OPTIMAL SITING AND SIZING OF DISTRIBUTED GENERATION RESOURCES IN RADIAL DISTRIBUTION SYSTEMS

A DISSERTATION

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MASTER OF TECHNOLOGY
IN
POWER SYSTEM

Submitted By

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CERTIFICATE

I hereby certify that the Project Dissertation titled "OPTIMAL SITING AND SIZING OF DISTRIBUTED GENERATION RESOURCES IN RADIAL DISTRIBUTION SYSTEMS" which is submitted by VARSHA AGGARWAL, Roll No. 2K16/PSY/19 student of M.Tech (Power System) to the Department of Electrical Engineering, Delhi Technological University, Delhi in partial fulfillment of the requirement for the award of the degree of Master of Technology, is a record of the project work carried out by the student under my supervision. To the best of my knowledge this work has not been submitted in part or full for any Degree or Diploma to this University or elsewhere.

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ABSTRACT

This thesis proposes an approach for the optimal sizing and placement of various types of Distributed Generation (DG) resources with the objective of minimizing the active power losses and improving the voltage profile improvement. Load flow studies have been carried out using BIBC and BCBV matrices. Teaching Learning Based Optimization (TLBO) and Artificial Bee Colony (ABC) algorithms have been implemented for optimal allocation of Type-1, Type-2 and Type-3 DG.

To check the effectiveness, these two algorithms have been tested on the IEEE-33 bus, 69 bus and 119 bus radial distribution systems and compared with different existing techniques like Bacterial Foraging Optimization (BFO) and particle swarm optimization (PSO) algorithms. 24-hour load variation has been considered for some cases. The simulation results show that maximum reduction of losses take place when Type-3 DGs are used.

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LIST OF ABBREVIATIONS

DG Distributed Generation

FACTS Flexible Alternating Current Transmission Systems

STATCOM Static Synchronous Compensator

SVC Static VAR Compensator

TCR Thyristor Controlled Reactor

UPFC Unified Power Flow Controller

TCSC Thyristor Controlled Series Capacitor

RDS Radial Distribution Systems

GA Genetic Algorithm

TLBO Teaching Learning Based Optimization

ABC Artificial Bee Colony

PSO Particle Swarm Optimization

DSTATCOM Distribution Static Compensator

BIBC Bus Injection to Branch Current

BCBV Branch-Current to Bus-Voltage

CHAPTER-1

INTRODUCTION AND LITERATURE REVIEW

1.1 INTRODUCTION

The main objective of power systems is to supply reliable and economical electric power to the consumers. But generally, the generating stations are situated far away from the loads. In the process of supplying electric power to these widely spread users, a power system experiences a huge amount of transmission losses and costs. About 13% of the total generated power is wasted as real power losses [1]. Real power losses are higher in the distribution systems as compared to the transmission systems as the R/X ratio is higher in distribution systems [2]. These losses have a considerable effect on the overall performance of the power system. For reducing the losses, the following methods can be adopted-:

- DG placement
- Reactive power compensation
- Feeder reconfiguration
- High voltage distribution system

1.1.1 Distributed Generation

DG stands for distributed generation or dispersed generation which involves renewable and non-renewable sources of energy scattered throughout the power system or energy sources that are being installed near the load centers [3]. They are either used for fulfilling load requirements or to minimize losses and their size may vary from few KW to about 10 MW. Installation of DGs may offer a helpful alternative to a traditional system for different applications. It provides cleaner energy with more efficiency. Integration of DGs in the distribution system adds several operational complexities like power quality issues, voltage fluctuations, protection co-ordinations etc[4].

1.1.2 Types of DGs

On the basis of the type of energy supplied DGs can be classified into four types:-

- Type 1 This type of DG delivers active power only e.g. photovoltaic arrays, fuel cells etc. They are integrated into the system with the help of converters.
- Type 2 This type of DG delivers reactive power only e.g. capacitors, SVCs, STATCOMs.
- Type 3 This type of DG delivers both active and reactive power e.g. synchronous generators.
- Type 4 This type of DG delivers active power but consumes reactive power e.g. induction generators.

1.1.3 Benefits of DG integration in distribution systems

Power Loss Minimization

The reduction in active power losses remains a major concern for the utility because it reflects the efficiency of the system. This can be achieved with the help of DGs. The DG units are generally installed near the load points. This reduces real power losses.

• Improvement In Voltage Profile

As the system operator is required to maintain the system voltage profile within a specified range, by injecting active and reactive power into the system this can be improved. Voltage profile gets significantly affected by number and size of DGs.

• Environmental benefits

Most of the conventional energy generation methods release greenhouse gases like sulphur dioxide, carbon dioxide and nitrogen oxide. By increasing the use of renewable energy based DGs, this emission can be reduced.

The main reason for the escalating uses of DGs can be summarized as given below [5]-:

- 1. DG units are generally installed near loads. This reduces transmission and distribution losses and operational costs.
- 2. It is easier to find locations for installation of generators of small ratings as compared to those with larger ratings.
- 3. Due to a reduction in transmission and distribution losses, efficiency is improved.
- 4. Setting up time for DG is very small.

- 5. It offers various other benefits like improving voltage fluctuations, improving power quality etc.
- 6. It presents a flexible combination of various resources (like solar power) that are available locally.
- 7. DG technology is more environment-friendly as compared to the traditional system.

To improve system performance, FACTS devices are also installed along with DGs supplying active power. This is because node voltage decreases if the load is at a distant location from the supply point. So, to maintain this voltage, sufficient reactive power is needed. For this reactive compensation is required [6]. Some FACTS devices that are used for this purpose are STATCOM,SVC,TCR,UPFC etc. These FACTS devices have the ability to increase the reliability of the system. Some of its advantages are lower harmonic distortion, better voltage profile, immune to resonance etc. However, these should be placed optimally or else instead of improving the performance, they may deteriorate it. A lot of research work is going on for siting and sizing of these devices.

1.2 OBJECTIVE OF THE WORK

The main focus of the work is to find out suitable size and location of the DGs for different types. This work has been carried out using two techniques. The first technique is using TLBO and the second is the ABC based optimization. The analysis is done on multi-type DGs i.e. for Type-1, Type-2 and Type-3 DGs. Optimal allocation of all three types of DGs is tested on three different radial distribution systems— the IEEE 33-bus, 69-bus, and 118 bus systems. 24-hour load variation has also been considered for some cases.

1.3 LITERATURE REVIEW

1.3.1 Load flow Technique

Load flow analysis is a study of the flow of power in a system. It is an important area to be focussed as it provides an absolute link between the distribution system and consumers. Load flow analysis is different for distribution systems as compared to transmission systems. Various researchers have proposed several methods for this.

In [7], Newton-based power flow method was proposed but this method requires large memory requirement. In [8], a fast decoupled load flow method was proposed for unbalanced radial distribution networks. This method takes less memory as compared to Newton's method but its convergence is slow for distribution systems. In [9], a modification over fast decoupled load flow method was proposed. In [10], a compensation based power flow solution was developed for radial and weakly meshed networks. This method proved to be more efficient and robust as compared to Newton Raphson method. But this method takes more computational time as compared to the Newton's and the Fast Decoupled methods.

In [11], a new method for load flow was reported that uses the topological structure of the system. Since this method does not involve matrix inversion, it takes very less computational time as compared to other methods. This method is also free from initial assumptions so there is no chance of divergence that may happen with the Newton Raphson algorithm if initial assumptions are wrong. This method is valid for radial distribution networks as well as weakly meshed networks.

1.3.2 DG placement

Various researchers have implemented different algorithms for optimal placement of DGs. Both analytical and heuristic methods have been used for this. In [12], an analytical method was developed for optimal siting and sizing of DGs for a different type of static load but there was no information of the load profile. In [13], another analytical method was proposed for finding out the optimal sites and size of DGs in both radial and meshed type networks involving the use of admittance matrix due to which it takes more computational time. In [14], an analytical method using the theory of loss sensitivity factor based on equivalent current injection was developed that

proved to be a more robust technique. This method works without computing the admittance matrix and provided the comparable result to classical grid search algorithms in less time.

Several techniques other than analytical ones have been suggested for optimal placement of DGs. In [15], genetic algorithm was implemented for optimal siting and sizing of DGs in RDS for active power loss reduction by placing DGs strategically. This algorithm was tested on the IEEE 33-bus system. In [16], a new method named Hereford Ranch Algorithm was developed for further improvement in GA by means of selective breeding in choosing parents for the genetic string. This improved the convergence time and prevented premature convergence. In [17], PSO based planning of distributed generation was done for which a multi-objective function was formulated for power loss minimization for curtailing the cost of power loss and improving the annual energy savings. The concept of 'weight factors' was used for obtaining the best proportion of this cost. In [18], Cuckoo algorithm was implemented for voltage profile improvement and reduction in power losses. The main criterion used was voltage indices to minimize deviations in voltage from the target value. In [19], a new metaheuristic technique named ABC algorithm was implemented in radial distribution systems for determining the DG size, power factor and location of DG in order to minimize the power losses. In [20], TLBO based method was implemented for finding the optimal site, size and number of DGs in order to minimize power losses and improve the voltage profile. The results were compared with three techniques - GA, PSO and Cuckoo Search Algorithm and proved to be more effective in terms of percentage power loss reduction. In [21], a hybrid method of Fuzzy and ABC algorithm was proposed for the placement of DGs with the objective of minimizing power losses and operational costs. This method was also used to find out the suitable number, size and location of DGs, keeping voltage deviation as constraints.

In [22], Tabu Search algorithm was implemented for optimal siting and sizing of shunt capacitors in RDS to minimize investment cost and energy losses. In this approach, sensitivity analysis concept has been used to select those nodes which have maximum impact on the real power losses. In [23], Genetic Algorithm (GA) based optimal sitting and sizing of capacitors has been suggested considering the additional constraint of harmonic distortion, when nonlinear loads are present in the network. Particle swarm optimization (PSO) has been used in [24] for the placement of capacitors considering harmonic distortion limits with varying load. In [25], modified artificial bee colony

(MABC) algorithm has been used for the placement of capacitors for maximum cost savings and loss minimization.

Advancement in power-electronics has paved the way for many FACTS devices as controllable reactive power sources. These static devices provide better transient stability, small signal stability, power loss reduction and voltage profile than a conventional capacitor.

In [26], PSO was implemented for the optimal placement of STATCOM in RDS. The results were validated on a 45-bus system considering voltage deviation constraint at each bus. In [27], DSTATCOM was allocated using Bat Algorithm (BA) on the basis of voltage stability index (VSI). In [28], Index vector method has been used for the optimal allocation of DSTATCOM for several load models and load growth.

In [29], Bacterial Foraging Algorithm (BFA) has been implemented for evaluating suitable locations and sizes of multiple DGs and DSTATCOMs taking Loss Sensitivity Factor as a predetermining factor. In [30], SVC along with DG has been implemented using differential search algorithm. In this study, two penetration levels for DG have been considered and cost analysis has been done along with power loss reduction and voltage profile improvement.

CHAPTER-2

PROBLEM FORMULATION

2.1 OBJECTIVE FUNCTION

The problem is to find out suitable size and site for DGs so that active power losses can be minimized subject to inequality constraints. So our main objective function is power loss minimization. The proposed method uses bus injection to branch current (BIBC) matrix and branch-current to bus-voltage (BCBV) matrix for load flow. These matrices are developed on the basis of the topological structure of the distribution system [31]. The development of these matrices is explained in chapter 3.

2.1.1 Active power loss reduction

For real power loss calculation, the current injected at each node is computed which is specified by given equation 2.1

$$\mathbf{I_i} = ((P_i + jQ_i)^* / V_i^*) \tag{2.1}$$

where i varies from 1 to n, n is the no. of buses, $\mathbf{I_i}$ is the corresponding current injection, P_i and Q_i are the corresponding real and reactive powers injected at each node and $\mathbf{V_i}$ is the node voltage. Our main objective is to curtail active power losses represented by equation 2.2.

Objective Function =
$$min(P_{loss})$$
 (2.2)

$$P_{loss} = \sum_{i,j=1}^{n} I_i^2 * r_j \tag{2.3}$$

In this equation 'i', 'j' and 'n' represents bus number , branch number and total number of buses.

2.1.2 Constraints

• Voltage constraints

The voltage magnitude at each node should be in the specified range

$$V_{min} \leq V_i \leq V_{max}$$

Where V_{max} and V_{min} are the maximum and minimum value of node voltage magnitude in p.u. i.e. 1.05 p.u. and 0.9 p.u respectively.

• ACTIVE AND REACTIVE POWER SOURCE CAPACITY LIMITS

The active and reactive powers injected by the sources to be installed must be within their specified rating limits i.e.

$$P_{min} \leq P_i \leq P_{max}$$

$$Q_{min} \leq Q_i \leq Q_{max}$$

Where P_{max} and P_{min} are the maximum and minimum values of active power source ratings i.e. 3 MW (5 MW for 119 bus system) and zero respectively. Similarly, Q_{max} and Q_{min} are the maximum and minimum values of reactive power source ratings i.e. 3MVAr (5 MVAr for 119 bus system) and zero respectively.

CHAPTER-3

LOAD FLOW STUDIES

3.1 LOAD FLOW TECHNIQUE

Load flow analysis is basically an study of the flow of active and reactive powers in a power system. Its solution presents knowledge about the voltage profile, phase angles, active and reactive power flows. Conventional methods used for load flow are Gauss Siedel, Newton-Raphson and fast-decoupled method etc[31]. But these methods are not suitable for distribution systems due to various reasons like large number of branches and nodes, radial and weakly meshed networks, extensive ranges of resistance and reactance values. For these methods, it would require a matrix of large dimension (according to the number of buses and branches), a long computational time and more memory requirements. To eradicate all these drawbacks a novel method has been developed based on the topology of distribution system[11]. The only input of this method is the bus-branch related data. By using this data, two matrices named bus injection to branch current (BIBC) and branch current to bus voltage (BCBV) are developed. The development of these matrices is explained later.

This load flow technique is mainly based on these two matrices BIBC and BCBV. For explaining its development a sample of the radial distribution network is shown in fig 3.1.

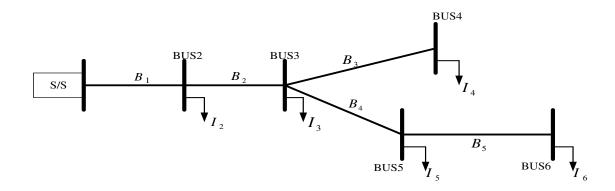


Fig. 3.1 A typical distribution network

The power injections at every bus can be converted into respective current injections which is represented in equation 3.1 and by using Kirchhoff's Current Law at each node branch current can be obtained which is shown in equations 3.2 to 3.6.

$$\mathbf{I}_{i} = ((\boldsymbol{P}_{i} + \boldsymbol{j}\boldsymbol{Q}_{i})/V_{i})^{*} \tag{3.1}$$

$$B_1 = I_2 + I_3 + I_4 + I_5 + I_6 (3.2)$$

$$B_2 = I_3 + I_4 + I_5 + I_6 \tag{3.3}$$

$$B_3 = I_4 \tag{3.4}$$

$$B_4 = I_5 + I_6 \tag{3.5}$$

$$B_5 = I_6 \tag{3.6}$$

From equations 3.2 to 3.6, the relation between bus current injection and branch current can be represented in matrix form which is given by equation 3.7.

$$\begin{bmatrix}
B_1 \\
B_2 \\
B_3 \\
B_4 \\
B_5
\end{bmatrix} = \begin{bmatrix}
1 & 1 & 1 & 1 & 1 \\
0 & 1 & 1 & 1 & 1 \\
0 & 0 & 1 & 0 & 0 \\
0 & 0 & 0 & 1 & 1 \\
0 & 0 & 0 & 0 & 1
\end{bmatrix} \begin{bmatrix}
I_2 \\
I_3 \\
I_4 \\
I_5 \\
I_6
\end{bmatrix}$$
(3.7)

Equation 3.7 in generalised form can be represented by equation 3.8.

$$[B] = [BIBC][I] \tag{3.8}$$

The relationships between branch currents and bus voltages can be characterized by using KVL and is represented in equation 3.9-3.13.

$$V_2 = V_1 - B_1 Z_{12} \tag{3.9}$$

$$V_3 = V_2 - B_2 Z_{23} \tag{3.10}$$

$$V_4 = V_3 - B_3 Z_{34} \tag{3.11}$$

$$V_5 = V_3 - B_4 Z_{35} \tag{3.12}$$

$$V_6 = V_5 - B_5 Z_{56} \tag{3.13}$$

From equations 3.9, 3.10 and 3.11 we can write V_4 as per equation 3.14

$$V_4 = V_1 - B_1 Z_{12} - B_2 Z_{23} - B_3 Z_{34}$$
 (3.14)

$$V_5 = V_1 - B_1 Z_{12} - B_2 Z_{23} - B_4 Z_{35}$$
 (3.15)

$$V_6 = V_1 - B_1 Z_{12} - B_2 Z_{23} - B_4 Z_{35} - B_5 Z_{56}$$
 (3.16)

Equation 3.17 in generalized form can be represented as

$$[\Delta V] = [BCBV][B] \tag{3.18}$$

From 3.8,

$$[\Delta V] = [BCBV][BIBC][I] \tag{3.19}$$

$$[DLF] = [BCBV][BIBC] \tag{3.20}$$

$$[\Delta V] = [DLF][I] \tag{3.21}$$

The solution of load flow can be obtained by solving equations (3.22),(3.23) and (3.24) iteratively.

$$I_i^k = \left((P_i + jQ_i) / V_i^k \right)^* \tag{3.22}$$

$$\left[\Delta V^{k+1}\right] = [DLF][I^k] \tag{3.23}$$

$$[V^{k+1}] = [V^0] + [\Delta V^{k+1}]$$
 (3.24)

3.2 MATRIX DEVELOPMENT ALGORITHM

3.2.1 BIBC Matrix Development

1. For BIBC matrix, a null matrix of size m×n is initialized, where m is the number of branches and n is number of buses. The bus-branch data is read.

- 2. If a branch (B_z) is connected between bus x and bus y then the data of the x^{th} bus column is copied to the y^{th} bus column in the BIBC matrix and +1 is placed in the z^{th} row and y^{th} column.
- 3. The same procedure for each branch section is repeated.
- 4. A matrix of row from 1 to m and column from 2 to n is selected. This gives the BIBC matrix of size m×(n-1).

3.2.2 BCBV Matrix Development

- 1. For BCBV matrix, a null matrix of size n×m is initialized, where m is the number of branches and n is number of the buses. Bus-branch data is read.
- 2. If a branch (B_z) is connected between bus x and bus y then the data of the x^{th} bus row is copied to the y^{th} bus row in the BIBC matrix and Z_{xy} is placed in the y^{th} row and z^{th} column.
- 3. The same procedure is repeated for each branch section.
- 4. A matrix of column from 1 to m and row from 2 to n is selected. This will give BCBV matrix of size (n-1)×m.

3.2.3 Steps of the algorithm

- 1. Read bus-branch data.
- 2. Develop BIBC matrix.
- 3. Develop BCBV matrix.
- 4. Calculate DLF matrix as per equation 3.20.
- 5. Find out ΔV as per equation 3.21.
- 6. Initialize k=1.
- 7. Update voltages by using equations 3.22, 3.23 and 3.24.
- 8. Set k=k+1.
- 9. If $|V^{k+1}| |V^k| > 10^{-6}$ go to step 7 otherwise go to step 10.
- 10. Find other parameters like branch currents, active power losses and reactive power losses.

3.3 TEST RESULTS

The following method has been analyzed on the different bus system. The result has been summarized in table 3.1

TABLE 3.1: Load Flow Results of Different RDS

| Bus-System | Active Power Loss | Min voltage (p.u.) |
|----------------|-------------------|--------------------|
| | (kW) | |
| 33 Bus-System | 202.677 | 0.91309 |
| 69 Bus-system | 224.995 | 0.90918 |
| 119 Bus-System | 1298.092 | 0.86889 |

CHAPTER-4

OPTIMAL SITING AND SIZING OF DG USING TLBO

4.1 INTRODUCTION

TLBO optimization technique is based on the concept of the teaching and learning process. This technique was proposed by V. Rao in 2011. This algorithm reflects the effect of the teacher on the learner's output (knowledge). In this algorithm, a group of students is treated as the population and different subjects are treated as different variables [32]. The fitness value of the objective function is considered as the knowledge of the student. As the teacher is symbolized as most knowledgeable and most experienced person, that's why the best solution is taken as the teacher. The students learn from two ways. The first is through the teacher which is known as 'Teacher Phase' and the second is via interaction between different learners which is known as 'Learner Phase'.

4.2 STEPS OF THE ALGORITHM

The steps of the given algorithm can be explained as follows -:

4.2.1. Initialization Phase

Randomly generate initial population by using equation 4.1.

$$X0 = X_{LOW} + (X_{UP} - X_{LOW}) * rand(NUMPOP, D)$$
 (4.1)

where X_{LOW} and X_{UP} are the minimum and maximum value of the variable used, NUMPOP is population size (number of students) and D is number of design variables (subjects).

Calculate the value of the fitness function by using the fitness function evaluation equation specific for a defined problem.

4.2.2 Teacher Phase

The best solution of the randomly initialized matrix is treated as the teacher and the mean of the learner's knowledge is shifted towards the teacher to improve their knowledge (outcome). The equation representing the teacher phase is given by equation 4.2.

$$X_{new}(i) = X0(i) + rand \times (X_{teacher} - TF * Mean)$$
(4.2)

where the Mean vector is the mean of the learners in the class for each variable (subject) which is computed during every iteration. $X_{teacher}$ is the best solution obtained so far and TF is the teaching factor which affects the shifting of the learner's result towards the teacher outcome or best solution. Its value is either 1 or 2 which is decided randomly in the algorithm and is given by equation 4.3.

$$TF = round(1 + rand) \tag{4.3}$$

After this, the fitness value of each X_{new} vector is calculated and compared correspondingly with the outcome of vector X0. If the result of the new vector (X_{new}) is better than the previous vector (X0), then X0 is updated.

4.2.3 Learner Phase

In this phase, the learners learn via each other. In the learner phase, different learners interact randomly with each other and improve their knowledge. For a given learner (i) a second learner (h) is selected randomly out of the given population or number of students such that $i\neq h$ and then the vector X_{new} is modified by using the equations.

$$X_{new}(i) = X0(i) + rand * (X0(i) - X0(h))$$
 (4.4)

The above equation is valid if the fitness of vector X0(i) is better than X0(h) otherwise learner follows equation 4.5.

$$X_{new}(i) = X0(i) + rand * (X0(h) - X0(i))$$
 (4.5)

4.2.4 Termination Phase

After termination criterion (maximum no. of iteration), the algorithm stops executing and presents the best solution.

The described algorithm has been applied on the problem described in chapter 2 and the results are summarized below.

4.2.5 Parameters Used

Population size : 200 Maximum No. of Iterations : 500

TF : [1,2]

4.3 Flow Chart of TLBO

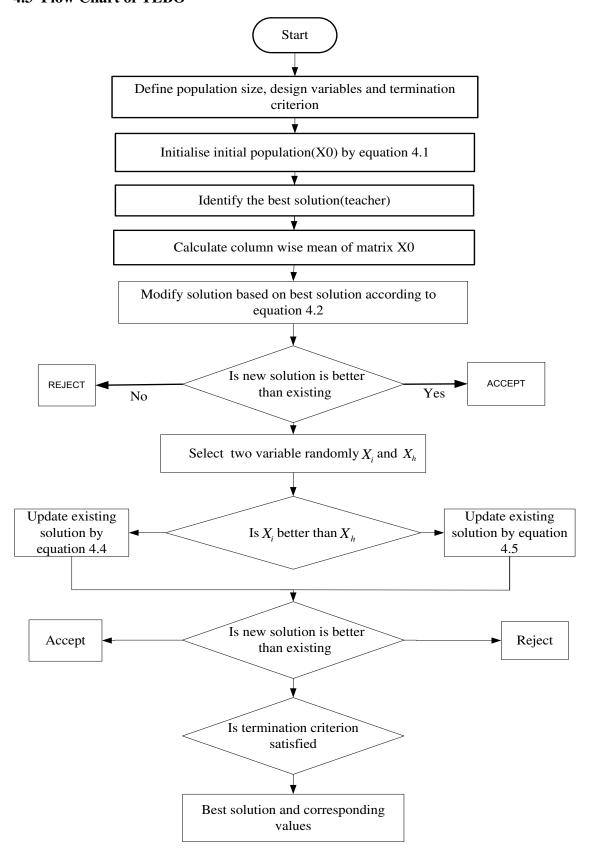


Fig. 4.1 Flow chart of TLBO method

4.4 OPTIMAL LOCATION FOR 33 BUS RADIAL DISTRIBUTION SYSTEM

IEEE 33 RDS is shown in figure [29]. It comprises of 33 buses and 32 branches. Out of the 33 buses, the first bus is the slack bus and rest 32 buses are available for installing different types of DGs. The data for this system has been taken from [33]. Selected base values are 12.66 kV and 100 MVA.

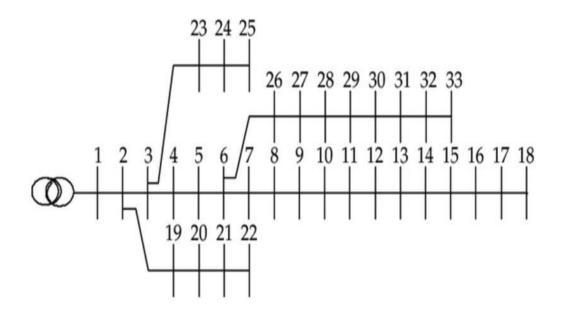


Fig. 4.2. Schematic diagram of 33 bus RDS [29]

Performance of 33 bus system without any DG (base case)

Active power load : 3715 kW

Reactive power load : 2300 kVAr

Total real power loss : 202.677 kW

Minimum voltage : 0.9131 p.u

4.4.1 Placement of Type-1 DGs in 33 bus RDS

TABLE 4.1: Allocation of Type-1 DG in 33 bus RDS by TLBO algorithm

| No. of DG | Active Power Loss (kW) | Power Loss Reduction (%) | Location (Bus no) | Size (MW) |
|-----------|------------------------|-----------------------------|-------------------|--------------|
| 0 | 202.677 | - | - | - |
| 1 | 103.966 | 48.70% | 6 | 2.575 |
| 2 | 85.910 | 57.61% | 13 | 0.846 |
| | | | 30 | 1.158 |
| | | | 14 | 0.753 |
| 3 | 71.457 | 64.74% | 24 | 1.099 |
| | | | 30 | 1.071 |
| | | | 7 | 0.9162 |
| 4 | 65.935 | 67.47% | 14 | 0.585 |
| 4 | 03.933 | 07.4770 | 24 | 0.980 |
| | | | 31 | 0.708 |
| | | | 7 | 0.908 |
| | | | 14 | 0.585 |
| 5 | 64.885 | 67.99% | 21 | 0.277 |
| | | | 24 | 0.970 |
| | | | 31 | 0.708 |

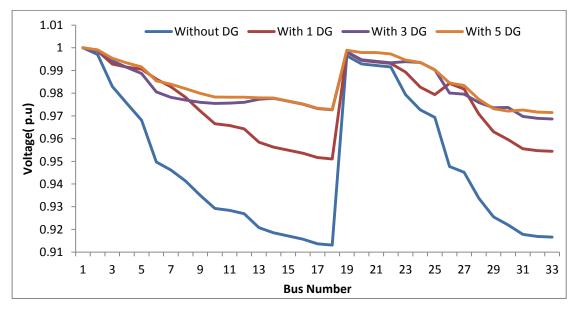


Fig. 4.3. Voltage profile with and without placing Type-1 DGs in 33 bus RDS by using TLBO algorithm

4.4.2 Placement of Type-2 DGs (DSTATCOM) in 33 bus RDS

TABLE 4.2: Allocation of Type-2 DG in 33 bus RDS by TLBO algorithm

| No. of DSTATCOM | Active Power Loss (kW) | Power Loss Reduction (%) | Location (bus no.) | Size (MVAr) |
|--------------------|---------------------------|-----------------------------|---------------------------|---|
| 0 | 202.677 | - | - | - |
| 1 | 143.602 | 29.15 | 30 | 1.253 |
| 2 | 135.753 | 33.02 | 12 30 | 0.469 1.058 |
| 3 | 132.173 | 34.78 | 13 24 30 | 0.379 0.544 1.037 |
| 4 | 130.688 | 35.51 | 7 14 24 30 | 0.442 0.276 0.483 0.904 |
| 5 | 130.315 | 35.70 | 7 14 24 30 32 | 0.442 0.276 0.483 0.709 0.194 |

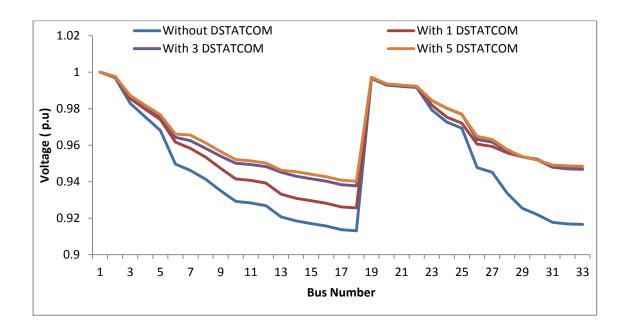


Fig. 4.4. Voltage profile with and without placing Type-2 DG in 33 bus RDS by using TLBO algorithm

4.4.3 Placement of Type-3 DGs in 33 bus RDS

TABLE 4.3: Allocation of Type-3 DG in 33 bus RDS by TLBO algorithm

| No. of DG | Real Power Loss (kW) | Power Loss Reduction | DG size | | Location (Bus No.) |
|--------------|-------------------------|-------------------------|---------|--------|---------------------|
| | Loss (RW) | (%) | (MW) | (MVAr) | (Du s 110.) |
| 0 | 202.677 | - | - | - | - |
| 1 | 61.363 | 69.72 | 2.545 | 1.750 | 6 |
| 2 | 28.492 | 85.94 | 0.839 | 0.396 | 13 |
| | | | 1.140 | 1.066 | 30 |
| | | | 0.747 | 0.350 | 14 |
| 3 | 11.630 | 94.26 | 1.078 | 0.521 | 24 |
| | | | 1.048 | 1.021 | 30 |
| | | | 0.788 | 0.377 | 7 |
| 4 | 6.427 | 96.83 | 0.586 | 0.272 | 14 |
| | 0.127 | 70.03 | 0.964 | 0.467 | 24 |
| | | | 0.788 | 0.896 | 30 |
| | | | 0.831 | 0.398 | 7 |
| | | | 0.586 | 0.272 | 14 |
| 5 | 5.078 | 97.49 | 0.782 | 0.378 | 25 |
| | | | 0.404 | 0.701 | 30 |
| | | | 0.383 | 0.193 | 32 |

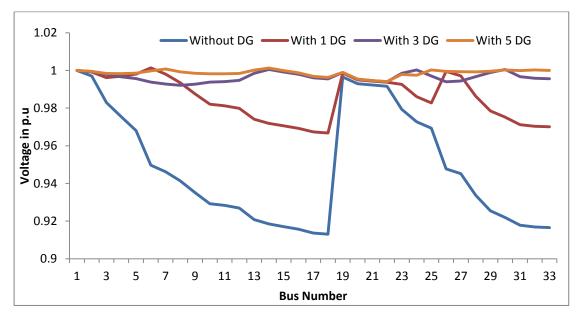


Fig. 4.5. Voltage profile with and without placing Type-3 DG in 33 bus RDS by using TLBO algorithm

4.5 OPTIMAL LOCATION FOR 69 BUS RADIAL DISTRIBUTION SYSTEM

IEEE 69 radial bus distribution system shown in figure [34]. It comprises of 69 buses and 68 branches. Out of the 69 buses, the first bus is the slack bus and rest 68 buses are available for installing different types of DGs. The data for this system has been taken from [35]. Selected base value are 12.66 kV and 100 MVA.

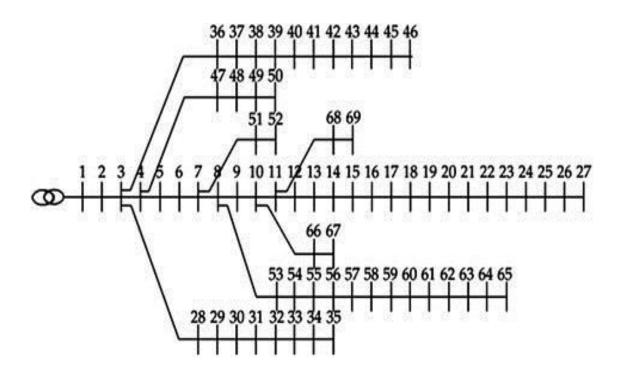


Fig.4.6. The schematic diagram of 69 radial bus distribution system

Performance of 69 bus system without placing DG

Active power load : 3802.19 kW

Reactive power load : 2694.6 kVAr

Total real power loss : 224.995 kW

Minimum voltage : 0.90919 p.u

4.5.1 Placement of Type-1 DG in 69 bus RDS

TABLE 4.4: Allocation of Type-1 DG in 69 bus RDS by TLBO algorithm

| No. Of DG | Active Power Loss (kW) | Power Loss Reduction (%) | Location (bus no.) | Size (MW) |
|-----------|------------------------|-----------------------------|----------------------------|---|
| 0 | 224.995 | - | - | - |
| 1 | 83.223 | 63.011 | 61 | 1.873 |
| 2 | 71.675 | 68.144 | 17 61 | 0.531 1.781 |
| 3 | 69.427 | 69.143 | 11 18 61 | 0.527 0.380 1.719 |
| 4 | 67.917 | 69.814 | 11 18 50 61 | 0.526 0.380 0.718 1.719 |
| 5 | 67.373 | 70.056 | 11 18 50 61 64 | 0.526 0.380 0.718 1.428 0.289 |

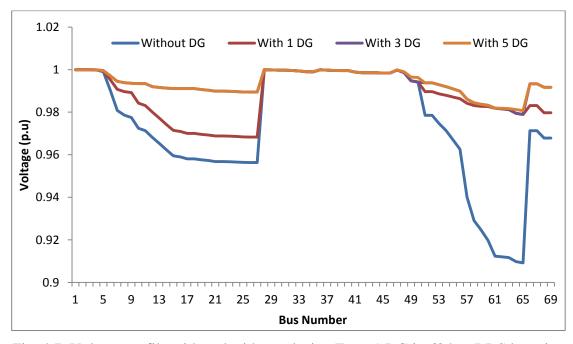


Fig. 4.7. Voltage profile with and without placing Type-1 DG in 69 bus RDS by using TLBO algorithm

4.5.2 Placement of Type-2 DG (DSTATCOM) in 69 bus RDS

TABLE 4.5: Allocation of Type-2 DG in 69 bus RDS by TLBO algorithm

| No. Of | Active Power Loss | Power Loss | Location | Size |
|----------|-------------------|---------------|-----------|--------|
| DSTATCOM | (kW) | Reduction (%) | (bus no.) | (MVAr) |
| 0 | 224.995 | - | - | - |
| 1 | 152.039 | 32.42 | 61 | 1.329 |
| 2 | 146.439 | 34.91 | 17 | 0.361 |
| | | | 61 | 1.275 |
| 3 | 145.114 | 35.50 | 11 | 0.413 |
| | | | 21 | 0.231 |
| | | | 61 | 1.232 |
| 4 | 144.332 | 35.85 | 11 | 0.413 |
| | | | 21 | 0.231 |
| | | | 50 | 0.517 |
| | | | 61 | 1.232 |
| 5 | 143.996 | 36.00 | 11 | 0.415 |
| | | | 18 | 0.232 |
| | | | 50 | 0.509 |
| | | | 61 | 1.031 |
| | | | 64 | 0.200 |

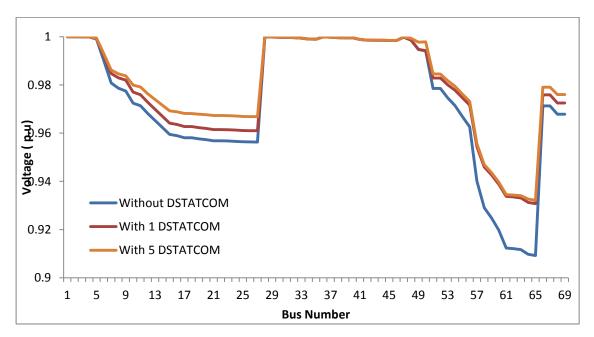


Fig. 4.8. Voltage profile with and without placing Type-2 DG in 69 bus RDS by using TLBO algorithm

4.5.3 Placement of Type-3 DG in 69 bus RDS

TABLE 4.6: Allocation of Type-3 DG in 69 bus RDS by TLBO algorithm

| No. Of DG | Real Power Loss (kW) | Power Loss Reduction (%) | Optim (MW) | al DG Size (MVAr) | Location |
|--------------|-------------------------|--------------------------------|---|---|----------------------------|
| 0 | 224.995 | - (70) | - | - | - |
| 1 | 23.171 | 89.702 | 1.828 | 1.301 | 61 |
| 2 | 7.204 | 96.798 | 0.522 1.735 | 0.353 1.238 | 17 61 |
| 3 | 4.268 | 98.103 | 0.494 0.379 1.674 | 0.354 0.251 1.195 | 11 18 61 |
| 4 | 1.997 | 99.112 | 0.493 0.379 0.718 1.674 | 0.353 0.252 0.513 1.195 | 11 17 50 61 |
| 5 | 1.633 | 99.274 | 0.388 0.312 0.718 0.279 1.647 | 0.273 0.207 0.512 0.201 1.175 | 12 21 50 53 61 |

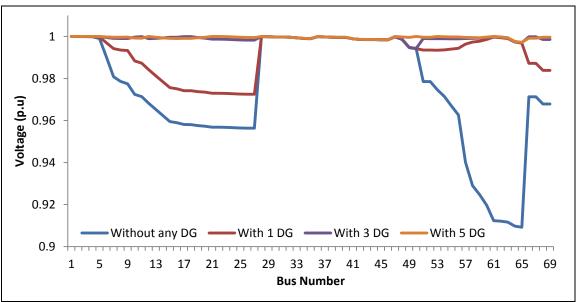


Fig. 4.9. Voltage profile with and without placing Type-3 DG in 69 bus RDS by using TLBO algorithm

4.6 OPTIMAL LOCATION FOR 119 BUS RADIAL DISTRIBUTION SYSTEM

IEEE 119 radial bus distribution system shown in figure [29]comprises 119 buses and 118 branches. Out of 119 buses first bus is slack bus and rest 118 buses are available for installing different types of DG. The data for this system has been taken from [36]. Selected base values are 11 kV and 100 MVA.

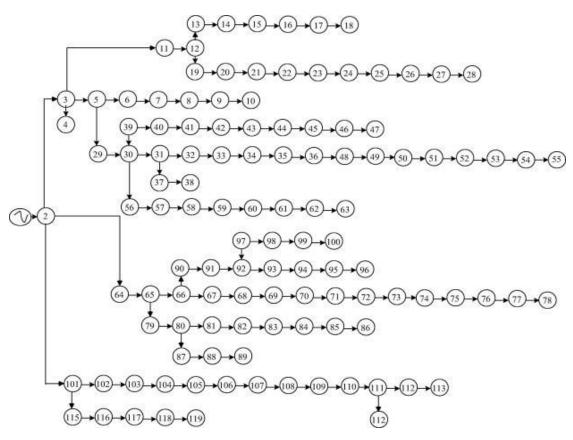


Fig. 4.10. The schematic diagram of 119 bus radial distribution system

Performance of 119 bus system without placing DG

Active power load : 22.70972 MW

Reactive power load : 17.0410 MVAr

Total real power loss : 1298.092 kW

Minimum voltage : 0.86889 p.u.

4.6.1 Placement of Type-1 DG in 119 bus RDS

TABLE 4.7: Allocation of Type-1 DG in 119 bus RDS by TLBO algorithm

| No. of DG | Active Power Loss | Power Loss | Location | Size |
|-----------|-------------------|---------------|-----------|-------|
| | (kW) | Reduction (%) | (bus no.) | (MW) |
| 0 | 1298.092 | - | - | - |
| 1 | 1016.758 | 21.67 | 72 | 2.978 |
| 2 | 805.249 | 37.97 | 72 | 2.978 |
| | | | 110 | 3.119 |
| | | | 51 | 2.883 |
| 3 | 667.294 | 48.59 | 72 | 2.978 |
| | | | 110 | 3.119 |
| | | | 51 | 2.883 |
| 4 | 616.154 | 52.53 | 73 | 2.606 |
| 4 | 010.134 | 32.33 | 97 | 1.820 |
| | | | 110 | 3.119 |
| | | | 51 | 2.883 |
| | | | 73 | 2.533 |
| 5 | 574.652 | 55.73 | 81 | 2.094 |
| | | | 97 | 1.663 |
| | | | 110 | 3.119 |

1.01 0.99 0.97 **Noltage (p.**0.95 0.93 0.89 0.87 ─With 3 DG — Without DG --With 1 DG -With 5 DG 0.85 19 28 37 10 64 73 91 100 109 **Bus Number**

Fig. 4.11. Voltage profile with and without placing Type-1 DG in 119 bus RDS using TLBO algorithm

4.6.2 Placement of Type-2 DG (DSTATCOM) in 119 bus RDS

TABLE 4.8: Allocation of Type-2 DG (DSTATCOM) in 119 bus RDS by TLBO algorithm

| No. of | Real Power Loss | Reduction in Power | Location | Size |
|--------|-----------------|--------------------|----------|--------|
| DG | with DSTATCOM | loss (%) | (bus no) | (MVAr) |
| | (kW) | | | |
| 0 | 1298.092 | - | - | - |
| 1 | 1153.301 | 11.154 | 111 | 2.333 |
| 2 | 1027.750 | | 72 | 1.956 |
| 2 | 1027.730 | 20.83 | 111 | 2.333 |
| | | | 51 | 2.610 |
| 3 | 913.060 | 29.66 | 72 | 1.956 |
| | | | 111 | 2.333 |
| | | | 51 | 2.610 |
| 4 | 882.163 | 32.04 | 73 | 1.780 |
| | 002.103 | 32.04 | 81 | 1.794 |
| | | | 111 | 2.333 |
| | | | 51 | 2.610 |
| | | | 75 | 1.538 |
| 5 | 861.526 | 33.63 | 81 | 1.672 |
| | | | 97 | 1.138 |
| | | | 111 | 2.333 |

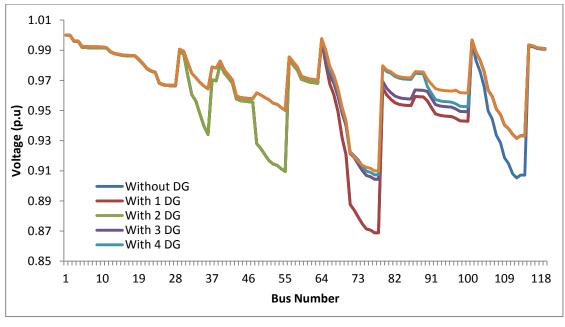


Fig. 4.12. Voltage profile with and without placing Type-2 DG in 119 bus RDS by using TLBO algorithm

4.6.3 Placement of Type-3 DG in 119 bus RDS

TABLE 4.9: Allocation of Type-3 DG in 119 bus RDS by TLBO algorithm

| No. of DG | Real Power | Power loss | Optimal | DG size | Location | Optimal |
|-----------|------------|------------|---------|---------|-----------|---------|
| | Loss(kW) | Reduction | | | (bus no.) | Power |
| | | (%) | MW | MVAr | | Factor |
| 0 | 1298.092 | - | - | - | - | - |
| 1 | 919.847 | 29.138 | 2.934 | 1.889 | 72 | 0.841 |
| 2 | 584.900 | 54.941 | 2.935 | 1.889 | 72 | 0.841 |
| | 301.500 | 31.711 | 2.799 | 2.318 | 111 | 0.770 |
| | | | 2.874 | 2.588 | 51 | 0.743 |
| 3 | 344.432 | 73.466 | 2.934 | 1.889 | 72 | 0.841 |
| | | | 2.799 | 2.318 | 111 | 0.770 |
| | | | 2.874 | 2.588 | 51 | 0.743 |
| 4 | 269.671 | 79.225 | 2.669 | 1.709 | 73 | 0.842 |
| | 207.071 | 17.223 | 2.508 | 1.867 | 81 | 0.802 |
| | | | 2.799 | 2.318 | 111 | 0.770 |
| | | | 2.874 | 2.588 | 51 | 0.743 |
| | | | 2.291 | 1.475 | 75 | 0.841 |
| 5 | 212.762 | 83.609 | 2.076 | 1.574 | 81 | 0.797 |
| | | | 1.745 | 1.131 | 92 | 0.839 |
| | | | 2.799 | 2.318 | 111 | 0.770 |

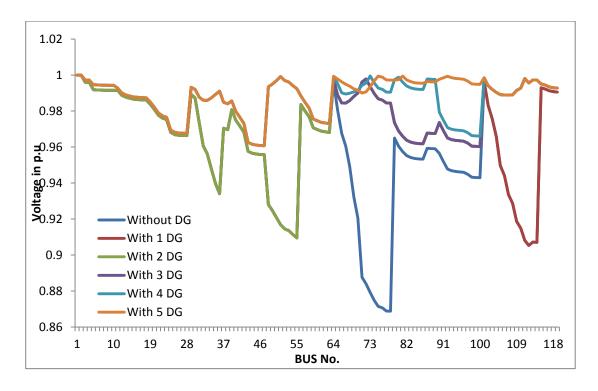


Fig. 4.13. Voltage profile with and without placing Type-3 DG in 119 bus RDS by using TLBO algorithm

CHAPTER-5

OPTIMAL PLACEMENT OF DG USING ARTIFICIAL BEE COLONY ALGORITHM

5.1 INTRODUCTION

This algorithm was introduced by Karaboga in 2005[37]. It is a nature-inspired algorithm based on the foraging behavior of bees. The strategy of this algorithm can be explained by three types of bees i.e. employed bees, onlooker bees and scout bees. Each type of bee performs different function. Every food source is searched by one employed bee. So, number of employed bees is equal to the number of food sources. Food source basically represents the amount of nectar quantity which we can relate with fitness value of the function that is to be optimized. Initially a scout bee goes for a search of nectar or food and saves the location of that food source and becomes an employed bee. The employed bees compare the different nearby available food sources and store the information of the best one. Then these employed bees share the information of the food source through waggle dance. Through their waggle dance onlooker bees judge the quality of nectar and go in search of food suggested by the employed bees. First-half bees are employed bees and second half is onlooker bees. The algorithm is constrained by two factors. The first one is the bee colony size and the second one is the limit i.e. the number of attempts after which employed bee will discard their solution and after which scout bees will generate a new solution. The functioning of these bees can be summarized as follows-:

1. **Employed Bees**-:_Employed bees basically perform exploration of food sources. It had been allocated a location of food resources. They find out food sources in the given search space (means in the neighbourhood of that location also) and share this information with the onlooker bees through waggle dance. The given information includes quantity, distance, and direction of the nectar source.

- 2. **Onlooker Bees**-: Onlooker bees perform exploitation by using the information given by the employed bees. They try to find out food in the region suggested by the employed bees and perform as newly employed bees related to that food source.
- 3. **Scout Bees**-: An employed bee, whose solution has been abandoned after a certain number (LIMIT), becomes a scout bee which randomly generates a new solution in the given range.

Control Parameters-:

LIMIT- no. of the count after which employed bees abandon solution, NUMPOP-no. of population size, CN- Number of the cycle for which the algorithm is to be iterated.

5.2 STEPS OF THE ALGORITHM

5.2.1 Initialization Phase

• Randomly generate initial population by using equation 5.1

$$X0 = X_{LOW} + (X_{UP} - X_{LOW}) * rand(NUMPOP, D)$$
 (5.1)

where X_{LOW} is the lower limit of the solution, X_{UP} is the upper limit of solution and D is the dimension of the problem.

- Calculate the value of the fitness function by using the fitness function evaluating equation specific for a defined problem.
- Set count equals 1.
- Set iteration to 1 and run until iteration equals CN.

5.2.2. Employed Phase

• Generate a new matrix by using X0 matrix with the equation 5.2.

$$V0_{i,j} = X0_{i,j} + (-1,1) * (X0_{i,j} - X0_{k,j})$$
(5.2)

where i varies from 1 to half of the population size, j varies from 1 to dimension and k is any value from 1 to half of the population except i.

- Again calculate fitness function for V0 vector and compare one by one with fitness value of X0 vector.
- If fitness value of the new solution is better than the fitness value of the old solution, then update the old solution with a new one and reset the count otherwise increase the count by 1.

5.2.3. Onlooker Bees

• Onlooker bees decide food source depending on the various information provided by the employed bees. They select the location of a food source and then find out its probability. If the probability is greater than a random value then it generates the new matrix with the help of the previous matrix by using equation 5.2. To find out the probability, equation 5.3 is used or roulette wheel selection method can be used.

$$p_i = \frac{fit_i}{\sum_{i=1}^n fit_i} \tag{5.3}$$

where n is equal to half of the size of the population.

• Then the fitness function of the new generated matrix of onlooker bees is computed. If fitness value of the new solution is better than the fitness value with the old solution, then the old solution is updated with the new one and the count is reset otherwise it is increased by 1.

5.2.4. Scout Bees

• The count number for each solution is checked. If count number exceeds the LIMIT then a new solution is generated and the count is reset to 1.

5.2.5. Termination Phase

• If termination criterion is met then the algorithm stops executing and presents the best solution otherwise it goes to step 2 i.e. employed bee phase and iteration number is increased by 1.

5.3 Implementation of the ABC Algorithm for Optimal Siting and Sizing of DGs

The strategic location of DGs enhances power reliability and reduces the operational costs of the distribution network. For finding out the optimal location and size of the DGs, ABC algorithm has been applied. For this, several case studies are carried out. At first, the placement of Type-1 DGs is considered. Then its two sub-cases are investigated – the first one is for constant load and second one is for varying load throughout the whole day. The second case is for the placement of Type-2 DGs. The third case is for the placement of Type-3 DGs. The given case studies have been implemented in the IEEE 33-bus, 69-bus and 119-bus radial distribution system .Single line diagram of these distribution systems are shown in chapter 4.

5.4 OPTIMAL LOCATION of DGs IN IEEE 33-BUS RDS

5.4.1 Placement of Type-1 DGs in 33 RDS for constant load

TABLE 5.1: Allocation of Type-1 DG in 33 bus RDS by ABC algorithm

| No. of DG | Real Power Loss | Power loss | Location | Size |
|-----------|-----------------|---------------|----------------|-------------------------|
| | (kW) | Reduction (%) | (bus no) | (MW) |
| 0 | 202.677 | - | - | - |
| 1 | 103.966 | 48.70 | 6 | 2.575 |
| 2 | 85.910 | 57.61 | 13 30 | 0.846 1.158 |
| 3 | 71.457 | 64.74 | 14 24 | 0.754 1.099 |
| | | | 7 | 1.071 0.916 |
| 4 | 65.935 | 67.47 | 14 24 31 | 0.585 0.981 0.708 |
| | | | 7 | 0.908 |
| 5 | 64.885 | 67.99 | 14 21 | 0.585 0.277 |
| | | | 24 31 | 0.970 0.708 |

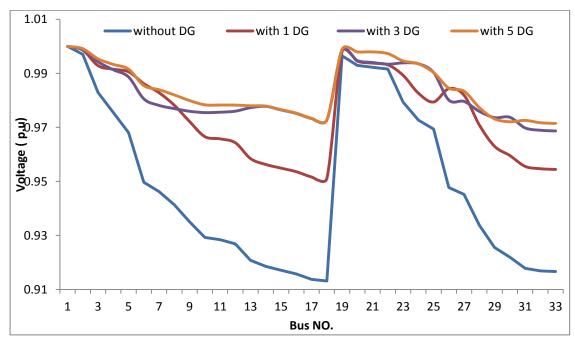


Fig. 5.1. Voltage profile with and without placing Type-1 DGs in 33 bus RDS by using ABC algorithm

5.4.2 Placement of Type1 DGs in 33 bus RDS with varying load

The algorithm has been implemented on 24 hours load data during summer seasons. The 24-hour load data has been taken from [39].

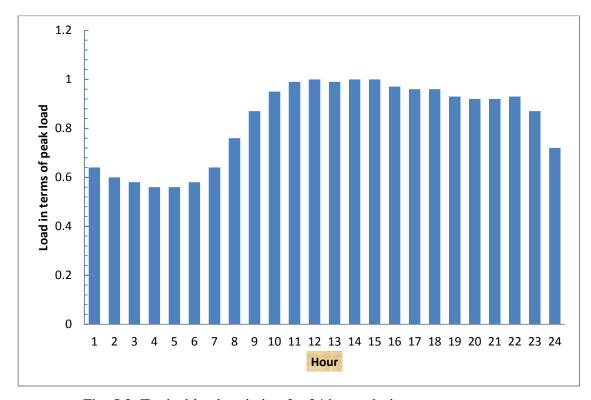


Fig. 5.2. Typical load variation for 24 hours during summer season

For this type of load profile, ABC algorithm has been used to find out the suitable locations and sizes of the DGs and the result has been summarized in table 5.2. For this three cases have been considered. Case 1 is without placing DG, Case 2 is for placing single DG and Case 3 is for placing three DGs. For case 2, optimized location is at bus no. 6 and for case 3, the three optimized locations are at bus nos. 14, 24 and 30. Load in terms of Peak load is considered.

TABLE 5.2: Allocation of Type-1 DGs in 33 bus RDS with varying load by ABC Algorithm

| Power Loss (I-W) DC size (MW) | | | | | | | | |
|-------------------------------|---------|----------------|------------|------------------------|--|--|--|--|
| | 1 | Power Loss (kV | <i>w</i>) | DG size (MW) | | | | |
| Load (p.u.) | Case1 | Case2 | Case3 | Case2 with DG at Bus 6 | Case3with DG at bus 14,24 and 30 | | | |
| 0.56 | 59.541 | 31.488 | 21.813 | 1.407 | 0.419 0.609 0.592 | | | |
| 0.58 | 64.050 | 33.830 | 23.427 | 1.459 | 0.434 0.631 0.614 | | | |
| 0.6 | 68.738 | 36.259 | 25.100 | 1.511 | 0.449 0.653 0.635 | | | |
| 0.64 | 78.655 | 41.383 | 28.627 | 1.615 | 0.479 0.697 0.678 | | | |
| 0.72 | 100.705 | 52.704 | 36.408 | 1.825 | 0.540 0.786 0.765 | | | |
| 0.76 | 112.866 | 58.908 | 40.665 | 1.931 | 0.570 0.830 0.808 | | | |
| 0.87 | 150.356 | 77.872 | 53.650 | 2.224 | 0.654 0.953 0.928 | | | |
| 0.92 | 169.425 | 87.430 | 60.180 | 2.358 | 0.692 1.009 0.983 | | | |
| 0.93 | 173.395 | 89.412 | 61.534 | 2.385 | 0.700 1.021 0.994 | | | |
| 0.95 | 181.493 | 93.450 | 64.289 | 2.439 | 0.716 1.043 1.016 | | | |
| 0.96 | 185.622 | 95.505 | 65.690 | 2.467 | 0.723 1.054 1.027 | | | |
| 0.97 | 189.805 | 97.584 | 67.108 | 2.494 | 0.731 1.066 1.038 | | | |
| 0.99 | 198.332 | 101.814 | 69.991 | 2.548 | 0.746 1.088 1.060 | | | |
| 1 | 202.677 | 103.966 | 71.457 | 2.575 | 0.754 1.099 1.071 | | | |

5.4.3 Placement of Type-2 DG (DSTATCOM) in 33 bus RDS

TABLE 5.3: Allocation of Type-2 DG in 33 bus RDS by ABC algorithm

| No. of DSTATCOM | Real Power Loss (kW) | Power loss Reduction (%) | Location (bus no) | Size (MVAr) |
|--------------------|-------------------------|---------------------------|---------------------------|---|
| 0 | 202.677 | - | _ | - |
| 1 | 143.602 | 29.15 | 30 | 1.252 |
| 2 | 135.753 | 33.02 | 12 30 | 0.469 1.058 |
| 3 | 132.173 | 34.78 | 13 24 30 | 0.378 0.544 1.036 |
| 4 | 130.688 | 35.51 | 7 14 24 30 | 0.442 0.276 0.482 0.904 |
| 5 | 130.315 | 35.70 | 7 14 24 30 32 | 0.442 0.276 0.482 0.709 0.194 |

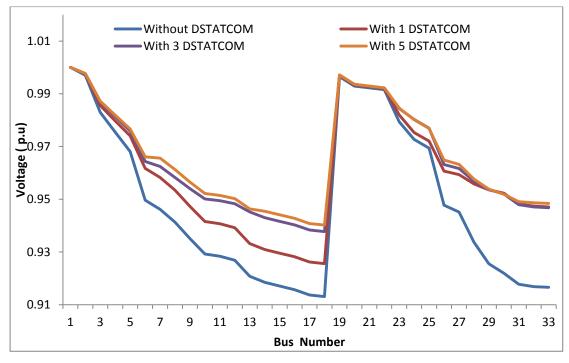


Fig. 5.3. Voltage profile with and without placing Type-2 DG in 33 bus RDS by using ABC algorithm

5.4.4 Placement of Type-3 DG in 33 bus RDS

TABLE 5.4: Allocation of Type-3 DGs in 33 bus RDS by ABC algorithm

| No. of DG | Active Power Loss (kW) | Power loss Reduction (%) | Optima MW | al DG size MVAr | Optimal Location |
|-----------|---------------------------|--------------------------------|---|---|---------------------------|
| 0 | 202.677 | - | - | - | - |
| 1 | 61.363 | 69.72 | 2.545 | 1.750 | 6 |
| 2 | 28.492 | 85.94 | 0.839 1.140 | 0.395 1.065 | 13 30 |
| 3 | 11.629 | 94.26 | 0.747 1.078 1.048 | 0.350 0.521 1.021 | 14 24 30 |
| 4 | 6.427 | 96.83 | 0.788 0.585 0.964 0.788 | 0.376 0.272 0.467 0.896 | 7 14 24 30 |
| 5 | 5.07 | 97.50 | 0.817 0.553 0.957 0.401 0.386 | 0.393 0.259 0.464 0.707 0.189 | 7 15 24 30 32 |

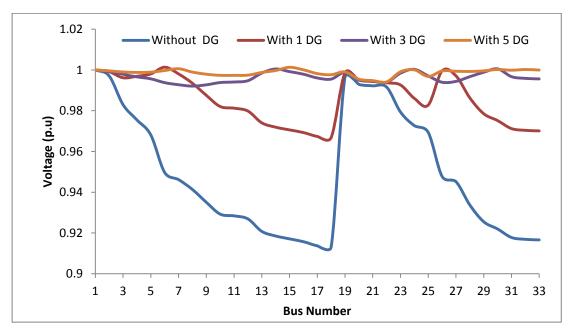


Fig. 5.4. Voltage profile with and without placing Type-3 DG in 33 bus RDS by using ABC algorithm

5.5 OPTIMAL LOCATION FOR 69 BUS RADIAL DISTRIBUTION SYSTEM

5.5.1 Placement of Type-1 DG in 69 bus RDS

TABLE 5.5: Allocation of Type-1 DG in 69 bus RDS by ABC algorithm

| No. of DG | Active Power Loss (kW) | Power loss Reduction (%) | Location | Size (MW) |
|-----------|---------------------------|-----------------------------|----------------------------|---|
| 0 | 224.995 | - | - | - |
| 1 | 83.222 | 63.01 | 61 | 1.873 |
| 2 | 71.675 | 68.14 | 17 61 | .531 1.781 |
| 3 | 69.426 | 69.14 | 11 18 61 | .526 .380 1.719 |
| 4 | 67.917 | 69.81 | 11 18 50 61 | .520 .382 .719 1.719 |
| 5 | 67.372 | 70.06 | 11 18 50 61 64 | 0.526 0.379 0.717 1.427 0.289 |

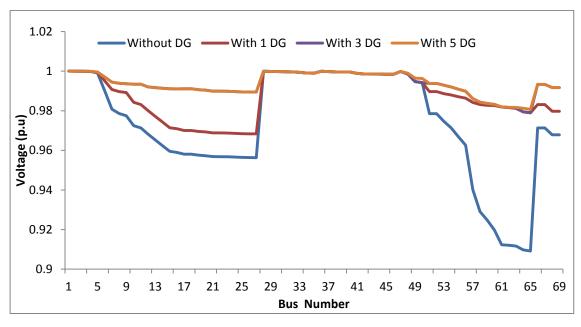


Fig. 5.5. Voltage profile with and without placing Type-1 DG in 69 bus radial distribution system by using ABC algorithm

5.5.2 Placement of Type-2 DGs (DSTATCOMs) in 69 bus RDS with constant load

TABLE 5.6: Allocation of DSTATCOM in 69 bus RDS by ABC algorithm

| No. of DSTATCOM | Active Power Loss (kW) | Power loss Reduction (%) | Location | Size (MVAr) |
|--------------------|-------------------------|--------------------------------|----------------------------|---|
| 0 | 224.995 | - | - | - |
| 1 | 152.039 | 32.43 | 61 | 1.329 |
| 2 | 146.439 | 34.91 | 17 61 | 0.361 1.275 |
| 3 | 145.114 | 35.50 | 11 21 61 | 0.413 0.230 1.232 |
| 4 | 144.331 | 35.85 | 11 21 50 61 | 0.413 0.231 0.517 1.232 |
| 5 | 143.995 | 36.00 | 11 18 50 61 64 | 0.412 0.231 0.517 1.025 0.206 |

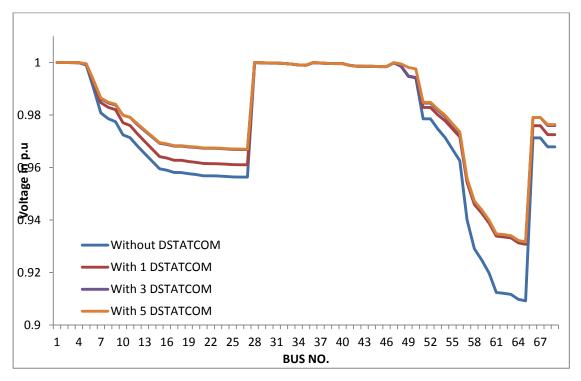


Fig. 5.6. Voltage profile with and without placing Type-2 DG in 69 bus RDS by using ABC algorithm

5.5.3 Placement of Type-2 DGs (DSTATCOM) in 69 bus RDS with varying load

For this case, 24 hours load data is shown in Fig. 5.2.Case 1 is for without any Type-2 DG, Case 2 is for placement of a single Type-2 DG and Case 3 is for placing three Type-2 DGs. For case 2, optimized location is at bus no. 61 and for case 3 three optimized locations are at bus nos. 11, 21 and 61.

TABLE 5.7: Allocation of Type-2 DG (DSTATCOM) in 69 bus RDS for varying load by ABC algorithm

| | Po | wer Loss (k | (W) | DSTATCOM Size (MVAr) | | |
|--------|---------|-------------|---------|----------------------|------------------|--|
| Load | Case1 | Case2 | Case3 | Case 2 with | Case 3 with | |
| (p.u.) | | | | DSTATCOM at | DSTATCOM at | |
| | | | | bus 61 | bus 11,21 and 61 | |
| | | | | | 0.221 | |
| 0.56 | 65.364 | 45.040 | 43.044 | 0.736 | 0.129 | |
| | | | | | 0.680 | |
| | | | | | 0.237 | |
| 0.58 | 70.345 | 48.434 | 46.285 | 0.763 | 0.138 | |
| | | | | | 0.729 | |
| | | | | | 0.237 | |
| 0.6 | 75.527 | 51.960 | 49.653 | 0.789 | 0.138 | |
| | | | | | 0.730 | |
| | | | | | 0.254 | |
| 0.64 | 86.504 | 59.416 | 56.770 | 0.843 | 0.147 | |
| | | | | | 0.779 | |
| | | | | | 0.288 | |
| 0.72 | 110.967 | 75.963 | 72.565 | 0.950 | 0.166 | |
| | | | | | 0.879 | |
| | | | | | 0.306 | |
| 0.76 | 124.490 | 85.073 | 81.258 | 1.004 | 0.175 | |
| | | | | | 0.929 | |
| | | | | | 0.354 | |
| 0.87 | 166.313 | 113.091 | 107.985 | 1.153 | 0.201 | |
| | | | | | 1.067 | |
| | | | | | 0.377 | |
| 0.92 | 187.658 | 127.306 | 121.539 | 1.221 | 0.212 | |
| | | | | | 1.131 | |
| | | | | | 0.381 | |
| 0.93 | 192.109 | 130.267 | 124.357 | 1.234 | 0.214 | |
| | | | | | 0.114 | |
| | | | | | 0.390 | |
| 0.95 | 201.193 | 136.291 | 130.104 | 1.262 | 0.219 | |
| | | | | | 1.169 | |
| | | | | | 0.395 | |
| 0.96 | 205.828 | 139.362 | 133.032 | 1.275 | 0.221 | |
| | | | | | 1.194 | |

| | | | | | 0.399 |
|------|---------|---------|---------|-------|-------|
| 0.97 | 210.525 | 142.473 | 135.996 | 1.289 | 0.224 |
| | | | | | 1.194 |
| | | | | | 0.408 |
| 0.99 | 220.108 | 148.811 | 142.037 | 1.316 | 0.228 |
| | | | | | 1.220 |
| | | | | | 0.413 |
| 1 | 224.995 | 152.038 | 145.113 | 1.330 | 0.231 |
| | | | | | 1.232 |

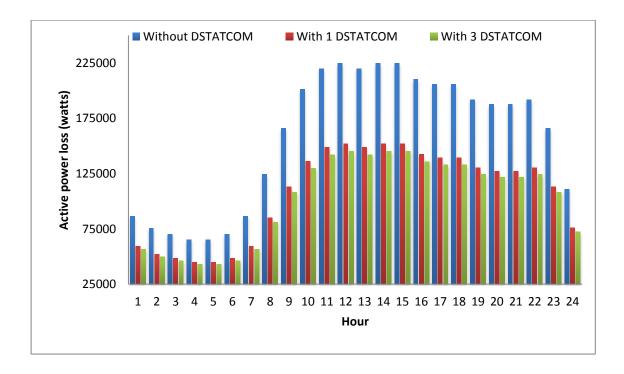


Fig. 5.7. Comparison of active power losses in different cases with 24 hour varying load in case of 69 bus RDS

5.5.4 Placement of Type-3 DGs in 69 bus RDS

TABLE 5.8: Allocation of Type-3 DGs in 69 bus RDS by ABC algorithm

| No. of | Active Power | Power loss | DG | size | DG | Optimal |
|--------|--------------|------------|-------|-------|----------|---------|
| DG | Loss (kW) | Reduction | | | Location | Power |
| | | (%) | MW | MVAr | | Factor |
| 0 | 224.995 | - | - | - | - | - |
| 1 | 23.1709 | 89.701 | 1.828 | 1.301 | 61 | 0.8148 |
| 2 | 7.2041 | | 0.522 | 0.353 | 17 | 0.8282 |
| | | 96.7980 | 1.735 | 1.238 | 61 | 0.8138 |
| | | | 0.494 | 0.354 | 11 | 0.8132 |
| 3 | 4.2677 | 98.1031 | 0.379 | 0.251 | 18 | 0.8332 |
| | | | 1.674 | 1.195 | 61 | 0.8138 |
| | | | 0.494 | 0.353 | 11 | 0.8132 |
| 4 | 1.9951 | 99.1132 | 0.379 | 0.251 | 18 | 0.8332 |
| | | | 0.718 | 0.513 | 50 | 0.8138 |
| | | | 1.674 | 1.195 | 61 | 0.8138 |
| | | | 0.514 | 0.352 | 11 | 0.8246 |
| | | | 0.352 | 0.225 | 21 | 0.8432 |
| 5 | 1.3558 | 99.39 | 0.775 | 0.598 | 49 | 0.7917 |
| | | | 1.321 | 1.075 | 61 | 0.7756 |
| | | | 0.366 | 0.121 | 64 | 0.9494 |

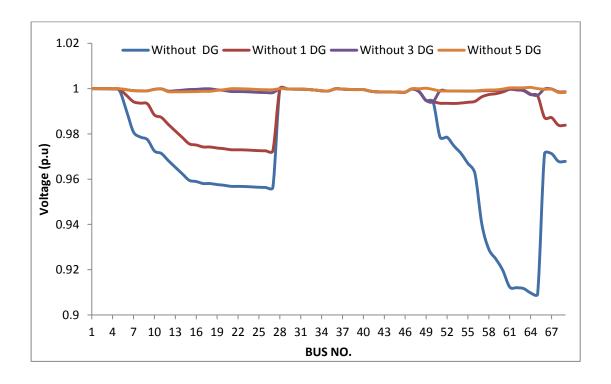


Fig. 5.8. Voltage profile with and without placing Type-3 DG in 69 radial distribution system by using ABC algorithm

5.6 OPTIMAL LOCATIONS FOR 119 BUS RADIAL DISTRIBUTION SYSTEM5.6.1 Placement of Type-1 DGs in 119 bus RD

TABLE 5.9: Allocation of Type-1 DGs in 119 bus RDS by ABC algorithm

| No. Of DG | Active Power Loss (kW) | Power loss Reduction (%) | Location | Size (MW) |
|-----------|------------------------|--------------------------------|-----------------------------|---|
| 0 | 1298.091617 | - | - | - |
| 1 | 1016.75852 | 21.67 | 72 | 2.978 |
| 2 | 805.249 | 37.97 | 72 110 | 2.978 3.119 |
| 3 | 667.294 | 48.59 | 51 72 110 | 2.883 2.978 3.119 |
| 4 | 616.154 | 52.53 | 51 73 97 110 | 2.883 2.606 1.820 3.119 |
| 5 | 574.952 | 55.70 | 51 74 81 97 111 | 2.883 2.417 2.107 1.688 2.869 |

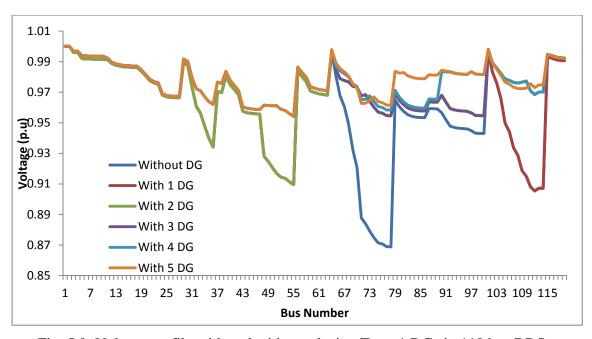


Fig. 5.9. Voltage profile with and without placing Type-1 DGs in 119 bus RDS

5.6.2 Placement of Type-2 DGs (DSTATCOM) in 119 bus RDS

TABLE 5.10: Allocation of Type-2 DGs in 119 bus RDS by ABC algorithm

| No. of DSTATCOM | Real Power Loss (kW) | Power loss Reduction | Location | Size (MVAr) |
|-----------------|----------------------|-------------------------|-----------------------------|---|
| 0 | 1298.092 | (%) | - | - |
| 1 | 1153.301 | 11.15 | 111 | 2.333 |
| 2 | 1027.750 | 20.83 | 72 111 | 1.956 2.333 |
| 3 | 913.060 | 29.66 | 51 72 111 | 2.610 1.956 2.333 |
| 4 | 882.163 | 32.04 | 51 73 81 111 | 2.610 1.781 1.794 2.333 |
| 5 | 861.526 | 33.63 | 51 75 81 97 111 | 2.610 1.538 1.672 1.138 2.333 |

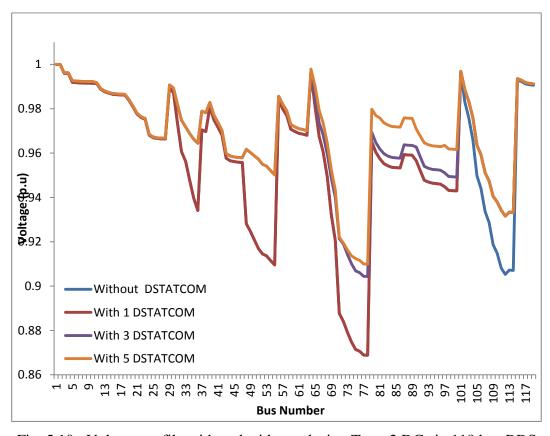


Fig. 5.10. Voltage profile with and without placing Type-2 DGs in 119 bus RDS

5.6.3 Placement of Type-3 DGs in 119 bus RDS

TABLE 5.11: Allocation of Type-3 DGs in 119 bus RDS by ABC algorithm

| No. of DG | Real Power Loss (kW) | Power loss Reduction (%) | DG MW | size MVAr | DG Location | Power Factor |
|--------------|-------------------------|--------------------------------|---|---|-----------------------------|--|
| 0 | 1298.09 | - | - | - | - | - |
| 1 | 919.847 | 29.14 | 2.935 | 1.889 | 72 | 0.8408 |
| 2 | 584.900 | 54.94 | 2.935 2.799 | 1.889 2.318 | 72 111 | 0.8408 0.7702 |
| 3 | 344.432 | 73.47 | 2.874 2.935 2.799 | 2.588 1.889 2.318 | 51 72 111 | 0.7432 0.8408 0.7702 |
| 4 | 269.217 | 79.26 | 2.874 2.680 2.275 2.799 | 2.588 1.716 1.711 2.318 | 51 73 81 111 | 0.7432 0.8421 0.7991 0.7702 |
| 5 | 210.999 | 83.74 | 2.877 2.299 2.089 1.669 2.799 | 2.588 1.479 1.583 1.074 2.318 | 51 75 81 97 111 | 0.7435 0.8410 0.7969 0.8408 0.7702 |

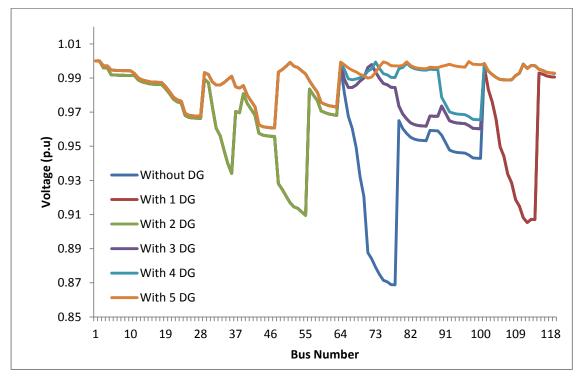


Fig. 5.11. Voltage profile with and without placing Type-3 DGs in 119 bus RDS

CHAPTER-6

PERFORMANCE COMPARISON AND ANALYSIS

6.1 INTRODUCTION

In this chapter, results obtained using TLBO and the ABC have been shown and compared with other techniques like bat algorithm, PSO with constriction factor etc. The results have been categorized into various subsections depending upon the RDS, type, and numbers of DGs. Different comparisons have been done to reflect the efficiency of the algorithm in power loss reduction and voltage profile improvement.

6.2 RESULTS FOR 33 BUS RADIAL DISTRIBUTION SYSTEM

6.2.1 For Type-1 DGs

TABLE 6.1: Comparison of allocation of Type-1 DG in 33 bus RDS by various techniques

| No. of DG | Method | DG | DG Size | Power Losses |
|-----------|-------------|-----------|---------|--------------|
| | | Location | (MW) | (MW) |
| | | (Bus No.) | | |
| | ABC | 6 | 2.575 | 0.104 |
| 1 DG | TLBO | 6 | 2.575 | 0.104 |
| | PSOCFA[40] | 6 | 2.575 | 0.104 |
| | ABC | 14 | 0.754 | 0.071 |
| | | 24 | 1.099 | |
| | | 30 | 1.071 | |
| | | | | |
| | TLBO | 14 | 0.754 | 0.071 |
| 3DG | | 24 | 1.099 | |
| | | 30 | 1.071 | |
| | PSOCFA[40] | 10 | 1.049 | |
| | 1500171[10] | 25 | 0.878 | 0.076 |
| | | 33 | 0.805 | 0.070 |
| | | 7 | 0.909 | |
| | ABC | 14 | 0.585 | |
| | | 21 | 0.277 | |
| | | 24 | 0.970 | 0.065 |
| | | 31 | 0.708 | |
| | | | | |

| 5DG | TLBO | 7 14 21 24 | 0.909 0.585 0.277 0.970 | 0.065 |
|-----|------------|---------------------|----------------------------------|-------|
| | | 31 | 0.708 | |
| | | 4 | 0.517 | |
| | | 15 | 0.584 | |
| | PSOCFA[40] | 25 | 0.727 | 0.066 |
| | | 26 | 0.824 | |
| | | 32 | 0.639 | |

6.2.2 For Type-2 DG

TABLE 6.2: Comparison of allocation of Type-2 DGs in 33 bus RDS by various techniques

| No. of | Method | DSTATCOM | DSTATCOM | Power Losses |
|--------|--------|-----------|-------------|--------------|
| DG | | Location | Size (MVAr) | (MW) |
| | | (Bus No.) | | |
| | ABC | 30 | 1.253 | 0.144 |
| 1 DG | | | | |
| | TLBO | 30 | 1.253 | 0.144 |
| | | | | |
| | ABC | 13 | 0.379 | 0.132 |
| | | 24 | 0.544 | |
| 3DG | | 30 | 1.037 | |
| | | | | |
| | TLBO | 13 | 0.379 | 0.132 |
| | | 24 | 0.544 | |
| | | 30 | 1.037 | |
| | | 7 | 0.442 | |
| | | 14 | 0.277 | |
| | | 24 | 0.482 | |
| | ABC | 30 | 0.709 | 0.130 |
| | | 32 | 0.194 | |
| | | | | |
| 5DG | | 7 | 0.442 | |
| | | 14 | 0.276 | |
| | TLBO | 21 | 0.483 | 0.130 |
| | | 24 | 0.709 | |
| | | 31 | 0.194 | |
| | | | | |

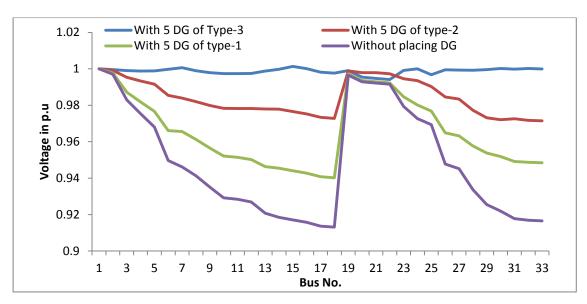


Fig. 6.1. Voltage profile comparison for various cases in 33 bus RDS

6.2.3 For Type-3 DGs

TABLE 6.3: Comparison of allocation of Type-3 DGs in 33 bus RDS by various techniques

| No. of DG | Method | DG Location | DG Size (MW/MVAr) | Power Loss (kW) |
|--------------|--------|----------------|----------------------|-----------------|
| | | (Bus No.) | , | |
| | ABC | 6 | 2.545 / 1.750 | 61.363 |
| 1 DG | TLBO | 6 | 2.545 / 1.750 | 61.363 |
| | ABC | 14 | 0.747 / 0.350 | |
| | | 24 | 1.078 / 0.521 | 11.629 |
| | | 30 | 1.049 / 1.021 | |
| 3DG | | | | |
| | TLBO | 14 | 0.747 / 0.350 | |
| | | 24 | 1.078 / 0.521 | |
| | | 30 | 1.048 / 1.021 | 11.629 |
| | | 7 | 0.817 / 0.393 | |
| | | 15 | 0.553 / 0.259 | |
| | ABC | 24 | 0.957 / 0.464 | |
| | | 30 | 0.401 / 0.707 | 5.073 |
| | | 32 | 0.386 / 0.189 | |
| 5DG | | | | |
| | | 7 | 0.831 / 0.398 | |
| | | 14 | 0.586 / 0.272 | |
| | TLBO | 25 | 0.782 / 0.378 | 5.073 |
| | | 30 | 0.404 / 0.701 | |
| | | 32 | 0.384 / 0.193 | |
| | | | | |

6.3 RESULTS FOR 119 BUS RADIAL DISTRIBUTION SYSTEM

6.3.1 For Type-1 DG

TABLE 6.4: Comparison of allocation of Type-1 DGs in 119 bus RDS by various techniques

| No. of | Method | DG Location | DG Size | Power Losses |
|--------|-----------|-------------|---------|--------------|
| DG | | (Bus No) | (MW) | (MW) |
| | ABC | 72 | 2.979 | 1.017 |
| 1 DG | | | | |
| | TLBO | 72 | 2.979 | 1.017 |
| | | | | |
| | BFA[41] | 93 | 2.871 | 1.017 |
| | ABC | 51 | 2.883 | 0.667 |
| | | 72 | 2.978 | |
| 3DG | | 110 | 3.120 | |
| | | | | |
| | TLBO | 51 | 2.883 | 0.667 |
| | | 72 | 2.978 | |
| | | 110 | 3.120 | |
| | | | | |
| | BFA [41] | 58 | 2.836 | |
| | | 93 | 2.871 | 0.668 |
| | | 115 | 2.769 | |
| | ABC | 51 | 2.883 | |
| 5DG | | 74 | 2.417 | |
| | | 81 | 2.107 | |
| | | 97 | 1.688 | 0.575 |
| | | 111 | 2.869 | |
| | | | • 622 | |
| | | 51 | 2.883 | |
| | TLBO | 73 | 2.533 | 0.5== |
| | | 81 | 2.095 | 0.575 |
| | | 97 | 1.663 | |
| | | 110 | 3.119 | |
| | | ~ 0 | 2.026 | |
| | | 58 | 2.836 | |
| | DE 4 5443 | 70 | 2.075 | 0.555 |
| | BFA [41] | 84 | 1.664 | 0.576 |
| | | 96 | 2.277 | |
| | | 115 | 2.769 | |

6.3.2 For Type-2 DG

TABLE 6.5: Comparison of allocation of Type-2 DGs in 119 bus RDS by various techniques

| No. of | Method | DSTATCOM | DSTATCOM | Power Losses |
|----------|----------|-----------|-------------|--------------|
| DSTATCOM | | Location | Size (MVAr) | (MW) |
| | | (Bus No.) | , , | , , |
| | ABC | 111 | 2.333 | 1.153 |
| 1 | | | | |
| | TLBO | 111 | 2.333 | 1.153 |
| | ABC | 51 | 2.610 | 0.913 |
| | | 72 | 1.956 | |
| 3 | | 111 | 2.333 | |
| | | | | |
| | TLBO | 51 | 2.610 | 0.913 |
| | | 72 | 1.956 | |
| | | 111 | 2.333 | |
| | ABC | 51 | 2.610 | |
| | | 75 | 1.538 | |
| | | 81 | 1.672 | |
| | | 97 | 1.138 | 0.861 |
| | | 111 | 2.331 | |
| | | | | |
| | | 51 | 2.610 | |
| 5 | TLBO | 75 | 1.538 | |
| | | 81 | 1.672 | 0.861 |
| | | 97 | 1.138 | |
| | | 110 | 2.333 | |
| | | | | |
| | | 38 | 2.514 | |
| | | 46 | 1.425 | |
| | BFOA[30] | 74 | 1.521 | 0.871 |
| | | 91 | 1.715 | |
| | | 118 | 2.021 | |

6.3.3 For Type-3 DG

TABLE 6.6: Comparison of allocation of Type-3 DGs in 119 bus RDS by various techniques

| No. of DG | Method | DG | DG Size | Power Loss |
|-----------|------------|----------|----------------|------------|
| | | Location | (MW)/p.f | (MW) |
| | ABC | 72 | 2.935 / 0.841 | 0.919 |
| 1 DG | | | | |
| | TLBO | 72 | 2.935 / 0.841 | 0.919 |
| | ABC | 51 | 2.874 / 0.7432 | 0.344 |
| | | 72 | 2.935 / 0.841 | |
| | | 111 | 2.799 / 0.770 | |
| 3DG | | | | |
| | TLBO | 51 | 2.874 / 0.743 | 0.344 |
| | | 72 | 2.935 / 0.841 | |
| | | 111 | 2.799 / 0.770 | |
| | ABC | 51 | 2.877 / 0.743 | |
| | | 75 | 2.299 / 0.841 | |
| | | 81 | 2.088 / 0.797 | |
| | | 97 | 1.669 / 0.841 | 0.211 |
| | | 111 | 2.799 /0.770 | |
| | | | | |
| | | 51 | 2.874 / 0.743 | |
| | TLBO | 75 | 2.291 / 0.841 | |
| 5DG | | 81 | 2.0761 / 0.797 | 0.213 |
| | | 97 | 1.745 / 0.839 | |
| | | 110 | 2.799 / 0.770 | |
| | | 20 | 2 052 10 56 | |
| | | 38 | 2.952 / 0.76 | |
| | DEO 4 (20) | 46 | 2.141 / 0.83 | 0.220 |
| | BFOA[30] | 74 | 2.803 / 0.84 | 0.229 |
| | | 91 | 2.346 / 0.79 | |
| | | 118 | 3.029 / 0.77 | |

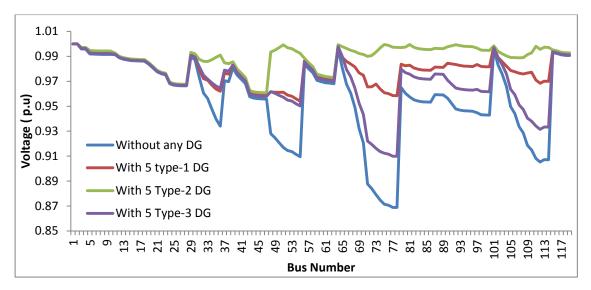


Fig. 6.2. Voltage profile comparison for various cases in 119 bus RDS

6.4 CONVERGENCE COMPARISON OF TLBO and ABC

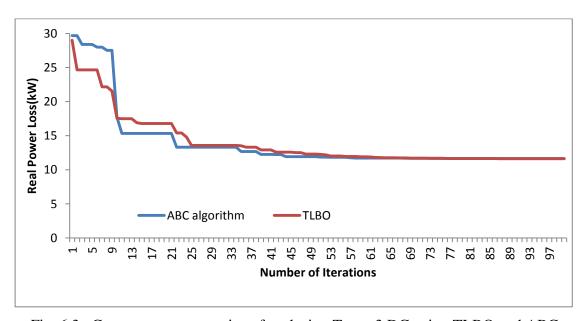


Fig. 6.3. Convergence comparison for placing Type- 3 DG using TLBO and ABC

It is observed from fig. 6.3 that TLBO algorithm shows continuous convergence towards final solution while ABC algorithm is showing abrupt changes in convergence graph due to exploration nature of scout bee phase.

This behaviour of TLBO algorithm is due to its nature of equation (4.2) which enable it to move towards mean of the all vectors which helps in providing final solution with continuous change towards converged solution.

6.4 CONCLUSIONS

This work presents the implementation of ABC algorithm and TLBO for optimal allocation of different types of DGs in radial distribution systems (RDS) which resulted in active power loss reduction and bus voltage profile improvement. The proposed algorithm was implemented for allocation of DGs in the IEEE 33-bus, 69-bus and 119-bus radial bus distribution systems. Results show that the best result is obtained when Type-3 DGs are connected. As an example, by installing 5 Type-1 DGs in the 119 bus RDS, the active power losses are reduced by 55.70 %. When 5 Type-3 DGs are installed, the same losses are reduced by 83.74%.

ABC and TLBO both presented good results when compared to other techniques but ABC is slightly superior to TLBO when the system is more complex like 119 bus system as TLBO has only two phases which are related to exploration but not in exploitation while ABC is also good in exploration also.

APPENDIX

TABLE A.1: Bus Data for 33bus radial distribution system

| Branch | Sending | Receiving | R | X |
|--------|---------|-----------|--------|--------|
| No. | Bus | Bus | (ohm) | (ohm) |
| 1 | 1 | 2 | 0.0922 | 0.047 |
| 2 | 2 | 3 | 0.493 | 0.2511 |
| 3 | 3 | 4 | 0.366 | 0.1864 |
| 4 | 4 | 5 | 0.3811 | 0.1941 |
| 5 | 5 | 6 | 0.819 | 0.707 |
| 6 | 6 | 7 | 0.1872 | 0.6188 |
| 7 | 7 | 8 | 0.7114 | 0.2351 |
| 8 | 8 | 9 | 1.03 | 0.74 |
| 9 | 9 | 10 | 1.044 | 0.74 |
| 10 | 10 | 11 | 0.1966 | 0.065 |
| 11 | 11 | 12 | 0.3744 | 0.1238 |
| 12 | 12 | 13 | 1.468 | 1.155 |
| 13 | 13 | 14 | 0.5416 | 0.7129 |
| 14 | 14 | 15 | 0.591 | 0.526 |
| 15 | 15 | 16 | 0.7463 | 0.545 |
| 16 | 16 | 17 | 1.289 | 1.721 |
| 17 | 17 | 18 | 0.732 | 0.574 |
| 18 | 2 | 19 | 0.164 | 0.1565 |
| 19 | 19 | 20 | 1.5042 | 1.3554 |
| 20 | 20 | 21 | 0.4095 | 0.4784 |
| 21 | 21 | 22 | 0.7089 | 0.9373 |
| 22 | 3 | 23 | 0.4512 | 0.3083 |
| 23 | 23 | 24 | 0.898 | 0.7091 |
| 24 | 24 | 25 | 0.896 | 0.7011 |
| 25 | 6 | 26 | 0.203 | 0.1034 |
| 26 | 26 | 27 | 0.2842 | 0.1447 |
| 27 | 27 | 28 | 1.059 | 0.9337 |
| 28 | 28 | 29 | 0.8042 | 0.7006 |
| 29 | 29 | 30 | 0.5075 | 0.2585 |
| 30 | 30 | 31 | 0.9744 | 0.963 |
| 31 | 31 | 32 | 0.3105 | 0.3619 |
| 32 | 32 | 33 | 0.341 | 0.5302 |

TABLE A.2: Load Data for 33bus radial distribution system

| BUS NO. | . LOAD | |
|---------|--------|-------|
| | kW | kVAR |
| 1 | 0 | 0 |
| 2 | 0.1 | 0.06 |
| 3 | 0.09 | 0.04 |
| 4 | 0.12 | 0.08 |
| 5 | 0.06 | 0.03 |
| 6 | 0.06 | 0.02 |
| 7 | 0.2 | 0.1 |
| 8 | 0.2 | 0.1 |
| 9 | 0.06 | 0.02 |
| 10 | 0.06 | 0.02 |
| 11 | 0.045 | 0.03 |
| 12 | 0.06 | 0.035 |
| 13 | 0.06 | 0.035 |
| 14 | 0.12 | 0.08 |
| 15 | 0.06 | 0.01 |
| 16 | 0.06 | 0.02 |
| 17 | 0.06 | 0.02 |
| 18 | 0.09 | 0.04 |
| 19 | 0.09 | 0.04 |
| 20 | 0.09 | 0.04 |
| 21 | 0.09 | 0.04 |
| 22 | 0.09 | 0.04 |
| 23 | 0.09 | 0.05 |
| 24 | 0.42 | 0.2 |
| 25 | 0.42 | 0.2 |
| 26 | 0.06 | 0.025 |
| 27 | 0.06 | 0.025 |
| 28 | 0.06 | 0.02 |
| 29 | 0.12 | 0.07 |
| 30 | 0.2 | 0.6 |
| 31 | 0.15 | 0.07 |
| 32 | 0.21 | 0.1 |
| 33 | 0.06 | 0.04 |

TABLE A.3: Bus Data for 69 bus radial distribution system

| Branch | Sending | Receiving | R | X |
|--------|---------|-----------|--------|--------|
| No. | Bus | Bus | (ohm) | (ohm) |
| 1 | 1 | 2 | 0.0005 | 0.0012 |
| 2 | 2 | 3 | 0.0005 | 0.0012 |
| 3 | 3 | 4 | 0.0015 | 0.0036 |
| 4 | 4 | 5 | 0.0251 | 0.0294 |
| 5 | 5 | 6 | 0.366 | 0.1864 |
| 6 | 6 | 7 | 0.3811 | 0.1941 |
| 7 | 7 | 8 | 0.0922 | 0.047 |
| 8 | 8 | 9 | 0.0493 | 0.0251 |
| 9 | 9 | 10 | 0.819 | 0.2707 |
| 10 | 10 | 11 | 0.1872 | 0.0619 |
| 11 | 11 | 12 | 0.7114 | 0.2351 |
| 12 | 12 | 13 | 1.03 | 0.34 |
| 13 | 13 | 14 | 1.044 | 0.345 |
| 14 | 14 | 15 | 1.058 | 0.3496 |
| 15 | 15 | 16 | 0.1966 | 0.065 |
| 16 | 16 | 17 | 0.3744 | 0.1238 |
| 17 | 17 | 18 | 0.0047 | 0.0016 |
| 18 | 18 | 19 | 0.3276 | 0.1083 |
| 19 | 19 | 20 | 0.2106 | 0.0696 |
| 20 | 20 | 21 | 0.3416 | 0.1129 |
| 21 | 21 | 22 | 0.014 | 0.0046 |
| 22 | 22 | 23 | 0.1591 | 0.0526 |
| 23 | 23 | 24 | 0.3463 | 0.1145 |
| 24 | 24 | 25 | 0.7488 | 0.2475 |
| 25 | 25 | 26 | 0.3089 | 0.1021 |
| 26 | 26 | 27 | 0.1732 | 0.0572 |
| 27 | 3 | 28 | 0.0044 | 0.0108 |
| 28 | 28 | 29 | 0.064 | 0.1565 |
| 29 | 29 | 30 | 0.3978 | 0.1315 |
| 30 | 30 | 31 | 0.0702 | 0.0232 |
| 31 | 31 | 32 | 0.351 | 0.116 |
| 32 | 32 | 33 | 0.839 | 0.2816 |
| 33 | 33 | 34 | 1.708 | 0.5646 |
| 34 | 34 | 35 | 1.474 | 0.4873 |
| 35 | 3 | 36 | 0.0044 | 0.0108 |
| 36 | 36 | 37 | 0.064 | 0.1565 |
| 37 | 37 | 38 | 0.1053 | 0.123 |
| 38 | 38 | 39 | 0.0304 | 0.0355 |
| 39 | 39 | 40 | 0.0018 | 0.0021 |
| 40 | 40 | 41 | 0.7283 | 0.8509 |

| 41 | 41 | 42 | 0.31 | 0.3623 |
|---------------------------------------|---------|----|--------|--------|
| 42 | 42 | 43 | 0.041 | 0.0478 |
| 43 | 43 | 44 | 0.0092 | 0.0116 |
| 44 | 44 | 45 | 0.1089 | 0.1373 |
| 45 | 45 | 46 | 0.0009 | 0.0012 |
| 46 | 4 | 47 | 0.0034 | 0.0084 |
| 47 | 47 | 48 | 0.0851 | 0.2083 |
| 48 | 48 | 49 | 0.2898 | 0.7091 |
| 49 | 49 | 50 | 0.0822 | 0.2011 |
| 50 | 8 | 51 | 0.0928 | 0.0473 |
| 51 | 51 | 52 | 0.3319 | 0.1114 |
| 52 | 9 | 53 | 0.174 | 0.0886 |
| 53 | 53 | 54 | 0.203 | 0.1034 |
| 54 | 54 | 55 | 0.284 | 0.1447 |
| 55 | 55 | 56 | 0.2813 | 0.1433 |
| 56 | 56 | 57 | 1.59 | 0.5337 |
| 57 | 57 | 58 | 0.7837 | 0.263 |
| 58 | 58 | 59 | 0.3042 | 0.1006 |
| 59 | 59 | 60 | 0.3861 | 0.1172 |
| 60 | 60 | 61 | 0.5075 | 0.2585 |
| 61 | 61 | 62 | 0.0974 | 0.0496 |
| 62 | 62 | 63 | 0.145 | 0.0738 |
| 63 | 63 | 64 | 0.7105 | 0.3619 |
| 64 | 64 | 65 | 1.041 | 0.5302 |
| 65 | 11 | 66 | 0.2012 | 0.0611 |
| 66 | 66 | 67 | 0.0047 | 0.0014 |
| 67 | 12 | 68 | 0.7394 | 0.2444 |
| 68 | 68 | 69 | 0.0047 | 0.0016 |
| · · · · · · · · · · · · · · · · · · · | <u></u> | · | | |

TABLE A.4: Load Data for 69 bus radial distribution system

| BUS NO. | LC | OAD |
|---------|--------|--------|
| | kW | kVAr |
| 1 | 0 | 0 |
| 2 | 0 | 0 |
| 3 | 0 | 0 |
| 4 | 0 | 0 |
| 5 | 0 | 0 |
| 6 | 0.0026 | 0.0022 |
| 7 | 0.0404 | 0.03 |
| 8 | 0.075 | 0.054 |
| 9 | 0.03 | 0.022 |
| 10 | 0.028 | 0.019 |
| 11 | 0.145 | 0.104 |
| 12 | 0.145 | 0.104 |

| 12 | 0.000 | 0.0055 |
|----|---------|---------|
| 13 | 0.008 | 0.0055 |
| 14 | 0.008 | 0.0055 |
| 15 | 0 | 0 |
| 16 | 0.0455 | 0.03 |
| 17 | 0.06 | 0.035 |
| 18 | 0.06 | 0.035 |
| 19 | 0 | 0 |
| 20 | 0.001 | 0.0006 |
| 21 | 0.114 | 0.081 |
| 22 | 0.0053 | 0.0035 |
| 23 | 0 | 0 |
| 24 | 0.028 | 0.02 |
| 25 | 0 | 0 |
| 26 | 0.014 | 0.01 |
| 27 | 0.014 | 0.01 |
| 28 | 0.026 | 0.0186 |
| 29 | 0.026 | 0.0186 |
| 30 | 0 | 0 |
| 31 | 0 | 0 |
| 32 | 0 | 0 |
| 33 | 0.014 | 0.01 |
| 34 | 0.0195 | 0.014 |
| 35 | 0.006 | 0.004 |
| 36 | 0.026 | 0.01855 |
| 37 | 0.026 | 0.01855 |
| 38 | 0 | 0 |
| 39 | 0.024 | 0.017 |
| 40 | 0.024 | 0.017 |
| 41 | 0.0012 | 0.001 |
| 42 | 0 | 0 |
| 43 | 0.006 | 0.0043 |
| 44 | 0 | 0 |
| 45 | 0.03922 | 0.0263 |
| 46 | 0.03922 | 0.0263 |
| 47 | 0 | 0 |
| 48 | 0.079 | 0.0564 |
| 49 | 0.3847 | 0.2745 |
| 50 | 0.3847 | 0.2745 |
| 51 | 0.0405 | 0.0283 |
| 52 | 0.0036 | 0.0027 |
| 53 | 0.00435 | 0.0035 |
| 54 | 0.0264 | 0.019 |
| 55 | 0.024 | 0.0172 |
| 56 | 0 | 0 |
| 57 | 0 | 0 |
| L | ı | |

| 58 | 0 | 0 |
|----|-------|-------|
| 59 | 0.1 | 0.072 |
| 60 | 0 | 0 |
| 61 | 1.244 | 0.888 |
| 62 | 0.032 | 0.023 |
| 63 | 0 | 0 |
| 64 | 0.227 | 0.162 |
| 65 | 0.059 | 0.042 |
| 66 | 0.018 | 0.013 |
| 67 | 0.018 | 0.013 |
| 68 | 0.028 | 0.02 |
| 69 | 0.028 | 0.02 |

TABLE A.5: Bus Data for 119 bus radial distribution system

| Branch | Sending | Receiving | R | X |
|--------|---------|-----------|-------|---------|
| No. | Bus | Bus | (ohm) | (ohm) |
| 1 | 1 | 2 | 0 | 0 |
| 2 | 2 | 3 | 0.036 | 0.01296 |
| 3 | 3 | 4 | 0.033 | 0.01188 |
| 4 | 3 | 5 | 0.045 | 0.0162 |
| 5 | 5 | 6 | 0.015 | 0.054 |
| 6 | 6 | 7 | 0.015 | 0.054 |
| 7 | 7 | 8 | 0.015 | 0.0125 |
| 8 | 8 | 9 | 0.018 | 0.014 |
| 9 | 9 | 10 | 0.021 | 0.063 |
| 10 | 3 | 11 | 0.166 | 0.1344 |
| 11 | 11 | 12 | 0.112 | 0.0789 |
| 12 | 12 | 13 | 0.187 | 0.313 |
| 13 | 13 | 14 | 0.142 | 0.1512 |
| 14 | 14 | 15 | 0.18 | 0.118 |
| 15 | 15 | 16 | 0.15 | 0.045 |
| 16 | 16 | 17 | 0.16 | 0.18 |
| 17 | 17 | 18 | 0.157 | 0.171 |
| 18 | 12 | 19 | 0.218 | 0.285 |
| 19 | 19 | 20 | 0.118 | 0.185 |
| 20 | 20 | 21 | 0.16 | 0.196 |
| 21 | 21 | 22 | 0.12 | 0.189 |
| 22 | 22 | 23 | 0.12 | 0.0789 |
| 23 | 23 | 24 | 1.41 | 0.723 |
| 24 | 24 | 25 | 0.293 | 0.1348 |
| 25 | 25 | 26 | 0.133 | 0.104 |
| 26 | 26 | 27 | 0.178 | 0.134 |
| 27 | 27 | 28 | 0.178 | 0.134 |

| 28 5 29 0.015 0.0296 29 29 30 0.012 0.02766 30 30 31 0.12 0.2766 31 31 32 0.21 0.243 32 32 33 0.12 0.054 33 33 34 0.178 0.234 34 34 35 0.178 0.234 35 35 36 0.154 0.162 36 31 37 0.187 0.261 37 37 38 0.133 0.099 38 30 39 0.33 0.194 40 40 41 0.13 0.194 41 41 42 0.28 0.15 42 42 43 1.18 0.85 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 | | | | | |
|--|----|----|----|-------|---------|
| 30 30 31 0.12 0.2766 31 31 32 0.21 0.243 32 32 33 0.12 0.054 33 34 0.178 0.234 34 34 35 0.178 0.234 35 35 36 0.154 0.162 36 31 37 0.187 0.261 37 37 38 0.133 0.099 38 30 39 0.33 0.194 40 40 41 0.13 0.194 41 41 42 0.28 0.15 42 42 43 1.18 0.85 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 | 28 | 5 | 29 | 0.015 | 0.0296 |
| 31 31 32 0.21 0.243 32 32 33 0.12 0.054 33 33 34 0.178 0.234 34 34 35 0.154 0.162 36 31 37 0.187 0.261 37 37 38 0.133 0.099 38 30 39 0.33 0.194 40 40 41 0.13 0.194 41 41 42 0.28 0.15 42 42 43 1.18 0.85 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 49 49 | 29 | 29 | 30 | 0.012 | 0.0276 |
| 32 32 33 0.12 0.054 33 33 34 0.178 0.234 34 34 35 0.178 0.234 35 35 36 0.154 0.162 36 31 37 0.187 0.261 37 37 38 0.133 0.099 38 30 39 0.33 0.194 40 40 41 0.13 0.194 40 40 41 0.13 0.194 41 41 42 0.28 0.15 42 42 43 1.18 0.85 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 | 30 | 30 | 31 | 0.12 | 0.2766 |
| 33 33 34 0.178 0.234 34 34 35 0.178 0.234 35 35 36 0.154 0.162 36 31 37 0.187 0.261 37 37 38 0.133 0.099 38 30 39 0.33 0.194 40 40 41 0.13 0.194 40 40 41 0.13 0.194 41 41 42 0.28 0.15 42 42 43 1.18 0.85 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 50 50 | 31 | 31 | 32 | 0.21 | 0.243 |
| 34 34 35 0.178 0.234 35 35 36 0.154 0.162 36 31 37 0.187 0.261 37 37 38 0.133 0.099 38 30 39 0.33 0.194 39 39 40 0.31 0.194 40 40 41 0.13 0.194 40 40 41 0.13 0.194 41 41 42 0.28 0.15 42 42 43 1.18 0.85 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 50 50 | 32 | 32 | 33 | 0.12 | 0.054 |
| 35 35 36 0.154 0.162 36 31 37 0.187 0.261 37 37 38 0.133 0.099 38 30 39 0.33 0.194 39 39 40 0.31 0.194 40 40 41 0.13 0.194 41 41 42 0.28 0.15 42 42 43 1.18 0.85 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 49 49 50 0.15 0.0987 50 50 51 0.15 0.0987 51 51 | 33 | 33 | 34 | 0.178 | 0.234 |
| 36 31 37 0.187 0.261 37 37 38 0.133 0.099 38 30 39 0.33 0.194 39 39 40 0.31 0.194 40 40 41 0.13 0.194 41 41 42 0.28 0.15 42 42 43 1.18 0.85 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 49 49 50 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 | 34 | 34 | 35 | 0.178 | 0.234 |
| 37 37 38 0.133 0.099 38 30 39 0.33 0.194 39 39 40 0.31 0.194 40 40 41 0.13 0.194 41 41 42 0.28 0.15 42 42 43 1.18 0.85 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 49 49 50 0.15 0.0987 50 50 51 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 | 35 | 35 | 36 | 0.154 | 0.162 |
| 38 30 39 0.33 0.194 39 39 40 0.31 0.194 40 40 41 0.13 0.194 41 41 42 0.28 0.15 42 42 43 1.18 0.85 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 49 49 50 0.15 0.0987 50 50 51 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 | 36 | 31 | 37 | 0.187 | 0.261 |
| 39 39 40 0.31 0.194 40 40 41 0.13 0.194 41 41 42 0.28 0.15 42 42 43 1.18 0.85 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 49 49 50 0.15 0.0987 50 50 51 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 <td>37</td> <td>37</td> <td>38</td> <td>0.133</td> <td>0.099</td> | 37 | 37 | 38 | 0.133 | 0.099 |
| 40 40 41 0.13 0.194 41 41 42 0.28 0.15 42 42 43 1.18 0.85 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 49 49 50 0.15 0.0987 50 50 51 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 </td <td>38</td> <td>30</td> <td>39</td> <td>0.33</td> <td>0.194</td> | 38 | 30 | 39 | 0.33 | 0.194 |
| 41 41 42 0.28 0.15 42 42 43 1.18 0.85 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 49 49 50 0.15 0.0987 50 50 51 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 57 | 39 | 39 | 40 | 0.31 | 0.194 |
| 42 42 43 1.18 0.85 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 49 49 50 0.15 0.0987 50 50 51 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 57 58 0.406 0.1461 58 <td< td=""><td>40</td><td>40</td><td>41</td><td>0.13</td><td>0.194</td></td<> | 40 | 40 | 41 | 0.13 | 0.194 |
| 43 43 44 0.42 0.2436 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 49 49 50 0.15 0.0987 50 50 51 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 57 58 0.406 0.1461 58 58 59 0.706 0.5461 59 | 41 | 41 | 42 | 0.28 | 0.15 |
| 44 44 45 0.27 0.0972 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 49 49 50 0.15 0.0987 50 50 51 0.15 0.0987 50 50 51 0.15 0.0987 50 50 51 0.15 0.0987 50 50 51 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 <t< td=""><td>42</td><td>42</td><td>43</td><td>1.18</td><td>0.85</td></t<> | 42 | 42 | 43 | 1.18 | 0.85 |
| 45 45 46 0.339 0.1221 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 49 49 50 0.15 0.0987 50 50 51 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 57 58 0.406 0.1461 58 58 59 0.706 0.5461 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 | 43 | 43 | 44 | 0.42 | 0.2436 |
| 46 46 47 0.27 0.1779 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 49 49 50 0.15 0.0987 50 50 51 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 57 58 0.406 0.1461 58 58 59 0.706 0.5461 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 | 44 | 44 | 45 | 0.27 | 0.0972 |
| 47 36 48 0.21 0.1383 48 48 49 0.12 0.0789 49 49 50 0.15 0.0987 50 50 51 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 57 58 0.406 0.1461 58 58 59 0.706 0.5461 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 | 45 | 45 | 46 | 0.339 | 0.1221 |
| 48 48 49 0.12 0.0789 49 49 50 0.15 0.0987 50 50 51 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 57 58 0.406 0.1461 58 58 59 0.706 0.5461 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 | 46 | 46 | 47 | 0.27 | 0.1779 |
| 49 49 50 0.15 0.0987 50 50 51 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 57 58 0.406 0.1461 58 58 59 0.706 0.5461 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 | 47 | 36 | 48 | 0.21 | 0.1383 |
| 50 50 51 0.15 0.0987 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 57 58 0.406 0.1461 58 58 59 0.706 0.5461 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 | 48 | 48 | 49 | 0.12 | 0.0789 |
| 51 51 52 0.24 0.1581s 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 57 58 0.406 0.1461 58 58 59 0.706 0.5461 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 | 49 | 49 | 50 | 0.15 | 0.0987 |
| 52 52 53 0.12 0.0789 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 57 58 0.406 0.1461 58 58 59 0.706 0.5461 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 69 | 50 | 50 | 51 | 0.15 | 0.0987 |
| 53 53 54 0.405 0.1458 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 57 58 0.406 0.1461 58 58 59 0.706 0.5461 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 69 69 70 0.406 0.1461 | 51 | 51 | 52 | 0.24 | 0.1581s |
| 54 54 55 0.405 0.1458 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 57 58 0.406 0.1461 58 58 59 0.706 0.5461 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 52 | 52 | 53 | 0.12 | 0.0789 |
| 55 30 56 0.391 0.141 56 56 57 0.406 0.1461 57 57 58 0.406 0.1461 58 58 59 0.706 0.5461 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 53 | 53 | 54 | 0.405 | 0.1458 |
| 56 56 57 0.406 0.1461 57 57 58 0.406 0.1461 58 58 59 0.706 0.5461 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 54 | 54 | 55 | 0.405 | 0.1458 |
| 57 57 58 0.406 0.1461 58 58 59 0.706 0.5461 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 55 | 30 | 56 | 0.391 | 0.141 |
| 58 58 59 0.706 0.5461 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 56 | 56 | 57 | 0.406 | 0.1461 |
| 59 59 60 0.338 0.1218 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 57 | 57 | 58 | 0.406 | 0.1461 |
| 60 60 61 0.338 0.1218 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 58 | 58 | 59 | 0.706 | 0.5461 |
| 61 61 62 0.207 0.0747 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 59 | 59 | 60 | 0.338 | 0.1218 |
| 62 62 63 0.247 0.8922 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 60 | 60 | 61 | 0.338 | 0.1218 |
| 63 2 64 0.028 0.0418 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 61 | 61 | 62 | 0.207 | 0.0747 |
| 64 64 65 0.117 0.2016 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 62 | 62 | 63 | 0.247 | 0.8922 |
| 65 65 66 0.255 0.0918 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 63 | 2 | 64 | 0.028 | 0.0418 |
| 66 66 67 0.21 0.0759 67 67 68 0.383 0.138 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 64 | 64 | 65 | 0.117 | 0.2016 |
| 67 67 68 0.383 0.138 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 65 | 65 | 66 | 0.255 | 0.0918 |
| 68 68 69 0.504 0.3303 69 69 70 0.406 0.1461 | 66 | 66 | 67 | 0.21 | 0.0759 |
| 69 69 70 0.406 0.1461 | 67 | 67 | 68 | 0.383 | 0.138 |
| | 68 | 68 | 69 | 0.504 | 0.3303 |
| 70 71 0.962 0.761 | 69 | 69 | 70 | 0.406 | 0.1461 |
| | 70 | 70 | 71 | 0.962 | 0.761 |

| 71 71 72 0.165 0.06 72 72 73 0.303 0.1092 73 73 74 0.303 0.1092 74 74 75 0.206 0.144 75 75 76 0.233 0.084 76 76 77 0.591 0.1773 77 77 78 0.126 0.0453 78 65 79 0.559 0.3687 79 79 80 0.186 0.1227 80 80 81 0.186 0.1227 81 81 82 0.26 0.139 82 82 83 0.154 0.148 83 83 84 0.23 0.128 84 84 85 0.252 0.106 |
|---|
| 73 73 74 0.303 0.1092 74 74 75 0.206 0.144 75 75 76 0.233 0.084 76 76 77 0.591 0.1773 77 77 78 0.126 0.0453 78 65 79 0.559 0.3687 79 79 80 0.186 0.1227 80 80 81 0.186 0.1227 81 81 82 0.26 0.139 82 82 83 0.154 0.148 83 83 84 0.23 0.128 84 84 85 0.252 0.106 |
| 74 74 75 0.206 0.144 75 75 76 0.233 0.084 76 76 77 0.591 0.1773 77 77 78 0.126 0.0453 78 65 79 0.559 0.3687 79 79 80 0.186 0.1227 80 80 81 0.186 0.1227 81 81 82 0.26 0.139 82 82 83 0.154 0.148 83 83 84 0.23 0.128 84 84 85 0.252 0.106 |
| 75 75 76 0.233 0.084 76 76 77 0.591 0.1773 77 77 78 0.126 0.0453 78 65 79 0.559 0.3687 79 79 80 0.186 0.1227 80 80 81 0.186 0.1227 81 81 82 0.26 0.139 82 82 83 0.154 0.148 83 83 84 0.23 0.128 84 84 85 0.252 0.106 |
| 76 76 77 0.591 0.1773 77 77 78 0.126 0.0453 78 65 79 0.559 0.3687 79 79 80 0.186 0.1227 80 80 81 0.186 0.1227 81 81 82 0.26 0.139 82 82 83 0.154 0.148 83 83 84 0.23 0.128 84 84 85 0.252 0.106 |
| 77 77 78 0.126 0.0453 78 65 79 0.559 0.3687 79 79 80 0.186 0.1227 80 80 81 0.186 0.1227 81 81 82 0.26 0.139 82 82 83 0.154 0.148 83 83 84 0.23 0.128 84 84 85 0.252 0.106 |
| 78 65 79 0.559 0.3687 79 79 80 0.186 0.1227 80 80 81 0.186 0.1227 81 81 82 0.26 0.139 82 82 83 0.154 0.148 83 83 84 0.23 0.128 84 84 85 0.252 0.106 |
| 79 79 80 0.186 0.1227 80 80 81 0.186 0.1227 81 81 82 0.26 0.139 82 82 83 0.154 0.148 83 83 84 0.23 0.128 84 84 85 0.252 0.106 |
| 80 80 81 0.186 0.1227 81 81 82 0.26 0.139 82 82 83 0.154 0.148 83 83 84 0.23 0.128 84 84 85 0.252 0.106 |
| 81 81 82 0.26 0.139 82 82 83 0.154 0.148 83 83 84 0.23 0.128 84 84 85 0.252 0.106 |
| 82 82 83 0.154 0.148 83 83 84 0.23 0.128 84 84 85 0.252 0.106 |
| 83 83 84 0.23 0.128 84 84 85 0.252 0.106 |
| 84 84 85 0.252 0.106 |
| |
| |
| 85 85 86 0.18 0.148 |
| 86 80 87 0.16 0.182 |
| 87 87 88 0.2 0.23 |
| 88 88 89 0.16 0.393 |
| 89 66 90 0.669 0.2412 |
| 90 90 91 0.266 0.1227 |
| 91 91 92 0.266 0.1227 |
| 92 92 93 0.266 0.1227 |
| 93 93 94 0.266 0.1227 |
| 94 94 95 0.233 0.115 |
| 95 95 96 0.496 0.138 |
| 96 92 97 0.196 0.18 |
| 97 97 98 0.196 0.18 |
| 98 98 99 0.1866 0.122 |
| 99 99 100 0.0746 0.318 |
| 100 2 101 0.0625 0.0265 |
| 101 101 102 0.1501 0.234 |
| 102 102 103 0.1347 0.0888 |
| 103 103 104 0.2307 0.1203 |
| 104 104 105 0.447 0.1608 |
| 105 105 106 0.1632 0.0588 |
| 106 106 107 0.33 0.099 |
| 107 107 108 0.156 0.0561 |
| 108 108 109 0.3819 0.1374 |
| 109 109 110 0.1626 0.0585 |
| 110 110 111 0.3819 0.1374 |
| 111 111 112 0.2445 0.0879 |
| 112 111 113 0.2088 0.0753 |
| 113 113 114 0.2301 0.0828 |

| 114 | 101 | 115 | 0.6102 | 0.2196 |
|-----|-----|-----|--------|--------|
| 115 | 115 | 116 | 0.1866 | 0.127 |
| 116 | 116 | 117 | 0.3732 | 0.246 |
| 117 | 117 | 118 | 0.405 | 0.367 |
| 118 | 118 | 119 | 0.489 | 0.438 |

TABLE A.6: Load Data for 119 bus radial distribution system

| BUS | L | OAD |
|-----|----------|----------|
| NO. | kW | kVAr |
| 1 | 0 | 0 |
| 2 | 0 | 0 |
| 3 | 0.13384 | 0.10114 |
| 4 | 0.016214 | 0.011292 |
| 5 | 0.034315 | 0.021845 |
| 6 | 0.073016 | 0.063602 |
| 7 | 0.1442 | 0.068604 |
| 8 | 0.10447 | 0.061725 |
| 9 | 0.028547 | 0.011503 |
| 10 | 0.08756 | 0.051073 |
| 11 | 0.1982 | 0.10677 |
| 12 | 0.1468 | 0.075995 |
| 13 | 0.02604 | 0.018687 |
| 14 | 0.0521 | 0.02322 |
| 15 | 0.1419 | 0.1175 |
| 16 | 0.02187 | 0.02879 |
| 17 | 0.03337 | 0.02645 |
| 18 | 0.03243 | 0.02523 |
| 19 | 0.020234 | 0.011906 |
| 20 | 0.15694 | 0.078523 |
| 21 | 0.54629 | 0.3514 |
| 22 | 0.18031 | 0.1642 |
| 23 | 0.093167 | 0.054594 |
| 24 | 0.08518 | 0.03965 |
| 25 | 0.1681 | 0.095178 |
| 26 | 0.12511 | 0.15022 |
| 27 | 0.01603 | 0.02462 |
| 28 | 0.02603 | 0.02462 |
| 29 | 0.59456 | 0.52262 |
| 30 | 0.12062 | 0.059117 |
| 31 | 0.10238 | 0.099554 |
| 32 | 0.5134 | 0.3185 |
| 33 | 0.47525 | 0.45614 |

| 35 0.20538 0.083302 36 0.1316 0.093082 37 0.4484 0.36979 38 0.44052 0.32164 39 0.11254 0.055134 40 0.053963 0.038998 41 0.39305 0.3426 42 0.32674 0.27856 43 0.53626 0.24024 44 0.076247 0.066562 45 0.05352 0.03976 46 0.040328 0.031964 47 0.039653 0.020758 48 0.066195 0.042361 49 0.073904 0.051653 50 0.11477 0.057965 51 0.91837 1.2051 52 0.2103 0.14666 53 0.06668 0.056608 54 0.042207 0.040184 56 0.0621 0.02686 57 0.09246 0.08838 58 0.085188 0.0554 | 34 | 0.15143 | 0.13679 |
|--|--|----------|----------|
| 36 0.1316 0.093082 37 0.4484 0.36979 38 0.44052 0.32164 39 0.11254 0.055134 40 0.053963 0.038998 41 0.39305 0.3426 42 0.32674 0.27856 43 0.53626 0.24024 44 0.076247 0.066562 45 0.05352 0.03976 46 0.040328 0.031964 47 0.039653 0.020758 48 0.066195 0.042361 49 0.073904 0.051653 50 0.11477 0.057965 51 0.91837 1.2051 52 0.2103 0.14666 53 0.06668 0.056608 54 0.042207 0.040184 55 0.43374 0.28341 56 0.0621 0.02686 57 0.09246 0.08838 58 0.085188 0.05543 | | | |
| 37 0.4484 0.36979 38 0.44052 0.32164 39 0.11254 0.055134 40 0.053963 0.038998 41 0.39305 0.3426 42 0.32674 0.27856 43 0.53626 0.24024 44 0.076247 0.066562 45 0.05352 0.03976 46 0.040328 0.031964 47 0.039653 0.020758 48 0.066195 0.042361 49 0.073904 0.051653 50 0.11477 0.057965 51 0.91837 1.2051 52 0.2103 0.14666 53 0.06668 0.056608 54 0.042207 0.040184 55 0.43374 0.28341 56 0.0621 0.02686 57 0.09246 0.08838 58 0.085188 0.055436 59 0.3453 0.3224< | | | |
| 38 0.44052 0.32164 39 0.11254 0.055134 40 0.053963 0.038998 41 0.39305 0.3426 42 0.32674 0.27856 43 0.53626 0.24024 44 0.076247 0.066562 45 0.05352 0.03976 46 0.040328 0.031964 47 0.039653 0.020758 48 0.066195 0.042361 49 0.073904 0.051653 50 0.11477 0.057965 51 0.91837 1.2051 52 0.2103 0.14666 53 0.06668 0.056608 54 0.042207 0.040184 55 0.43374 0.28341 56 0.0621 0.02686 57 0.09246 0.08838 58 0.085188 0.055436 59 0.3453 0.3324 60 0.0225 0.01683< | <u> </u> | | |
| 39 0.11254 0.055134 40 0.053963 0.038998 41 0.39305 0.3426 42 0.32674 0.27856 43 0.53626 0.24024 44 0.076247 0.066562 45 0.05352 0.03976 46 0.040328 0.031964 47 0.039653 0.020758 48 0.066195 0.042361 49 0.073904 0.051653 50 0.11477 0.057965 51 0.91837 1.2051 52 0.2103 0.14666 53 0.06668 0.056608 54 0.042207 0.040184 55 0.43374 0.28341 56 0.0621 0.02866 57 0.09246 0.08838 58 0.085188 0.055436 59 0.3453 0.3324 60 0.0225 0.01683 61 0.080551 0.04915 | - | | |
| 40 0.053963 0.038998 41 0.39305 0.3426 42 0.32674 0.27856 43 0.53626 0.24024 44 0.076247 0.066562 45 0.05352 0.03976 46 0.040328 0.031964 47 0.039653 0.020758 48 0.066195 0.042361 49 0.073904 0.051653 50 0.11477 0.057965 51 0.91837 1.2051 52 0.2103 0.14666 53 0.06668 0.056608 54 0.042207 0.040184 55 0.43374 0.28341 56 0.0621 0.02686 57 0.09246 0.08838 58 0.085188 0.055436 59 0.3453 0.3324 60 0.0225 0.01683 61 0.080551 0.049156 62 0.09586 0.09075 | | | |
| 41 0.39305 0.3426 42 0.32674 0.27856 43 0.53626 0.24024 44 0.076247 0.066562 45 0.05352 0.03976 46 0.040328 0.031964 47 0.039653 0.020758 48 0.066195 0.042361 49 0.073904 0.051653 50 0.11477 0.057965 51 0.91837 1.2051 52 0.2103 0.14666 53 0.06668 0.056608 54 0.042207 0.040184 55 0.43374 0.28341 56 0.0621 0.02686 57 0.09246 0.08838 58 0.085188 0.055436 59 0.3453 0.3324 60 0.0225 0.01683 61 0.080551 0.049156 62 0.09586 0.090758 63 0.06292 0.04477< | | | |
| 42 0.32674 0.27856 43 0.53626 0.24024 44 0.076247 0.066562 45 0.05352 0.03976 46 0.040328 0.031964 47 0.039653 0.020758 48 0.066195 0.042361 49 0.073904 0.051653 50 0.11477 0.057965 51 0.91837 1.2051 52 0.2103 0.14666 53 0.06668 0.056608 54 0.042207 0.040184 55 0.43374 0.28341 56 0.0621 0.02686 57 0.09246 0.08838 58 0.085188 0.055436 59 0.3453 0.3324 60 0.0225 0.01683 61 0.080551 0.049156 62 0.09586 0.090758 63 0.06292 0.0477 64 0.4788 0.46374 </td <td>-</td> <td></td> <td></td> | - | | |
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| 71 0.4675 0.39514 72 0.59485 0.23974 73 0.1325 0.084363 74 0.052699 0.022482 | | | |
| 72 0.59485 0.23974 73 0.1325 0.084363 74 0.052699 0.022482 | <u> </u> | | |
| 73 0.1325 0.084363 74 0.052699 0.022482 | | | |
| 74 0.052699 0.022482 | 72 | 0.59485 | 0.23974 |
| | 73 | 0.1325 | 0.084363 |
| | 74 | 0.052699 | 0.022482 |
| 75 0.86979 0.614775 | 75 | 0.86979 | 0.614775 |
| 76 0.031349 0.029817 | 76 | 0.031349 | 0.029817 |
| 77 0.19239 0.12243 | 77 | 0.19239 | 0.12243 |
| 78 0.06575 0.04537 | 78 | 0.06575 | 0.04537 |

| 79 | 0.23815 | 0.22322 |
|------------------------------|----------|--------------------|
| 80 | 0.29455 | 0.22322 |
| 81 | | |
| h | 0.48557 | 0.43792 0.18303 |
| 82 | 0.24353 | 0.18303 |
| + - - - - - - - - - - | 0.24353 | |
| 84 | 0.13425 | 0.11929 |
| 85 | 0.02271 | 0.02796 |
| 86 | 0.049513 | 0.026515 |
| 87 | 0.38378 | 0.25716 |
| 88 | 0.04964 | 0.0206 |
| 89 | 0.022473 | 0.011806 |
| 90 | 0.06293 | 0.04296 |
| 91 | 0.03067 | 0.03493 |
| 92 | 0.06253 | 0.06679 |
| 93 | 0.11457 | 0.081748 |
| 94 | 0.081292 | 0.066526 |
| 95 | 0.031733 | 0.01596 |
| 96 | 0.03332 | 0.06048 |
| 97 | 0.53128 | 0.22485 |
| 98 | 0.50703 | 0.36742 |
| 99 | 0.02639 | 0.0117 |
| 100 | 0.04599 | 0.030392 |
| 101 | 0.10066 | 0.047572 |
| 102 | 0.45648 | 0.3503 |
| 103 | 0.52256 | 0.44929 |
| 104 | 0.40843 | 0.16846 |
| 105 | 0.14148 | 0.13425 |
| 106 | 0.10443 | 0.066024 |
| 107 | 0.096793 | 0.083647 |
| 108 | 0.49392 | 0.41934 |
| 109 | 0.22538 | 0.13588 |
| 110 | 0.50921 | 0.38721 |
| 111 | 0.1885 | 0.17346 |
| 112 | 0.91803 | 0.89855 |
| 113 | 0.30508 | 0.21537 |
| 114 | 0.05438 | 0.04097 |
| 115 | 0.21114 | 0.1929 |
| 116 | 0.067009 | 0.053336 |
| 117 | 0.16207 | 0.090321 |
| 118 | 0.048785 | 0.029156 |
| 119 | 0.0339 | 0.01898 |

TABLE A.7: Hourly Peak Load In Terms Of Daily Peak Load

| Hour Hourly load in terms of peak load 12-1 am 0.64 1-2 0.60 2-3 0.58 3-4 0.56 4-5 0.56 5-6 0.58 6-7 0.64 7-8 0.76 8-9 0.87 9-10 0.95 10-11 0.99 11-12pm 1.00 12pm-1 0.99 1-2 1.00 2-3 1.00 3-4 0.97 4-5 0.96 |
|---|
| 1-2 0.60 2-3 0.58 3-4 0.56 4-5 0.56 5-6 0.58 6-7 0.64 7-8 0.76 8-9 0.87 9-10 0.95 10-11 0.99 11-12pm 1.00 12pm-1 0.99 1-2 1.00 2-3 1.00 3-4 0.97 |
| 2-3 0.58 3-4 0.56 4-5 0.56 5-6 0.58 6-7 0.64 7-8 0.76 8-9 0.87 9-10 0.95 10-11 0.99 11-12pm 1.00 12pm-1 0.99 1-2 1.00 2-3 1.00 3-4 0.97 |
| 3-4 0.56 4-5 0.56 5-6 0.58 6-7 0.64 7-8 0.76 8-9 0.87 9-10 0.95 10-11 0.99 11-12pm 1.00 12pm-1 0.99 1-2 1.00 2-3 1.00 3-4 0.97 |
| 4-5 0.56 5-6 0.58 6-7 0.64 7-8 0.76 8-9 0.87 9-10 0.95 10-11 0.99 11-12pm 1.00 12pm-1 0.99 1-2 1.00 2-3 1.00 3-4 0.97 |
| 5-6 0.58 6-7 0.64 7-8 0.76 8-9 0.87 9-10 0.95 10-11 0.99 11-12pm 1.00 12pm-1 0.99 1-2 1.00 2-3 1.00 3-4 0.97 |
| 6-7 0.64 7-8 0.76 8-9 0.87 9-10 0.95 10-11 0.99 11-12pm 1.00 12pm-1 0.99 1-2 1.00 2-3 1.00 3-4 0.97 |
| 7-8 0.76 8-9 0.87 9-10 0.95 10-11 0.99 11-12pm 1.00 1-2 1.00 2-3 1.00 3-4 0.97 |
| 8-9 9-10 0.95 10-11 0.99 11-12pm 1.00 1-2 1.00 2-3 1.00 3-4 0.97 |
| 9-10 0.95 10-11 0.99 11-12pm 1.00 12pm-1 0.99 1-2 1.00 2-3 1.00 3-4 0.97 |
| 10-11 0.99 11-12pm 1.00 12pm-1 0.99 1-2 1.00 2-3 1.00 3-4 0.97 |
| 11-12pm 1.00 12pm-1 0.99 1-2 1.00 2-3 1.00 3-4 0.97 |
| 12pm-1 0.99 1-2 1.00 2-3 1.00 3-4 0.97 |
| 1-2 1.00 2-3 1.00 3-4 0.97 |
| 2-3 3-4 1.00 0.97 |
| 3-4 0.97 |
| |
| 4-5 0.96 |
| |
| 5-6 0.96 |
| 6-7 0.93 |
| 7-8 0.92 |
| 8-9 0.92 |
| 9-10 0.93 |
| 10-11 0.87 |
| 11-12 0.72 |

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