

MODEL REDUCTION OF DISCRETE TIME CONTROL SYSTEMS

A DISSERTATION

Submitted in Partial Fulfillment of the Requirement
For the Award of degree of

MASTER OF ENGINEERING

In

(CONTROL & INSTRUMENTATION)



by

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CERTIFICATE

This is to certify that the thesis entitled “**MODEL REDUCTION OF DISCRETE TIME SYSTEMS**” carried out by Anjali kalra(13/C&I/08) for the partial fulfilment of the requirements for the degree of **MASTER OFTECHNOLOGY (Control & Instrumentation)** is a bonafide record of the work done by the candidate under my guidance. To the best of my knowledge, this work has not been submitted for the award of any other degree.

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