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**Fourth SEMESTER**

Roll No:.....

**B.Tech. II**

Mid SEMESTER EXAMINATION

March, 2019

*MC-202, Real Analysis*

Time:  $1\frac{1}{2}$  Hours

Max. Marks: 25

*Note: Attempt all questions and assume the missing values.*

- (1) Define the *Completeness Axiom* and show that the greatest member of a set, if exists, is the sup of the set.
- (2) Define the convergence of a sequence. Prove that the sequence  $\left\{\left(1 + \frac{1}{n}\right)^n\right\}$  converges and find the limit.
- (3) Define divergent sequence with an example. If  $\{s_n\}$  and  $\{t_n\}$  are sequences of real numbers,  $\{s_n\}$  diverges to infinity and  $\{t_n\}$  is bounded, then prove that the sum  $\{s_n + t_n\}$  diverges to infinity.
- (4) Define Cauchy sequence with an example,. Show that every Cauchy sequence of real numbers is convergent.
- (5) Show that the set of all real numbers  $[0, 1]$  is uncountable.