.D. Ratcliff, E.S. Choi, E.J.G. Santos, and L. Balicas, Appl Phys Rev **8**, 041401 (2021).
- 26. M. Singh, R. Kumar, and R.K. Bibiyan, Eur Phys J Plus 137, 633 (2022).
- 27. A.K. Rajagopal and J. Callaway, Phys Rev B, 7, 1912-1919 (1973).
- 28. W. Kohn and L.J. Sham, Physical Review 140, A1133-A1138 (1965).
- 29. G. Kresse and J. Furthmüller, Phys Rev B Condens Matter Mater Phys 54, 11169-11186 (1996).
- 30. G. Kresse and D. Joubert, Phys Rev B Condens Matter Mater Phys 59, 1758-1775 (1999).
- 31. J.P. Perdew, K. Burke, and M. Ernzerhof, Phys Rev Lett 77, 3865-3868 (1996).
- 32. J.P. Perdew, J.A. Chevary, S.H. Vosko, K.A. Jackson, M.R. Pederson, D.J. Singh, and C. Fiolhais, Phys Rev B **46**, 6671-6687 (1992).
- 33. N. Marzari and D. Vanderbilt, Phys Rev B Condens Matter Mater Phys 56, 12847-12865 (1997).
- 34. A.A. Mostofi, J.R. Yates, G. Pizzi, Y.S. Lee, I. Souza, D. Vanderbilt, and N. Marzari, Comput Phys Commun 185, 2309-2310 (2014).
- 35. Q.S. Wu, S.N. Zhang, H.F. Song, M. Troyer, and A.A. Soluyanov, Comput Phys Commun **224**, 405-416 (2018).
- 36. L. Fu and C.L. Kane, Phys Rev B Condens Matter Mater Phys 76, 045302 (2007).
- 37. L. Fu, C.L. Kane, and E.J. Mele, Phys Rev Lett 98, 106803 (2007).